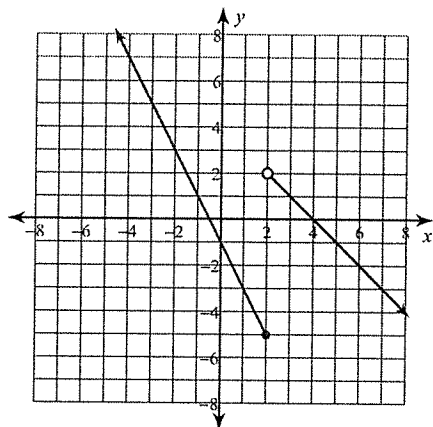


Piecewise Functions

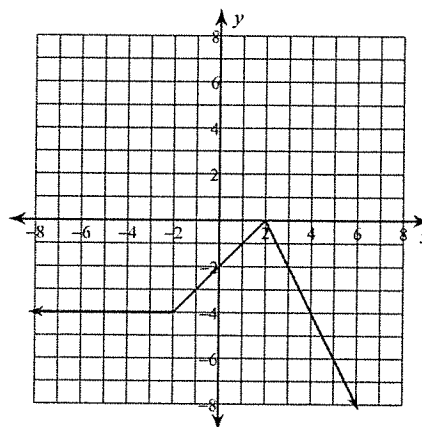
Date _____ Period _____

Sketch the graph of each function.

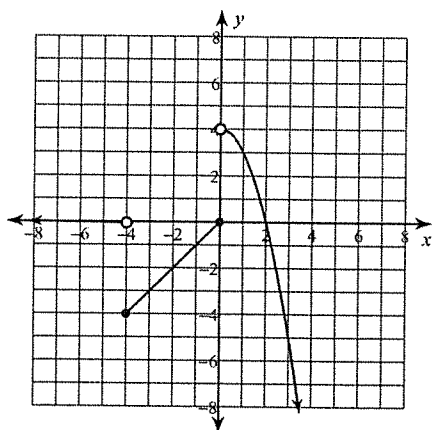
$$1) f(x) = \begin{cases} -2x - 1, & x \leq 2 \\ -x + 4, & x > 2 \end{cases}$$



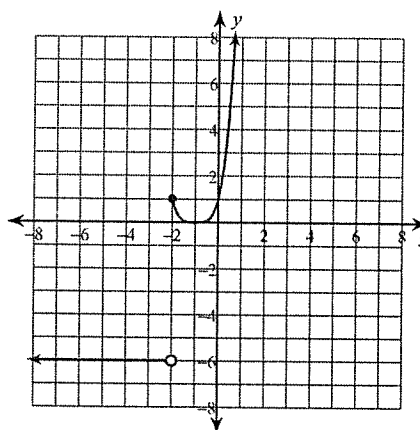
$$2) f(x) = \begin{cases} -4, & x \leq -2 \\ x - 2, & -2 < x < 2 \\ -2x + 4, & x \geq 2 \end{cases}$$



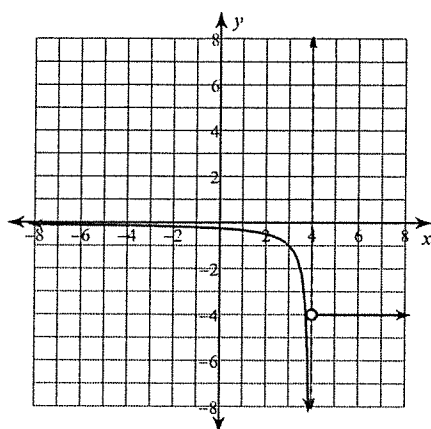
$$3) f(x) = \begin{cases} -2^x, & x < -4 \\ -|x|, & -4 \leq x \leq 0 \\ 4 - x^2, & x > 0 \end{cases}$$



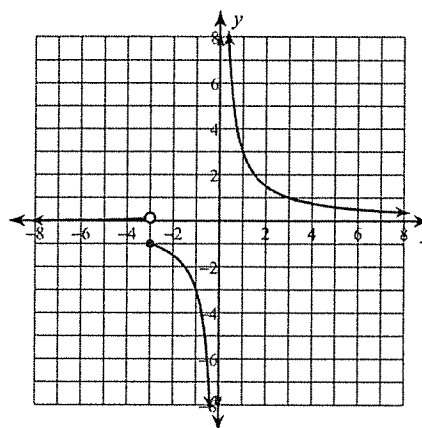
$$4) g(x) = \begin{cases} -6, & x < -2 \\ (x+1)^4, & x \geq -2 \end{cases}$$



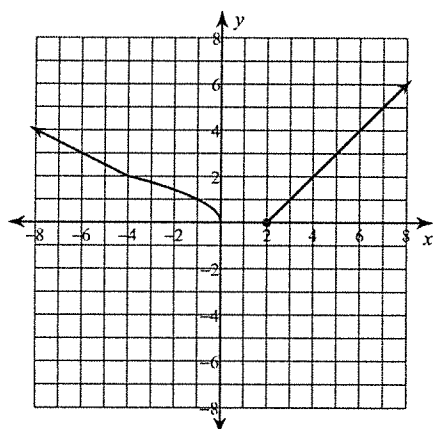
$$5) f(x) = \begin{cases} \frac{1}{x-4}, & x \leq 4 \\ -4, & x > 4 \end{cases}$$



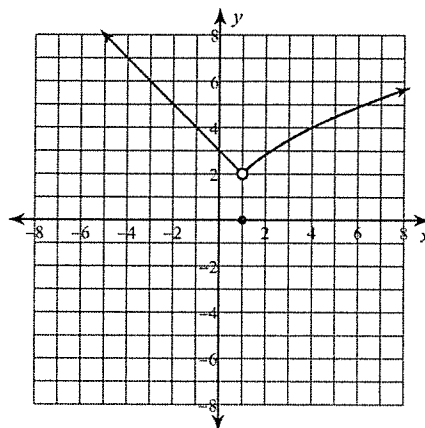
$$6) h(x) = \begin{cases} 2^x, & x < -3 \\ \frac{3}{x}, & x \geq -3 \end{cases}$$



$$7) w(x) = \begin{cases} \frac{|x|}{2}, & x \leq -4 \\ \sqrt{-x}, & -4 < x < 2 \\ |x-2|, & x \geq 2 \end{cases}$$



$$8) w(x) = \begin{cases} |x-3|, & x < 1 \\ (x-1)^4, & x = 1 \\ \sqrt{4x}, & x > 1 \end{cases}$$

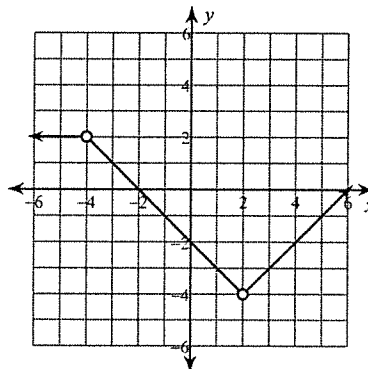


Critical thinking questions:

- 9) Write a rule for the sign function $s(n)$:
 $s(n)$ is -1 when n is negative, $+1$ when n is positive, and 0 otherwise.

$$s(n) = \begin{cases} -1, & n < 0 \\ 0, & n = 0 \\ 1, & n > 0 \end{cases}$$

- 10) Write a rule for the function shown.



$$f(x) = \begin{cases} 2, & x < -4 \\ -x-2, & -4 < x < 2 \\ x-6, & x > 2 \end{cases}$$

Answers to Assignment (ID: 4)

1) $a^3 - 1$

2) $-27n^2 + 36n - 9$

3) $6a - 4$

4) $-12x - 3$

5) $-4x - 1$

6) No

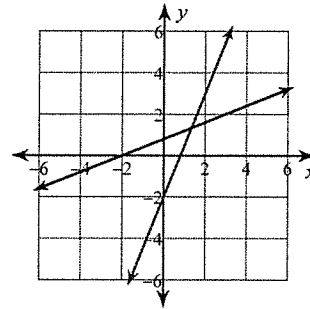
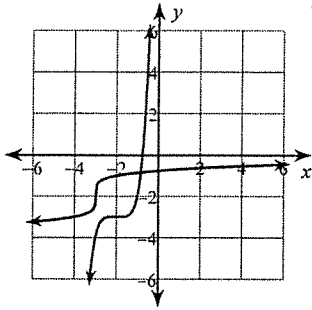
7) No

8)

9)

$g^{-1}(x) = (x + 2)^5 - 3$

$f^{-1}(x) = -2 + \frac{5}{2}x$



10) $g^{-1}(n) = -n - 3$

11) $f^{-1}(x) = 2x + 6$

12) $h^{-1}(n) = \frac{4}{n-2} - 1$

13) $f^{-1}(x) = -\frac{3}{x+1} + 2$

Answers to Assignment (ID: 3)

1) $2x - 3$

2) $6n - 6$

3) $n + 6$

4) $8x + 11$

5) $-n^3 + 3n^2 + 4$

6) No

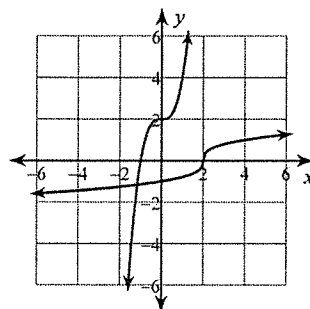
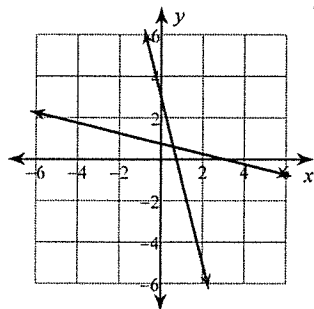
7) No

8)

9)

$h^{-1}(n) = -4n + 3$

$g^{-1}(n) = 2n^3 + 2$



10) $f^{-1}(x) = \frac{4}{x-1} + 2$

11) $f^{-1}(n) = -2n^5 - 3$

12) $g^{-1}(x) = \frac{3}{x-2} + 1$

13) $f^{-1}(x) = \sqrt[3]{x} + 2$

Answers to Assignment (ID: 2)

1) $-2t - 5$

4) $12x^2 - 19$

8)

2) $-9x^3 + 6x^2 + 1$

5) $n - 8$

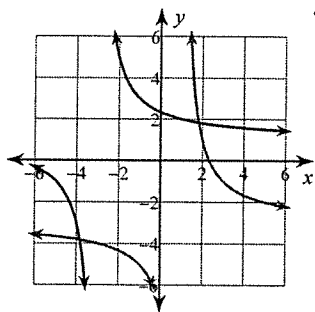
3) $-64n^3 + 96n^2 - 48n + 10$

6) No

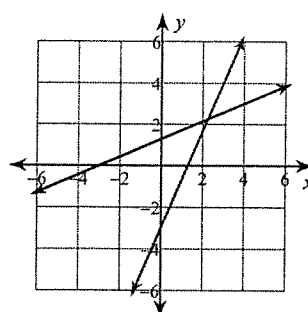
7) Yes

9)

$$g^{-1}(x) = \frac{4}{x-1} - 3$$



$$f^{-1}(n) = -3 + \frac{7}{3}n$$



10) $g^{-1}(n) = -2n^3$

11) $h^{-1}(n) = \frac{2}{n-1} + 2$

12) $g^{-1}(x) = \sqrt[3]{\frac{x}{2}}$

13) $f^{-1}(x) = \sqrt[3]{x}$

Answers to Assignment (ID: 1)

1) $-27n^2 - 90n - 77$

2) $8n^3 - 24n^2 + 14n + 2$

3) $9x^2 - 15x + 6$

4) $-6n - 1$

5) $4a^3 - 4a + 5$

6) Yes

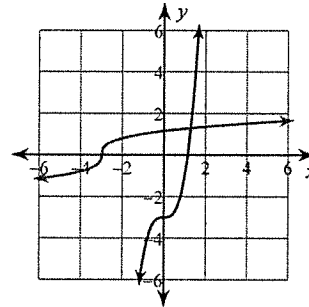
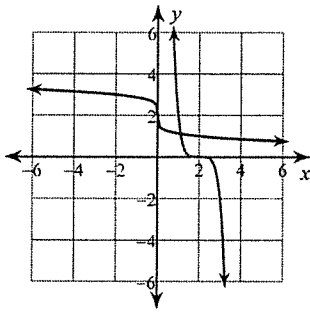
7) No

8)

9)

$f^{-1}(x) = -2(x - 2)^5$

$f^{-1}(n) = \sqrt[3]{\frac{n+3}{2}}$



10) $h^{-1}(x) = 2 - \frac{4}{3}x$

11) $g^{-1}(x) = \sqrt[3]{\frac{-x-1}{2}}$

12) $f^{-1}(n) = -\frac{3}{n-1} - 2$

13) $f^{-1}(n) = \frac{1}{3}n + \frac{2}{3}$