Lesson 8

Objective: Use the area model and multiplication to show the equivalence of two fractions.

Suggested Lesson Structure

Total Time	(60 minutes)
Student Debrief	(10 minutes)
Concept Development	(34 minutes)
Application Problem	(4 minutes)
Fluency Practice	(12 minutes)

Fluency Practice (12 minutes)

•	Multiply Mentally 4.0A.4	(4 minutes)
•	Count by Equivalent Fractions 3.NF.3	(4 minutes)

Multiply Mentally (4 minutes)

Draw Equivalent Fractions 4.NF.1

Materials: (S) Personal white board

Note: This fluency activity reviews Module 3 content.

- T: (Write $32 \times 3 =$.) Say the multiplication sentence.
- S: 32 × 3 = 96.
- T: (Write $32 \times 3 = 96$. Below it, write $32 \times 20 =$ ____.) Say the multiplication sentence.
- S: 32 × 20 = 640.
- T: (Write $32 \times 20 = 640$. Below it, write $32 \times 23 =$.) On your personal white board, solve 32×23 .

(4 minutes)

S: (Write 32 × 23 = 736.)

Continue with the following possible sequence: 42×2 , 42×20 , 42×22 ; and 21×4 , 21×40 , 21×44 .

Count by Equivalent Fractions (4 minutes)

Note: This fluency activity reviews Lesson 4.

- T: Count by twos to 12. Start at 0.
- S: 0, 2, 4, 6, 8, 10, 12.



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- T: Count by 2 thirds to 12 thirds. Start at 0 thirds. (Write as students count.)
- s. 0 2 4 6 8 10 12

5.	3'3'3'3'3'3'3'							
T:	1 is the same as how many thirds?	$\frac{0}{3}$	$\frac{2}{3}$	$\frac{4}{3}$	<u>6</u> 3	<u>8</u> 3	$\frac{10}{3}$	$\frac{12}{3}$
S:	3 thirds.		2	4		o	10	
T:	2 is the same as how many thirds?	0	<u>-</u> 3	4 3	2	8 3	$\frac{10}{3}$	4
S:	6 thirds.							

- T: (Beneath $\frac{6}{3}$, write 2.) 3 is the same as how many thirds?
- S: 9 thirds.
- T: 4 is the same as how many thirds?
- S: 12 thirds.
- T: (Beneath $\frac{12}{3}$, write 4.) Count by 2 thirds again. This time, say the whole numbers when you arrive at them. Start at zero.
- S: $0, \frac{2}{3}, \frac{4}{3}, 2, \frac{8}{3}, \frac{10}{3}, 4.$

Repeat the process, counting by 2 sixths to 18 sixths.

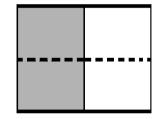
Draw Equivalent Fractions (4 minutes)

Materials: (S) Personal white board

Note: This fluency activity reviews Lesson 7.

- T: (Write $\frac{1}{2}$.) Say the fraction.
- S: 1 half.
- T: On your personal white board, draw a model to show $\frac{1}{2}$.
- S: (Draw a model partitioned into 2 equal units. Shade 1 unit.)
- T: (Write $\frac{1}{2} = \frac{\times}{\times} = \frac{1}{4}$.) Draw a dotted horizontal line to find the equivalent fraction. Then, complete the number sentence.
- S: (Draw a dotted horizontal line, breaking 2 units into 4 smaller units. Write $\frac{1}{2} = \frac{1 \times 2}{2 \times 2} = \frac{2}{4}$.)

Continue with the following possible sequence:
$$\frac{1}{2} = \frac{1}{8}$$
, $\frac{1}{3} = \frac{1}{9}$, $\frac{1}{4} = \frac{1}{8}$, $\frac{1}{5} = \frac{1}{15}$, and $\frac{1}{7} = \frac{1}{14}$.





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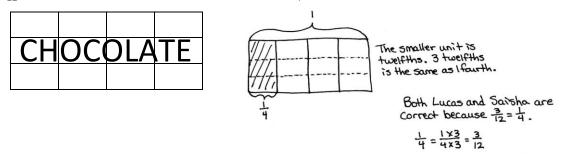
Use the area model and multiplication to show the equivalence of two fractions.



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Application Problem (4 minutes)

Saisha gives some of her chocolate bar, pictured below, to her younger brother Lucas. He says, "Thanks for $\frac{3}{12}$ of the bar." Saisha responds, "No. I gave you $\frac{1}{4}$ of the bar." Explain why both Lucas and Saisha are correct.



Note: This Application Problem reviews content from Lesson 7. This bridges into today's lesson, where students determine equivalent fractions of non-unit fractions. Revisit this problem in the Student Debrief by asking students to write the remaining portion as two equivalent fractions.

Concept Development (34 minutes)

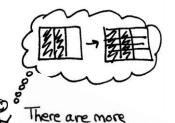
Materials: (S) Personal white board

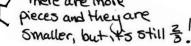
Problem 1: Determine that multiplying both the numerator and denominator by *n* results in an equivalent fraction.

- T: Draw an area model to represent 2 thirds. Draw three horizontal lines across the area model.
- S: (Draw and partition the model.)
- T: What happened to the size of the fractional units?
- S: The units are 4 times as small because we divided each unit into 4 smaller units.
- T: What happened to the number of units?
- S: There were 3, and now there are 12. \rightarrow There are 4 times as many units.
- MP.7 T: What happened to the number of selected units?
 - S: There were 2 units selected; now there are 8 units selected.
 - T: Discuss with your partner how to represent the equivalence of $\frac{2}{3}$ and $\frac{8}{12}$ using multiplication.
 - S: We can multiply the numerator and denominator by 4. We can write $\frac{2}{3} = \frac{2 \times 4}{3 \times 4} = \frac{8}{12}$.
 - T: How do you know the fraction is still representing the same amount?



 $\frac{2}{3} = \frac{2 \times 4}{3 \times 4} = \frac{8}{12}$







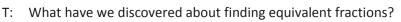
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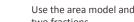
- S: I know it's the same size because I didn't change how much is selected. \rightarrow There are more smaller units instead of fewer bigger units, but the area of the selected fraction is still the same. \rightarrow The fractions are equivalent.
- T: What was different about this problem from the ones we did yesterday?
- S: The fraction that we are starting with doesn't have 1 as the numerator.
- T: We know any fraction can be decomposed into the sum of unit fractions. Yesterday, we saw that 1 third equals 4 twelfths. Today, we see that 2 thirds equals 4 twelfths plus 4 twelfths, or 8 twelfths.
- Draw an area model to represent $\frac{5}{c}$. Find an equivalent fraction with the T: **MP.7** denominator of 12. Explain to a partner how this is done.
 - S: We partition each of the 6 units into 2 parts so that we have 12 units. \rightarrow We double the number of units to make twelfths. \rightarrow There are twice as many units in the whole and twice as many units selected, but the parts are only half as big. $\rightarrow \frac{5}{6} = \frac{5 \times 2}{6 \times 2} = \frac{10}{12}$



S: The area of the fraction stays the same, but the number and size of the units change. \rightarrow The number of units increases. The size of the unit fraction decreases.

Problem 2: Determine that two fractions are equivalent using an area model and a number sentence.

- T: (Project $\frac{3}{4} = \frac{6}{8}$.) If the whole is the same, is this statement true or false?
- 3 times 2 is 6, and 4 times 2 is 8. Yes. It's true. \rightarrow If we multiply both the numerator and denominator by 2, we get $\frac{6}{2}$. \rightarrow Doubling the selected units and the number of units in the whole has the same area as $\frac{3}{4}$.
- T: Represent the equivalence in a number sentence using multiplication, and draw an area model to show the equivalence.
- S: (Do so as pictured to the right.)
- T: (Project $\frac{3}{4} = \frac{6}{12}$.) If the wholes are the same, is this statement true or false? How do you know? Discuss with your partner.
- S: Three times 2 is 6, and 4 times 3 is 12. It's false. We didn't multiply by the same number. \rightarrow This is false. I drew a model for $\frac{3}{4}$ and then decomposed it into twelfths. There are 9 units shaded, not 6. \rightarrow The numerator is being multiplied by 2, and the denominator is being multiplied by 3. They are not equivalent fractions.
- T: With your partner, revise the right side of the equation to make a true number sentence.
- S: We could change $\frac{6}{12}$ to $\frac{9}{12}$. \rightarrow Or we could change $\frac{6}{12}$ to $\frac{6}{8}$ because both the numerator and denominator would be multiplied by 2.



Use the area model and multiplication to show the equivalence of two fractions.

Lesson 8:

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engage

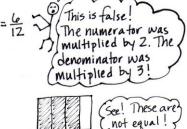
 $\frac{3}{4} = \frac{3 \times 2}{4 \times 2} = \frac{6}{8}$

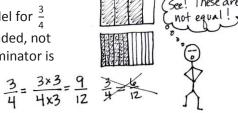
= 12

$$\frac{3}{4} = \frac{3 \times 2}{4 \times 2} = \frac{6}{8}$$

 $\frac{3}{4} = \frac{6}{8}$









Problem 3: Write a number sentence using multiplication to show the equivalence of two fractions. Draw the corresponding area model.

- Find an equivalent fraction without drawing an area model first. Write T: $\frac{3}{5}$ on your personal white board. How have we found equivalent fractions?
- S: We've doubled, tripled, or quadrupled the numerator and denominator. \rightarrow We multiply the numerator and denominator by the same number.
- Find an equivalent fraction to $\frac{3}{5}$ using multiplication. T:
- S: When I multiply the numerator and denominator by 2, l get $\frac{6}{10}$.
- T: Use an area model to confirm your number sentence.
- S: (Do so, correcting any errors as necessary. Answers may vary.)

Problem Set (10 minutes)

Student Debrief (10 minutes)

to show the equivalence of two fractions.

Students should do their personal best to complete the Problem Set within the allotted 10 minutes. For some classes, it may be appropriate to modify the assignment by specifying which problems they work on first. Some problems do not specify a method for solving. Students should solve these problems using the RDW approach used for Application Problems.

Lesson Objective: Use the area model and multiplication

The Student Debrief is intended to invite reflection and

Invite students to review their solutions for the Problem

partner before going over answers as a class. Look for

conversation to debrief the Problem Set and process the

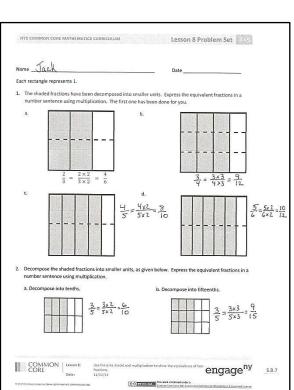
Any combination of the questions below may be used to

For Problem 3(a–d), how did you determine the number of horizontal lines to draw in each area

misconceptions or misunderstandings that can be addressed in the Debrief. Guide students in a

Set. They should check work by comparing answers with a

active processing of the total lesson experience.



NOTES ON

rectangles, such as circles and hexagons. This work may best be

virtual manipulatives.

MULTIPLE MEANS

OF ENGAGEMENT

discoveries about multiplying fractions by partitioning shapes other than

Invite students working above grade level and others to test their

lesson.

lead the discussion.

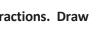
model?

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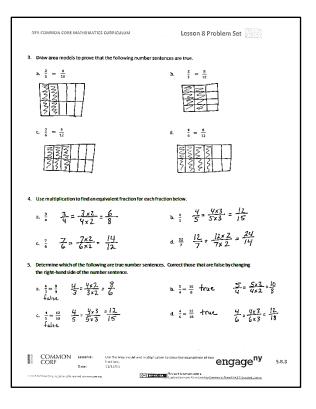


 $\frac{3}{5} = \frac{3 \times 2}{5 \times 2} = \frac{6}{10}$

- For Problem 5(c), did you and your partner have the same answer? Explain why you might have different answers.
- Explain when someone might need to use equivalent fractions in daily life.
- How are we able to show equivalence without having to draw an area model?
- Think back to the Application Problem. What fraction of the bar did Saisha receive?

Exit Ticket (3 minutes)

After the Student Debrief, instruct students to complete the Exit Ticket. A review of their work will help with assessing students' understanding of the concepts that were presented in today's lesson and planning more effectively for future lessons. The questions may be read aloud to the students.







Name _____

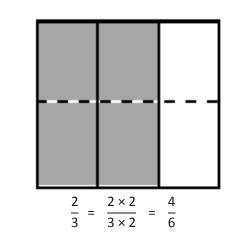
a.

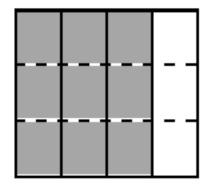
Date _____

Each rectangle represents 1.

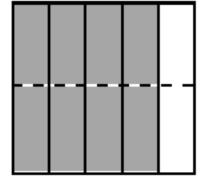
1. The shaded fractions have been decomposed into smaller units. Express the equivalent fractions in a number sentence using multiplication. The first one has been done for you.

b.

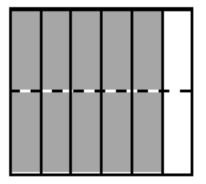




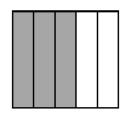
c.



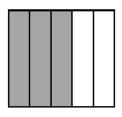




- 2. Decompose the shaded fractions into smaller units, as given below. Express the equivalent fractions in a number sentence using multiplication.
 - a. Decompose into tenths.



b. Decompose into fifteenths.





Lesson 8:



3. Draw area models to prove that the following number sentences are true.

a.
$$\frac{2}{5} = \frac{4}{10}$$
 b. $\frac{2}{3} = \frac{8}{12}$

c.
$$\frac{3}{6} = \frac{6}{12}$$
 d. $\frac{4}{6} = \frac{8}{12}$

- 4. Use multiplication to find an equivalent fraction for each fraction below.
 - a. $\frac{3}{4}$ b. $\frac{4}{5}$
 - c. $\frac{7}{6}$ d. $\frac{12}{7}$
- 5. Determine which of the following are true number sentences. Correct those that are false by changing the right-hand side of the number sentence.

a.
$$\frac{4}{3} = \frac{8}{9}$$
 b. $\frac{5}{4} = \frac{10}{8}$

c.
$$\frac{4}{5} = \frac{12}{10}$$
 d. $\frac{4}{6} = \frac{12}{18}$



Name _____

Date _____

1. Use multiplication to create an equivalent fraction for the fraction below.

2 5

2. Determine if the following is a true number sentence. If needed, correct the statement by changing the right-hand side of the number sentence.

 $\frac{3}{4} = \frac{9}{8}$



Lesson 8:



Name _____

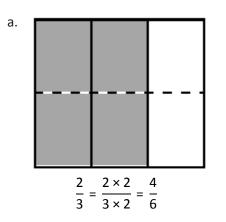
Date _____

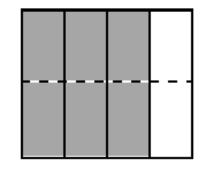
Each rectangle represents 1.

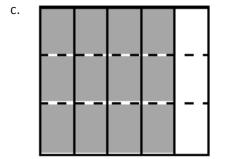
1. The shaded fractions have been decomposed into smaller units. Express the equivalent fractions in a number sentence using multiplication. The first one has been done for you.

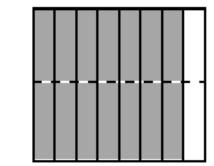
b.

d.





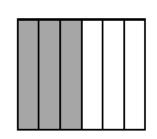


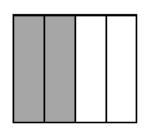


2. Decompose both shaded fractions into twelfths. Express the equivalent fractions in a number sentence using multiplication.

b.

a.







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Use the area model and multiplication to show the equivalence of two fractions.



This work is derived from Eureka Math [™] and licensed by Great Minds. ©2015-Great Minds. eureka math.org This file derived from G4-M5-TE-1.3.0-06.2015 3. Draw area models to prove that the following number sentences are true.

a.
$$\frac{1}{3} = \frac{2}{6}$$
 b. $\frac{2}{5} = \frac{4}{10}$

c.
$$\frac{5}{7} = \frac{10}{14}$$
 d. $\frac{3}{6} = \frac{9}{18}$

4. Use multiplication to create an equivalent fraction for each fraction below.

a.
$$\frac{2}{3}$$
 b. $\frac{5}{6}$

c.
$$\frac{6}{5}$$
 d. $\frac{10}{8}$

5. Determine which of the following are true number sentences. Correct those that are false by changing the right-hand side of the number sentence.

a.
$$\frac{2}{3} = \frac{4}{9}$$
 b. $\frac{5}{6} = \frac{10}{12}$

c.
$$\frac{3}{5} = \frac{6}{15}$$
 d. $\frac{7}{4} = \frac{21}{12}$



Lesson 8:

