

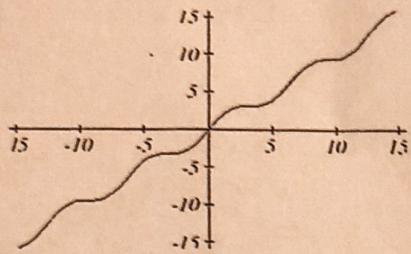
Name: Key

Hour: 2 Date: _____

Graphs of Periodic Functions Review

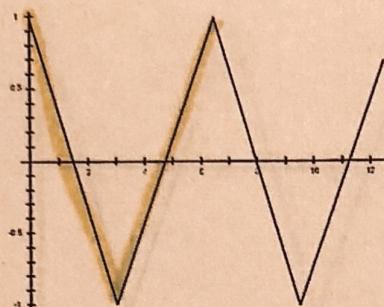
DIRECTIONS: Determine if the following graphs represent periodic functions. If not, explain why. If the graph is periodic find the period.

1)



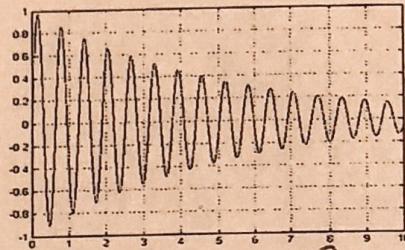
No! The function
is increasing.

2)



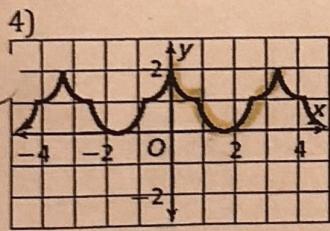
Yes!
Period = 6

3)



No! The function
is decreasing

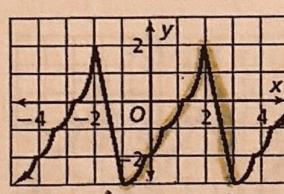
DIRECTIONS: (a) Highlight one cycle of each of the following periodic graphs. (b) Find the period. (c) Find the amplitude.



b) Period = 3.5

c) Amplitude = $\frac{1}{2}(2 - (-2)) = 1$

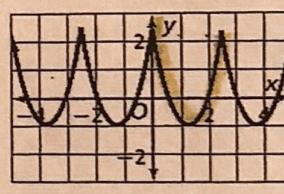
5)



b) Period = 4

c) Amplitude = $\frac{1}{2}(2 - (-2)) = \frac{1}{2}(4) = 2$

6)



b) Period = 2.5

c) Amplitude = $\frac{1}{2}(2 - (-2)) = \frac{1}{2}(4) = 2$

DIRECTIONS: Graph one cycle of each of the following trig functions. YOU MUST INCLUDE A TABLE.

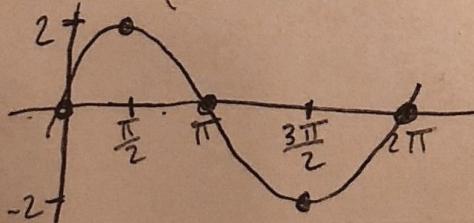
7) $y = 2\sin\theta$

$a=2$

$\omega=1$

Period = 2π

θ	y
$0(2\pi) = 0$	0
$\frac{1}{4}(2\pi) = \frac{2\pi}{4} = \frac{\pi}{2}$	2
$\frac{1}{2}(2\pi) = \frac{2\pi}{2} = \pi$	0
$\frac{3}{4}(2\pi) = \frac{6\pi}{4} = \frac{3\pi}{2}$	-2
$1(2\pi) = 2\pi$	0



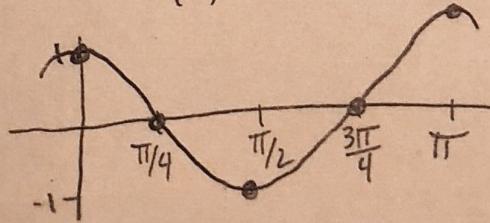
8) $y = \cos(2\theta)$

$a=1$

$b=2$

Period: π

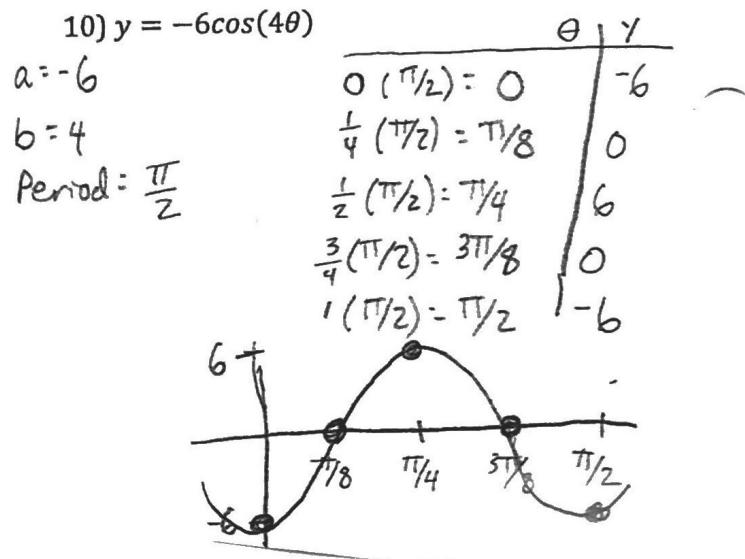
θ	y
$0(\pi) = 0$	1
$\frac{1}{4}(\pi) = \frac{\pi}{4}$	0
$\frac{1}{2}(\pi) = \frac{\pi}{2}$	-1
$\frac{3}{4}(\pi) = \frac{3\pi}{4}$	0
$1(\pi) = \pi$	1



9) $y = -5\sin(\pi\theta)$

θ	y
$0(2) = 0$	0
$\frac{1}{4}(2) = \frac{\pi}{2}$	-5
$\frac{1}{2}(2) = 1$	0
$\frac{3}{4}(2) = \frac{3\pi}{2}$	5
$1(2) = 2$	0

Period = 2



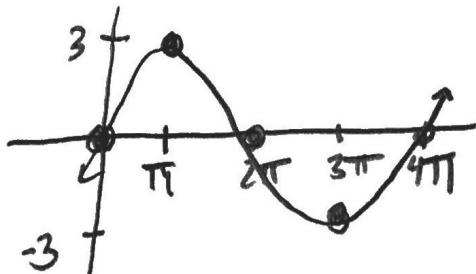
11) $y = 3\sin\frac{\theta}{2}$

a = 3

b = $\frac{1}{2}$

Period = $\frac{2\pi}{1}, \frac{2}{1} = 4\pi$

θ	y
0	0
π	3
2π	0
3π	-3
4π	0



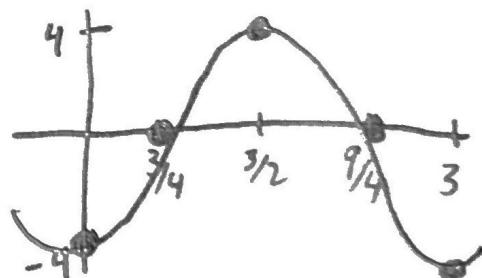
12) $y = -4\cos\frac{2\pi\theta}{3}$

a = -4

b = $\frac{2\pi}{3}$

Period = $\frac{2\pi}{1} \cdot \frac{3}{2\pi} = 3$

θ	y
0	-4
$\frac{3}{4}$	0
$\frac{1}{2}$	4
$\frac{9}{4}$	0
$\frac{3}{2}$	-4



DIRECTIONS: Write an equation that matches the given description.

- 13) A positive cosine function with amplitude of 3 and period of 4π .

$$y = a \cos b\theta$$

a = 3

b = $\frac{2\pi}{4\pi} = \frac{1}{2}$

$$\boxed{y = 3 \cos \frac{1}{2}\theta}$$

- 14) A negative sine function with amplitude of 4 and period of 3.

$$y = -a \sin b\theta$$

a = -1

b = $\frac{2\pi}{3}$

$$\boxed{y = -\sin \frac{2\pi}{3}\theta}$$

- 15) A positive sine function with amplitude of 10 and period of π .

$$y = a \sin b\theta$$

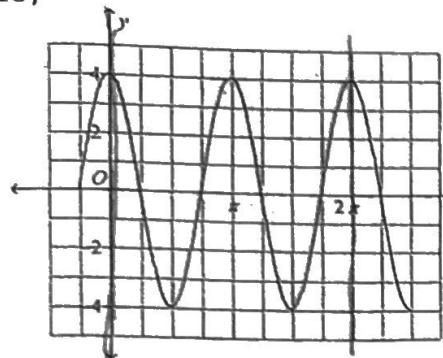
a = 10

b = $\frac{2\pi}{\pi} = 2$

$$\boxed{y = 10 \sin 2\theta}$$

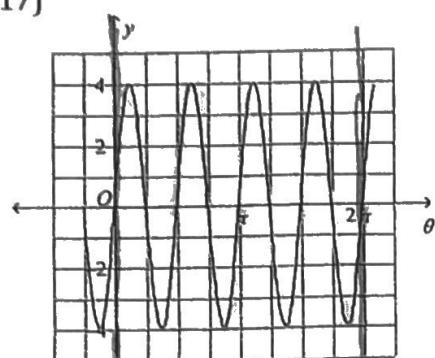
DIRECTIONS: Write an equation that satisfies the given periodic graph.

16)



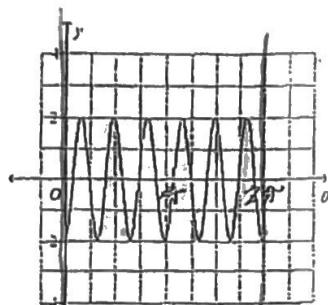
$$y = 4 \cos 2\theta$$

17)



$$y = 4 \sin 4\theta$$

18)



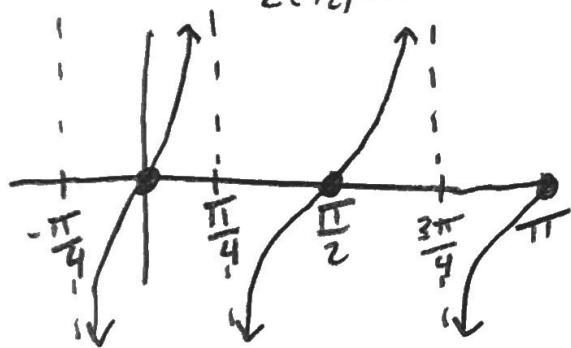
$$y = -2 \cos 6\theta$$

Graph two cycles of the following tangent functions. YOU MUST INCLUDE A TABLE.

19) $y = \tan 2\theta$

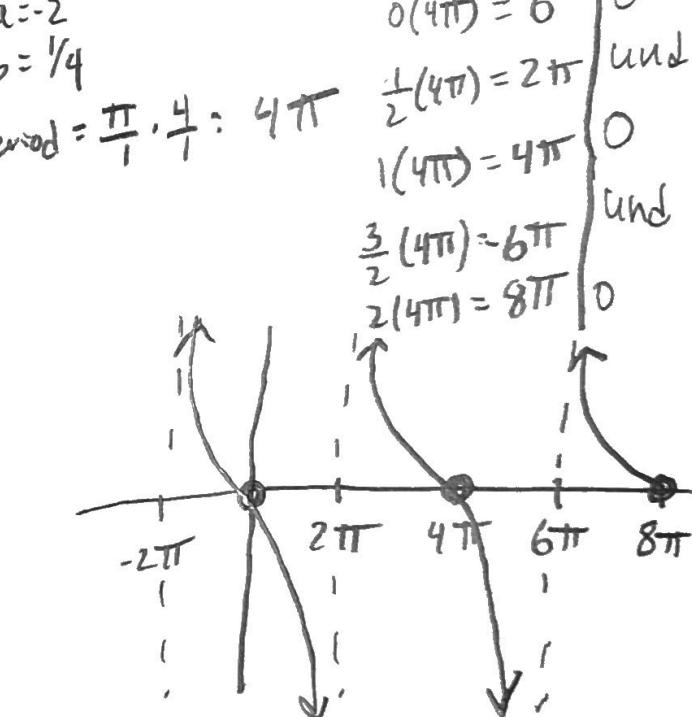
$$\begin{aligned} a &= 1 \\ b &= 2 \\ \text{Period} &= \frac{\pi}{2} \end{aligned}$$

θ	y
$0(\frac{\pi}{2}) = 0$	0
$\frac{1}{2}(\frac{\pi}{2}) = \frac{\pi}{4}$	und.
$1(\frac{\pi}{2}) = \frac{\pi}{2}$	0
$\frac{3}{2}(\frac{\pi}{2}) = \frac{3\pi}{4}$	und.
$2(\frac{\pi}{2}) = \pi$	0



20) $y = -2 \tan \frac{\theta}{4}$

$$\begin{aligned} a &= -2 \\ b &= \frac{1}{4} \\ \text{Period} &= \frac{\pi}{4} \cdot 4 = 4\pi \end{aligned}$$

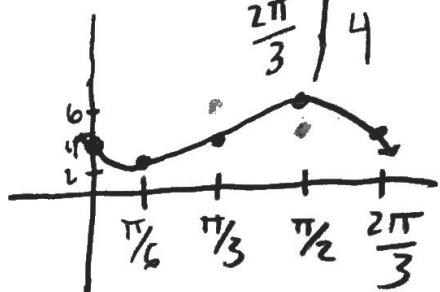


Graph the following trig functions. YOU MUST INCLUDE A TABLE.

21) $y = -2 \sin 3\theta + 4$

$$\begin{aligned} a &= -2 \\ b &= 3 \\ \text{Period} &= \frac{2\pi}{3} \end{aligned}$$

θ	$y + 4$
0	4
$\frac{\pi}{6}$	2
$\frac{\pi}{3}$	4
$\frac{\pi}{2}$	6
$\frac{2\pi}{3}$	4



22) $y = 3 \cos \frac{4\theta}{7} - 6$

$$\begin{aligned} a &= 3 \\ b &= \frac{4}{7} \\ \text{Period} &= \frac{2\pi}{4/7} = \frac{7\pi}{2} \end{aligned}$$

θ	$y - 6$
0	-3
$\frac{7\pi}{8}$	-6
$\frac{7\pi}{4}$	-9
$\frac{21\pi}{8}$	-6
$\frac{7\pi}{2}$	-3

