

Multiplying Polynomials Notes

Multiply the following polynomials and write their products in STANDARD FORM.

Classify each product by their degree/number of terms and describe their end behavior.

1) $(x+1)(x+2)(x+3)$

$$(x+1)(x^2+3x+2x+6)$$

$$(x+1)(x^2+5x+6)$$

$$x^3+5x^2+6x+x^2+5x+6$$

$$\boxed{x^3+6x^2+11x+6}$$

Cubic Polynomial
with four terms.

Positive Odd ($\downarrow \uparrow$)

Left: $x \rightarrow -\infty \quad y \rightarrow -\infty$

Right: $x \rightarrow +\infty \quad y \rightarrow +\infty$

2) $(x+1)(x-1)(x+2)$

$$(x+1)(x^2+2x-x-2)$$

$$(x+1)(x^2+x-2)$$

$$x^3+x^2-2x+x^2+x-2$$

$$\boxed{x^3+2x^2-x-2}$$

Cubic polynomial
with four terms

Positive Odd ($\downarrow \uparrow$)

Left: $x \rightarrow -\infty \quad y \rightarrow -\infty$

Right: $x \rightarrow +\infty \quad y \rightarrow +\infty$

3) $x(x-3)^2$ ← write twice!

$$x(x-3)(x-3)$$

$$x(x^2-3x-3x+9)$$

$$x(x^2-6x+9)$$

$$\boxed{x^3-6x^2+9x}$$

Cubic Trinomial

Positive Odd ($\downarrow \uparrow$)

Left: $x \rightarrow -\infty \quad y \rightarrow -\infty$

Right: $x \rightarrow +\infty \quad y \rightarrow +\infty$

4) $x^2(x^2 - 9)$

$x^4 - 9x^2$

Quartic Binomial

Positive Even ($\uparrow \uparrow$)

Left: $x \rightarrow -\infty$ $y \rightarrow +\infty$

Right: $x \rightarrow +\infty$ $y \rightarrow +\infty$

5) $(x-2)^3$ ← write out three times!

$(x-2)(x-2)(x-2)$

$(x-2)(x^2 - 2x - 2x + 4)$

$(x-2)(x^2 - 4x + 4)$

$x^3 - 4x^2 + 4x - 2x^2 + 8x - 8$

$x^3 - 6x^2 + 12x - 8$

Cubic Polynomial
with 4 terms

Positive Odd ($\downarrow \uparrow$)

Left: $x \rightarrow -\infty$ $y \rightarrow +\infty$

Right: $x \rightarrow +\infty$ $y \rightarrow +\infty$