

Name: Key Hour: _____ Date: _____

Radical & Rational Exponent Forms

Notes

$$\sqrt[n]{x^m} = x^{\frac{m}{n}}$$

If the n is not given, it's a 2!

Radical → Rational Exponent	Rational Exponent → Radical
$m=3 \ n=2$ $(\sqrt{3k})^3 = (3k)^{\frac{3}{2}}$	$(10r)^{\frac{2}{3}} = \sqrt[3]{(10r)^2} \quad \begin{matrix} m=2 \\ n=3 \end{matrix}$
$m=3 \ n=2$ $(\sqrt[3]{7x})^4 = (7x)^{\frac{4}{3}}$	$(6b)^{\frac{5}{2}} = \sqrt{(6b)^5} \quad \begin{matrix} m=5 \\ n=2 \end{matrix}$

Simplify!

$$9^{\frac{1}{2}} = \sqrt{9} = \boxed{\pm 3}$$

$$64^{\frac{2}{3}} = \sqrt[3]{64^2} = \cancel{= 0} = \frac{4^2}{16} = \boxed{16}$$

$$8^{\frac{1}{3}} = \sqrt[3]{8} = \boxed{2}$$

More Examples!

Writing in Exponential or Radical Form
Notes

Name:

Write each exponential in a radical form.

$$1) 7^{\frac{1}{2}} = \sqrt{7}$$

$$m=1$$

$$n=2$$

$$3) 2^{\frac{5}{3}} = \sqrt[3]{2^5}$$

$$m=5$$

$$n=3$$

$$5) 6^{\frac{3}{2}} = \sqrt{6^3}$$

$$m=3$$

$$n=2$$

$$2) 4^{\frac{4}{3}} = \sqrt[3]{4^4}$$

$$m=4$$

$$n=3$$

$$4) 7^{\frac{4}{3}} = \sqrt[3]{7^4}$$

$$m=4$$

$$n=3$$

$$6) 2^{\frac{1}{6}} = \sqrt[6]{2}$$

$$m=1$$

$$n=6$$

Write each radical in an exponential form.

$$7) (\sqrt{10})^3$$

$$m=3$$

$$n=2$$

$$10^{\frac{3}{2}}$$

$$8) \sqrt[6]{2}$$

$$m=1$$

$$n=6$$

$$2^{\frac{1}{6}}$$

$$9) (\sqrt[4]{2})^5$$

$$m=5$$

$$n=4$$

$$2^{\frac{5}{4}}$$

$$11) \sqrt[3]{2}$$

$$m=1$$

$$n=3$$

$$2^{\frac{1}{3}}$$

$$12) \sqrt[6]{10}$$

$$m=1$$

$$n=6$$

$$10^{\frac{1}{6}}$$