

Linear

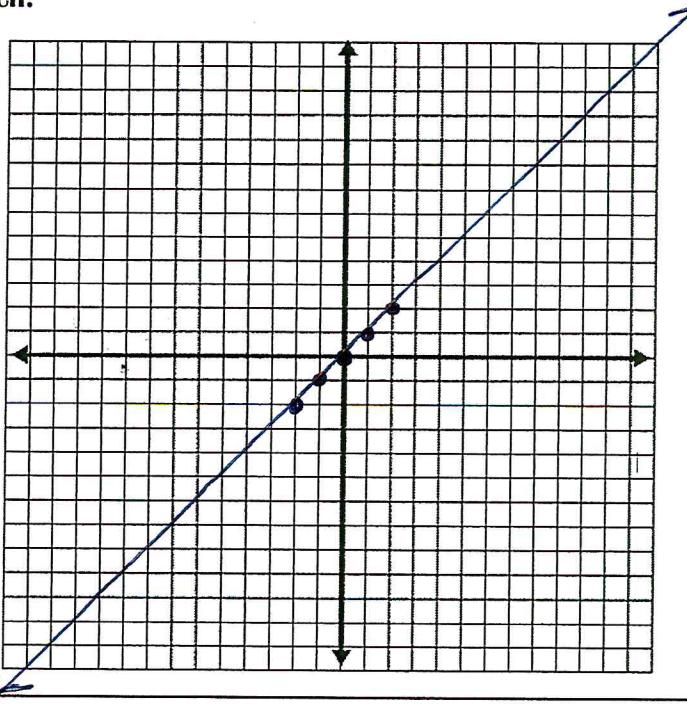
$$f(x) = x$$

Table of Values

choose two positive,
two negative and zero
for values of x

x	y
-2	-2
-1	-1
0	0
1	1
2	2

Sketch:



$$f(x) = x$$

Domain
(interval)

$$(-\infty, +\infty)$$

Range
(interval)

$$(-\infty, +\infty)$$

Increasing
(interval)

$$(-\infty, +\infty)$$

Decreasing
(interval)

N/A

Intercepts

$$x\text{-intercept: } (0, 0)$$

$$y\text{-intercept: } (0, 0)$$

Asymptotes

N/A

End behavior

Left:
 $\text{as } x \rightarrow -\infty, y \rightarrow -\infty$

Right:
 $\text{as } x \rightarrow +\infty, y \rightarrow +\infty$

Symmetry

odd

Additional info:

Straight line

Absolute Value

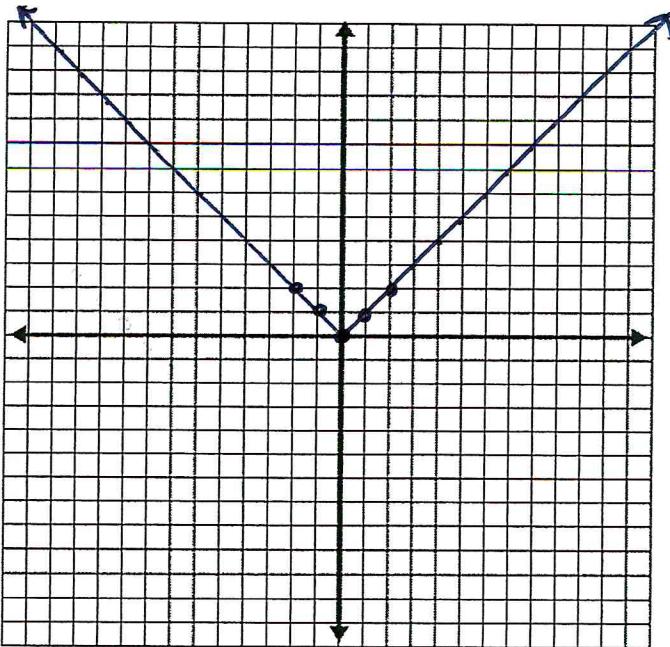
$$f(x) = |x|$$

Table of Values

choose two positive,
two negative and zero
for values of x

x	y
-2	2
-1	1
0	0
1	1
2	2

Sketch:



$f(x) = x $	
Domain (interval)	$(-\infty, +\infty)$
Range (interval)	$[0, +\infty)$
Increasing (interval)	$(0, +\infty)$
Decreasing (interval)	$(-\infty, 0)$
Intercepts	x -intercept: $(0,0)$
	y -intercept: $(0,0)$
Asymptotes	N/A
End behavior	<u>Left</u> : $x \rightarrow -\infty, y \rightarrow +\infty$
	<u>Right</u> : as $x \rightarrow +\infty, y \rightarrow +\infty$
Symmetry	Odd

Additional info:

"V-shaped"

Polynomial (Quadratic)

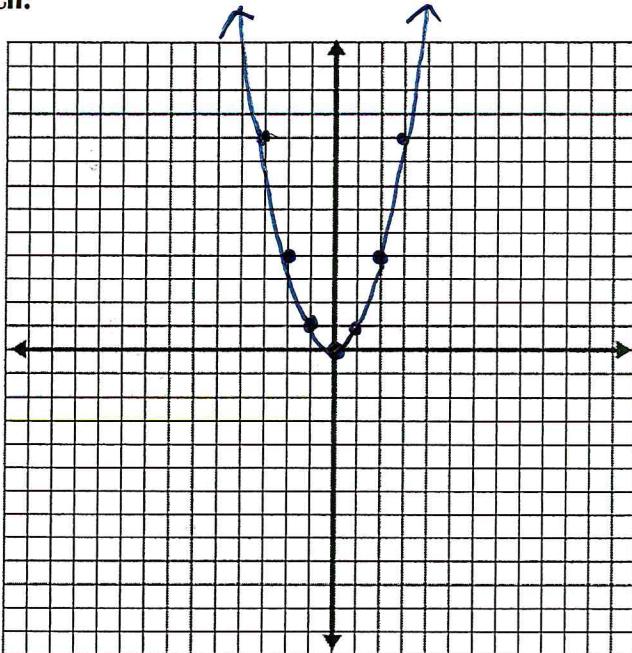
$f(x) = x^2$

Table of Values

choose two positive,
two negative and zero
for values of x

x	y
-2	4
-1	1
0	0
1	1
2	4

Sketch:



$f(x) = x^2$		
Domain (interval)	$(-\infty, +\infty)$	
Range (interval)	$[0, +\infty)$	
Increasing (interval)	$(0, +\infty)$	
Decreasing (interval)	$(-\infty, 0)$	
Intercepts	$x\text{-int.}$ $(0, 0)$	$y\text{-int.}$ $(0, 0)$
Asymptotes	N/A	
End behavior	<u>left</u> as $x \rightarrow -\infty$ $y \rightarrow +\infty$	<u>Right</u> as $x \rightarrow +\infty$ $y \rightarrow +\infty$
Symmetry	even	

Additional info:

Parabola ("u-shaped")

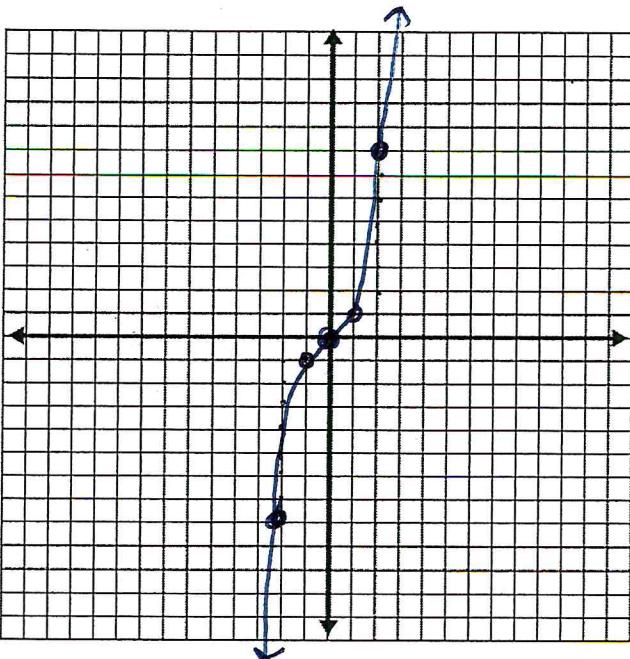
**Polynomial
(Cubic)
 $f(x) = x^3$**

Table of Values

choose two positive,
two negative and zero
for values of x

x	y
-2	-8
-1	-1
0	0
1	1
2	8

Sketch:



$f(x) = x^3$	
Domain (interval)	$(-\infty, +\infty)$
Range (interval)	$(-\infty, +\infty)$
Increasing (interval)	$(0, +\infty)$
Decreasing (interval)	$(-\infty, 0)$
Intercepts	$x\text{-int: } (0, 0)$ $y\text{-int: } (0, 0)$
Asymptotes	N/A
End behavior	<u>Left</u> as $x \rightarrow -\infty$ $y \rightarrow -\infty$ <u>Right</u> as $x \rightarrow +\infty$ $y \rightarrow +\infty$
Symmetry	odd

Additional info:

arrows point in opposite directions, one is up and the other is down

Radical (Square Root)

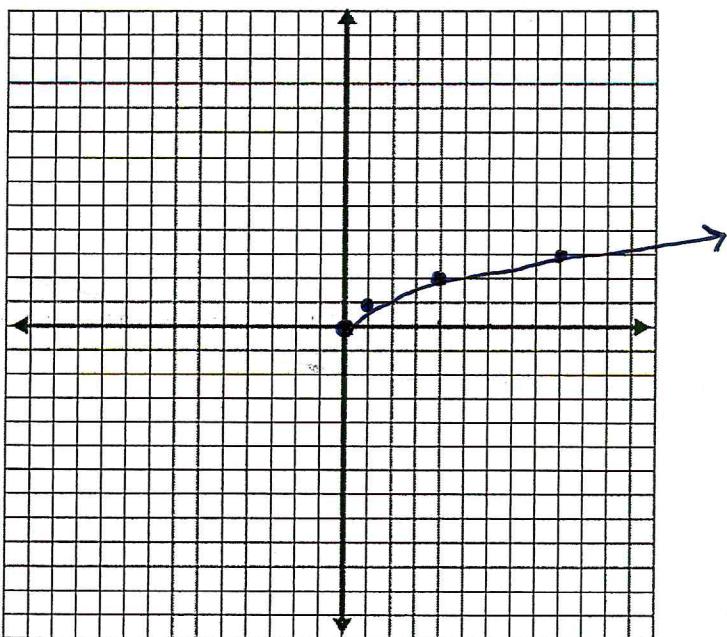
$$f(x) = \sqrt{x}$$

Table of Values

choose two positive,
two negative and zero
for values of x

x	y
-4	undef
-1	undef
0	0
1	1
4	2

Sketch:



$$f(x) = \sqrt{x}$$

Domain
(interval)

$$[0, +\infty)$$

Range
(interval)

$$[0, +\infty)$$

Increasing
(interval)

$$(0, +\infty)$$

Decreasing
(interval)

N/A

Intercepts

$$\begin{array}{ll} x\text{-int} & y\text{-int} \\ (0,0) & (0,0) \end{array}$$

Asymptotes

N/A

End behavior

Left:

none, no arrow

right:

as $x \rightarrow +\infty$ $y \rightarrow +\infty$

Symmetry

None

Additional info:

this parent function ~~stops~~ starts from the origin.

You can't take the square root of a negative number!

Radical (Cubic Root)

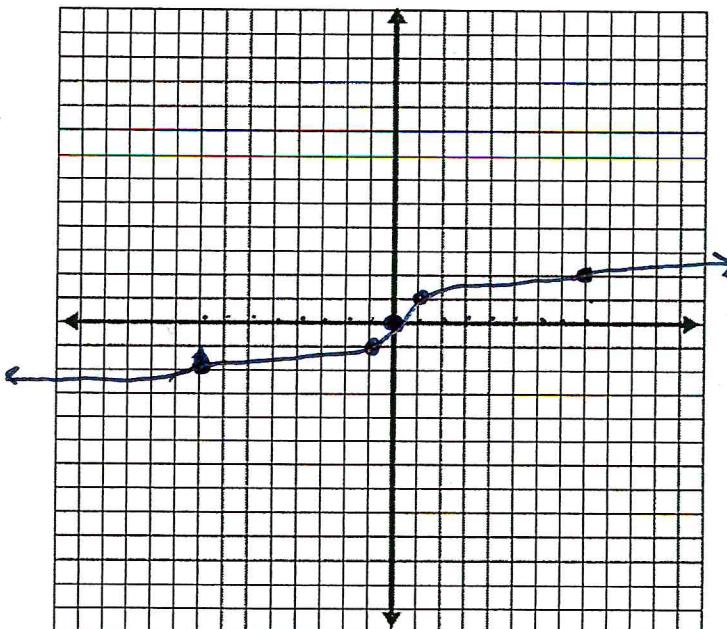
$$f(x) = \sqrt[3]{x}$$

Table of Values

choose two positive,
two negative and zero
for values of x

x	y
-8	-2
-1	-1
0	0
1	1
8	2

Sketch:



$$f(x) = \sqrt[3]{x}$$

Domain
(interval)

$$(-\infty, +\infty)$$

Range
(interval)

$$(-\infty, +\infty)$$

Increasing
(interval)

$$(-\infty, +\infty)$$

Decreasing
(interval)

N/A

Intercepts

$$x\text{-int: } (0, 0) \quad y\text{-int: } (0, 0)$$

Asymptotes

N/A

End behavior

Left
as $x \rightarrow -\infty$ $y \rightarrow -\infty$

Right
as $x \rightarrow +\infty$ $y \rightarrow +\infty$

Symmetry

N/A

Additional info:

- a "sideways S"

- one arrow points left and the other points right

Exponential Growth

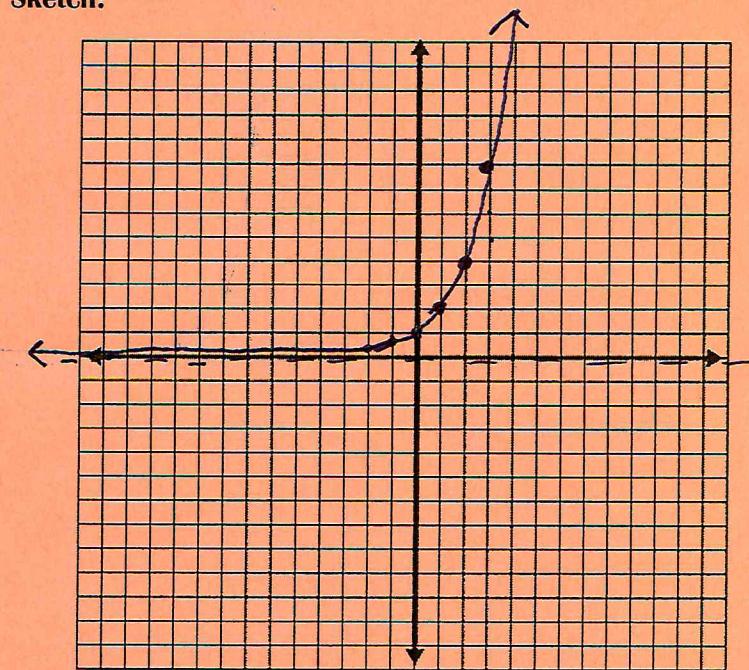
$$f(x) = 2^x$$

Table of Values

choose two positive,
two negative and zero
for values of x

x	y
-2	1/4
-1	1/2
0	1
1	2
2	4

Sketch:



$f(x) = 2^x$	
Domain (interval)	$(-\infty, +\infty)$
Range (interval)	$[0, +\infty)$
Increasing (interval)	$(0, +\infty)$
Decreasing (interval)	N/A
Intercepts	$x\text{-int: None}$ $y\text{-int: } (0, 1)$
Asymptotes	$y = 0$
End behavior	<u>left</u> as $x \rightarrow -\infty$ $y \rightarrow 0$ <u>right</u> as $x \rightarrow +\infty$ $y \rightarrow +\infty$
Symmetry	N/A

Additional info:

An asymptote is a line that a function will get closer and closer to but never touch or crosses. In this case that line is the x-axis, where $y=0$. An asymptote influences end behavior.

Exponential Decay

$$f(x) = \left(\frac{1}{3}\right)^x$$

Table of Values

choose two positive,
two negative and zero
for values of x

x	y
-2	9
-1	3
0	1
1	$\frac{1}{3}$
2	$\frac{1}{9}$

Sketch:



$$f(x) = \left(\frac{1}{3}\right)^x$$

Domain
(interval)

$$(-\infty, +\infty)$$

Range
(interval)

$$(0, +\infty)$$

Increasing
(interval)

N/A

Decreasing
(interval)

$$(-\infty, +\infty)$$

Intercepts

x-int: none
y-int: (0, 1)

Asymptotes

$$y = 0$$

End behavior

Left
as $x \rightarrow -\infty$, $y \rightarrow +\infty$

Right
as $x \rightarrow +\infty$, $y \rightarrow 0$

Symmetry

N/A

Additional info:

See exp. growth.