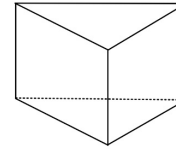


Tuesday, May 19, 2020

## Sec 11-2 Surface Areas of Prisms and Cylinders

### Prism:

- A polyhedron with exactly two congruent, parallel faces, called BASES.
- Other faces are called LATERAL FACES.

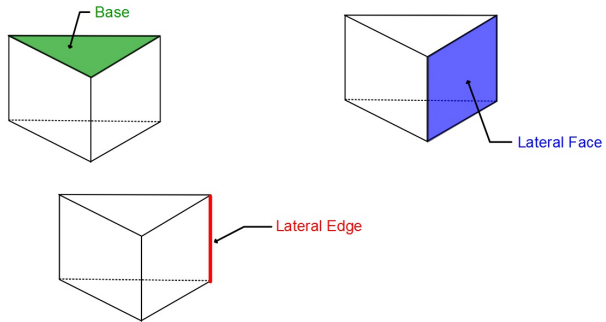


Prism Vocabulary:

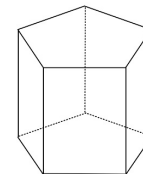
Base

Lateral Face

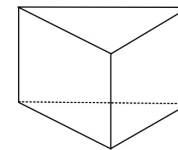
Lateral Edge



The name of a prism is given by the shape of its base.



Pentagonal Prism

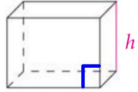


Triangular Prism

The **Height** of a Prism is the perpendicular distance between the bases.

A Prism can either be a Right Prism or an Oblique Prism.

Right Prism



When the lateral edges form a right angle with the bases

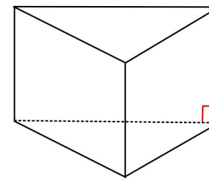
Oblique Prism



When the lateral edges **DON'T** form a right angle with the bases.

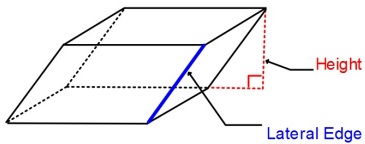
In a Right Prism:

- Lateral Faces are Rectangles
- Lateral Edge is an altitude (height).



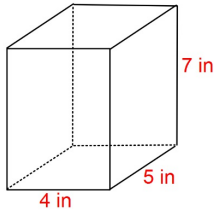
Lateral Edge = Height

Oblique Prism: Lateral Edge is NOT the height



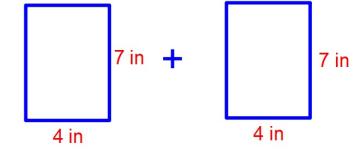
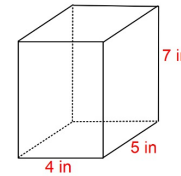
We'll work with Right Prisms only.

Find the number of square inches of wrapping paper it would take to cover this box (rectangular prism).



One method would be to find the area of all 6 faces and add them together.

Front and Back:

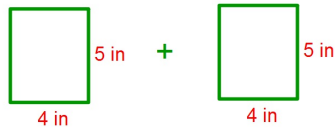
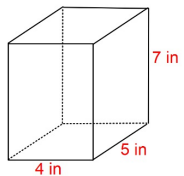


$$A = (4)(7) = 28 \text{ in}^2$$

$$A = (4)(7) = 28 \text{ in}^2$$

$$\text{Front and Back} = 2(28) = 56 \text{ in}^2$$

Top and Bottom:

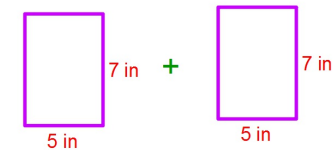
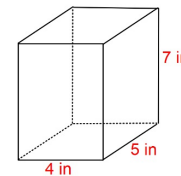


$$A = (4)(5) = 20 \text{ in}^2$$

$$A = (4)(5) = 20 \text{ in}^2$$

$$\text{Top and Bottom} = 2(20) = 40 \text{ in}^2$$

Left and Right:



$$A = (5)(7) = 35 \text{ in}^2$$

$$A = (5)(7) = 35 \text{ in}^2$$

$$\text{Left and Right} = 2(35) = 70 \text{ in}^2$$

Total Surface Area =

(Front and Back)+(Top and Bottom)+(Left and Right)=

$$(56)+(40)+(70) = 166 \text{ in}^2$$

Surface Area of a Prism:

$$SA = LA + 2B$$

LA: Lateral Area

2B: Area of the Bases

**Lateral Area:** Sum of areas of lateral faces.

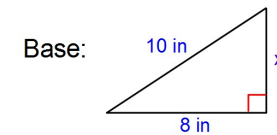
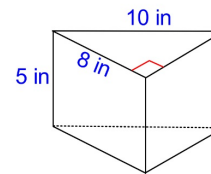
$$LA = ph$$

$$LA = (\text{perimeter of the Base})(\text{height})$$

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Area of the bases: Use the formula that applies to whatever the shape of the base is.

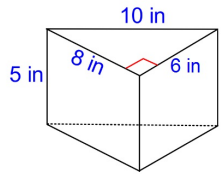
Find the Total Surface Area (SA) of the Right Triangular Prism.



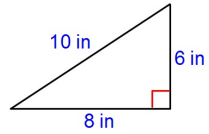
Find the third side:

$$\begin{aligned} 8^2 + x^2 &= 10^2 \\ x^2 &= 10^2 - 8^2 \\ x &= \sqrt{10^2 - 8^2} \quad x = 6 \end{aligned}$$

Find LA:

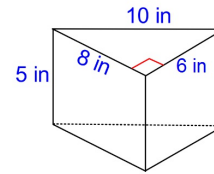


Base:

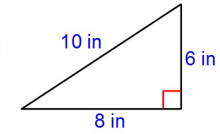


$$LA = (p)(h) = (10+8+6)(5) = (24)(5) = 120 \text{ in}^2$$

Find 2B:



Base:

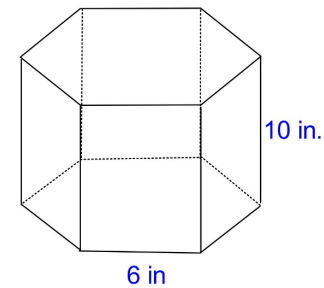


$$B = \text{area of the base} = \frac{1}{2}(b)(h) \\ = \frac{1}{2}(8)(6) = 24 \text{ in}^2$$

$$2B = 2(24) = 48 \text{ in}^2$$

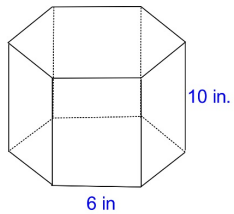
$$SA = LA + 2B = 120 + 48 = 168 \text{ in}^2$$

Find the SA of this regular hexagonal prism to the nearest tenth.



Find the SA of this regular hexagonal prism to the nearest hundredth.

Find LA:



$$LA = (p)(h)$$

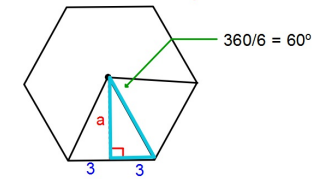
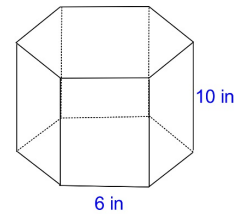
$$p = 6(\text{length of a side}) = 6(6) = 36$$

$$LA = (36)(10) = 360 \text{ in}^2$$

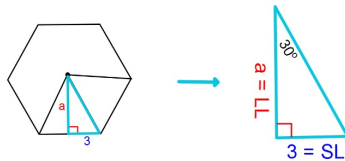
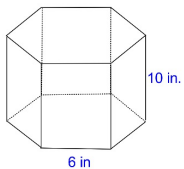
Find 2B: Base is a Regular Hexagon:  $B = \frac{1}{2}(a)(p)$

We already have the perimeter:  $p = 36$

Now we need the apothem:



Find 2B:

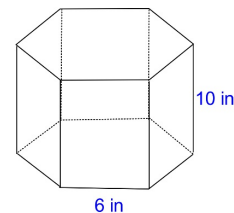


$$a = LL = \sqrt{3} \cdot SL = 3\sqrt{3}$$

$$B = \frac{1}{2}(a)(p) = \frac{1}{2}(3\sqrt{3})(36) = 54\sqrt{3}$$

$$2B = 108\sqrt{3}$$

Find the SA of this regular hexagonal prism to the nearest hundredth.



$$SA = LA + 2B$$

$$= 360 + 108\sqrt{3}$$

$$SA \approx 547.06 \text{ in}^2$$

You can continue working on Practice #25.

We'll continue tomorrow over this material.

Practice #25 will be due on Thursday, May 21  
by 10:00 pm