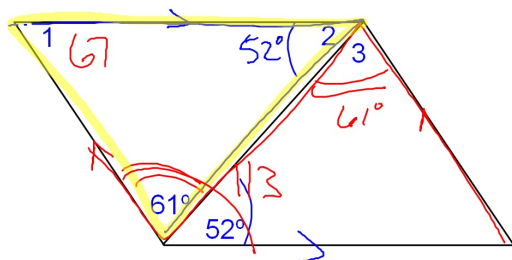
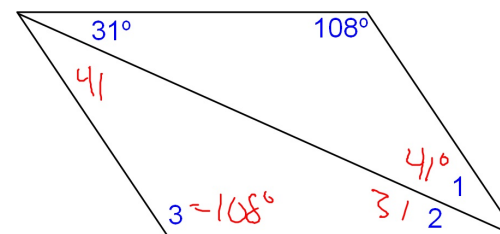


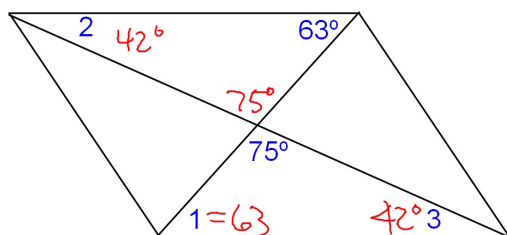
Find the measures of the numbered angles in this parallelogram.



Find the measures of the numbered angles in this parallelogram.



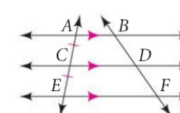
Find the measures of the numbered angles in this parallelogram.



#### Theorem 6-4

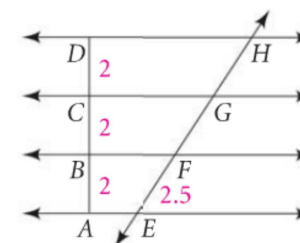
If three (or more) parallel lines cut off congruent segments on one transversal, then they cut off congruent segments on every transversal.

$$\overline{BD} \cong \overline{DF}$$



In the figure at the right,  $\overline{DH} \parallel \overline{CG} \parallel \overline{BF} \parallel \overline{AE}$ ,  $AB = BC = CD = 2$ , and  $EF = 2.5$ . Find  $EH$ .

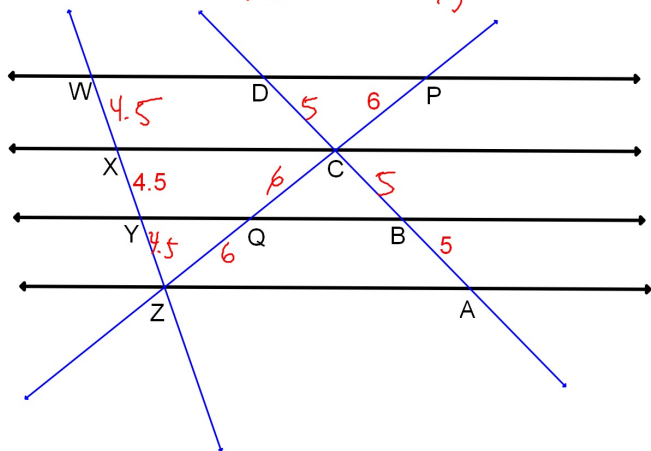
$$GH = 2.5 \quad EH = 7.5$$



The four black lines are parallel and  $AB=BC=CD$

Find each:  $ZC = 12$   $CD = 5$   $WZ = 13.5$

$QP = 12$   $AD = 15$



Hwk #17

Sec 6-2

Pages 316-317

Problems 24, 25, 29, 30, 37-39, 45

### Section 6-3: Proving That a Quadrilateral is a Parallelogram.

Property of a Parallelogram:

Both pairs of opposite sides are parallel

*Converse*

Converse:

If both pairs of opposite sides of a quadrilateral are parallel, then the quadrilateral is a parallelogram.

Is ABCD a Parallelogram?

A (4,3)

B (5,8)

C (-3,2)

D (-4,-3)

$$\begin{aligned} AB \quad m &= \frac{5}{1} \\ BC \quad m &= \frac{-6}{8} = -\frac{3}{4} \\ CD \quad m &= \frac{2-3}{-3-4} = \frac{1}{7} \\ DA \quad m &= \frac{3-3}{4-4} = \frac{0}{0} = \text{undefined} \end{aligned}$$

Yes ABCD is a parallelogram  
b/c both pair  
of opp sides  
are ||

Property of a Parallelogram:

Both pairs of opposite sides are congruent.

**Theorem 6-5**

If both pairs of opposite sides of a quadrilateral are congruent, then the quadrilateral is a parallelogram.

Is EFGH a Parallelogram?

E(3,-1)      F(6,5)      G(1,13)      H(-5,7)

$$EF \quad \sqrt{3^2 + 6^2} = \sqrt{45}$$

$$FG \quad \sqrt{\quad}$$

$$GH \quad \sqrt{6^2 + 6^2} = \sqrt{72}$$

$$HE \quad \sqrt{\quad}$$

NOT a ||-gram  
b/c opp  
sides aren't  
 $\cong$

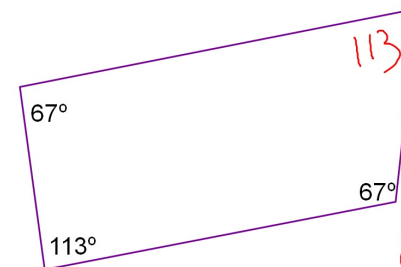
Property of a Parallelogram:

Both pairs of opposite angles are congruent.

**Theorem 6-6**

If both pairs of opposite angles of a quadrilateral are congruent, then the quadrilateral is a parallelogram.

Is PQRS a Parallelogram?



$$67 + 67 + 113 = 247$$

Yes, because both  
pair of opposite angles  
are congruent

$$360 - 247 = 113$$

Property of Parallelograms:

The diagonals bisect each other.

**Theorem 6-7**

If the diagonals of a quadrilateral bisect each other, then the quadrilateral is a parallelogram.

Is WXYZ a Parallelogram?

W(8,3)

X(-9,-1)

Y(4,5)

Z(21,10)

midpoint WY  $\left(\frac{8+4}{2}, \frac{3+5}{2}\right) = (6, 4)$   
midpoint XZ  $\left(\frac{-9+21}{2}, \frac{-1+10}{2}\right) = (6, 4.5)$   
NOT A ll-gram  
b/c diagonals don't bisect

On a piece of graph paper plot Point A in the second quadrant and Point D in the third quadrant.

From A do a rise of 2 and a run of 7. Label this point B

From D do a rise of 2 and a run of 7. Label this point C.

Connect the four points to create a quadrilateral.

How are AB and CD related to each other?  $\cong$  & ||

This figure is a parallelogram