

What conclusion can you make from the given information?

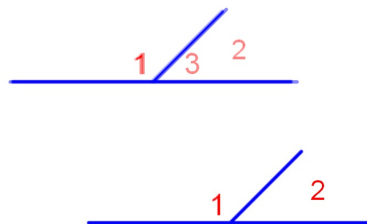
From yesterday.

Angle 1 is supplementary to Angle 3.

Angle 2 is supplementary to Angle 3.

$\therefore \angle 1 \cong \angle 2$

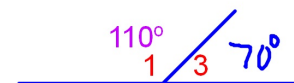
the symbol for "Therefore"....



Theorem 2-2

Congruent Supplements Theorem

If two angles are supplements of the same angle (or of congruent angles), then the two angles are congruent.



Given:

Angle 1 is supplementary to Angle 3.

Angle 2 is supplementary to Angle 3.

Steps	Reasons
1. Angle 1 is supplementary to Angle 3 Angle 2 is supplementary to Angle 3	1. Given
2. $\angle 1 + \angle 3 = 180^\circ$ $\angle 2 + \angle 3 = 180^\circ$	2. Def of suppl
3. $\angle 1 + \angle 3 = \angle 2 + \angle 3$	3. Substitution
4. $\angle 1 = \angle 2$	4. Subtr prop =

Given:

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Steps	Reasons
1. Angle 1 is supplementary to Angle 3 Angle 2 is supplementary to Angle 3	1. Given
2. $\angle 1 + \angle 3 = 180^\circ$ $\angle 2 + \angle 3 = 180^\circ$	2. Definition of Suppl
3. $\angle 1 + \angle 3 = \angle 2 + \angle 3$	3. Substitution
4. $\angle 1 = \angle 2$	4. Subtr Prop of =



This is called a 2-column proof.

Paragraph Proof:

Given the fact $\angle 1$ suppl to $\angle 3$ and $\angle 2$ suppl to $\angle 3$ by the definition of supplementary we know that $\angle 1 + \angle 3 = 180$ and $\angle 2 + \angle 3 = 180$. Using Substitution we get $\angle 1 + \angle 3 = \angle 2 + \angle 3$. Then we can subtract $\angle 3$ from both sides using the Subtraction Property of Equality and get $\angle 1 = \angle 2$.

Given: $\angle 1 \cong \angle 3$



$$\therefore \angle 2 \cong \angle 4$$

Step

1. $\angle 1 \cong \angle 3$
2. $\angle 1 + \angle 2 \cong 180^\circ$
 $\angle 3 + \angle 4 \cong 180^\circ$
3. $\angle 1 + \angle 2 \cong \angle 3 + \angle 4$
4. $\angle 1 + \angle 2 \cong \angle 1 + \angle 4$
5. $\angle 2 \cong \angle 4$

Reason

1. Given
2. Angle Add Post
3. Substitution
4. Substitution
5. Subtraction Post of \cong

Proving the Vertical Angles Theorem

Step

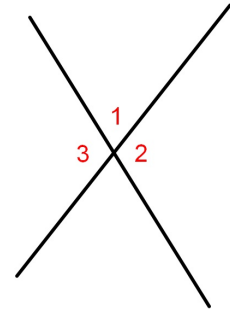
1. $\angle 1 + \angle 3 \cong 180^\circ$
 $\angle 1 + \angle 2 \cong 180^\circ$

Reason

1. Angle Add Post

2. $\angle 1 + \angle 3 \cong \angle 1 + \angle 2$ 2. Subst.

3. $\angle 3 \cong \angle 2$ 3. Subtr. prop =

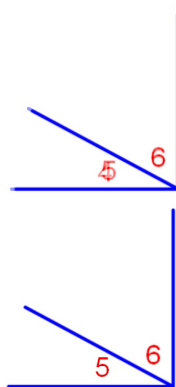


What conclusion can you make from the given information?

Angle 4 is complementary to Angle 6.

Angle 5 is complementary to Angle 6.

$$\therefore \angle 4 \cong \angle 5$$



Theorem 2-3

Congruent Complements Theorem

If two angles are complements of the same angle (or of congruent angles), then the two angles are congruent.

Given:

Angle 4 is complementary to Angle 6.

Angle 5 is complementary to Angle 6.

Steps	Reasons
1. Angle 4 is supplementary to Angle 6 Angle 5 is supplementary to Angle 6	1. Given
2. $\angle 4 + \angle 6 = 90^\circ$ $\angle 5 + \angle 6 = 90^\circ$	2. Def of comp
3. $\angle 4 + \angle 6 = \angle 5 + \angle 6$	3. Substitution
4. $\angle 4 = \angle 5$	4. subtr prop =

What conclusion can you make from the given information?

Angle P is a right angle

Angle Q is a right angle

$$\therefore \angle P \cong \angle Q$$

Theorem 2-4

All right angles are congruent.

Given: Angle P is a right angle
Angle Q is a right angle

Steps	Reasons
1. Angle P is a right angle Angle Q is a right angle	1. Given
2. $\angle P = 90^\circ$ and $\angle Q = 90^\circ$	2. Def. of Rt. Angle
3. $\angle P = \angle Q$	3. Substitution

Given: Angles G and H are supplementary
Angles G and H are congruent.

\therefore

Theorem 2-5

If two angles are congruent and supplementary, then each is a right angle.