

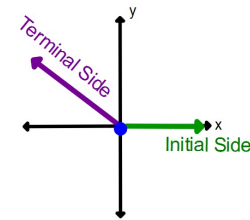
Wednesday, April 22, 2020

Angles in Standard Position and Reference Angles

Angles in Standard Position:

Vertex is at the origin.

One of the rays (sides) is on the positive x-axis.



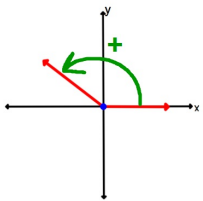
Initial Side:
The side on the Positive x-axis.

It's where the angle starts

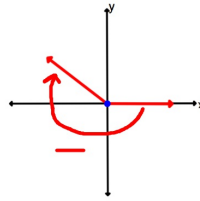
Terminal Side:
The other ray that forms the angle.

It's where the angle stops.

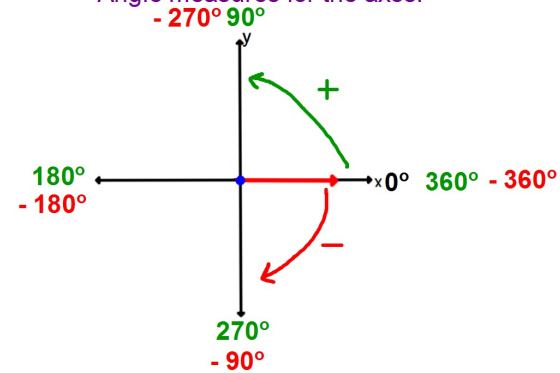
Positive Angles are measured starting from the positive x-axis and rotating in a **Counter-Clockwise** direction.



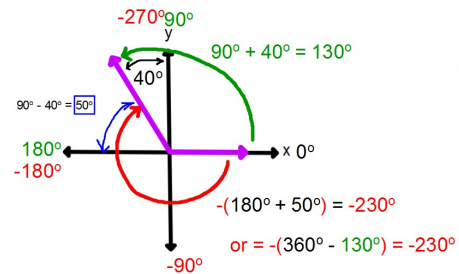
Negative Angles are measured starting from the positive x-axis and rotating in a **Clockwise** direction.



Angle measures for the axes:



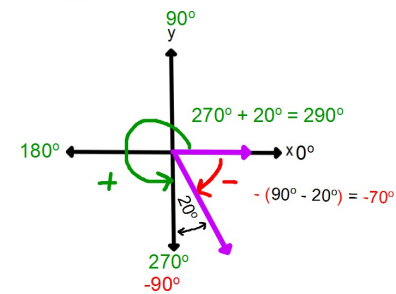
State both a **positive** and **negative** measure for this angle in **Standard Position**.



Pos: $\theta = 130^\circ$

Neg: $\theta = -230^\circ$

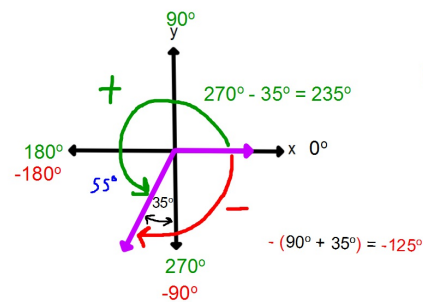
State both a **positive** and **negative** measure for this angle in **Standard Position**.



Pos: $\theta = 290^\circ$

Neg: $\theta = -70^\circ$

State both a **positive** and **negative** measure for this angle in **Standard Position**.



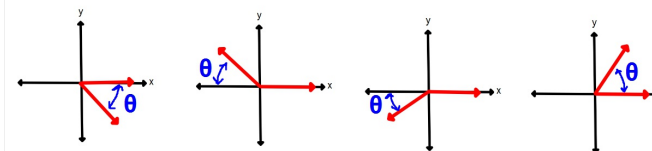
Pos: $\theta = 235^\circ$

Neg: $\theta = -125^\circ$

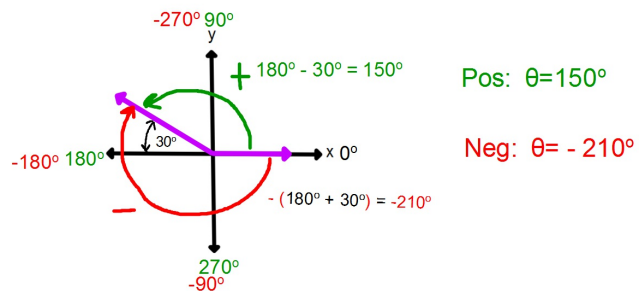
Reference Angle:

The acute angle formed by the terminal side and the x-axis.

θ is the reference angle for each angle shown in Standard Position



Use the given reference angle to state both a **positive** and **negative** measure for this angle in **Standard Position**.



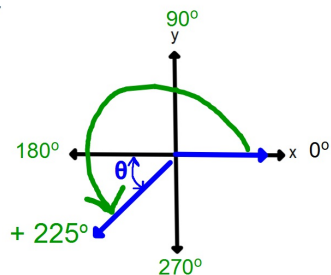
The measure of a **Reference Angle** can be calculated by finding the difference between the terminal side of the **Given Angle** and the measure at the **nearest x-axis**.

A **Reference Angle** is always positive so you'll be finding the POSITIVE difference (i.e. absolute value).

State the reference angle for the given angle that is in Standard Position:

$$\theta = 225^\circ$$

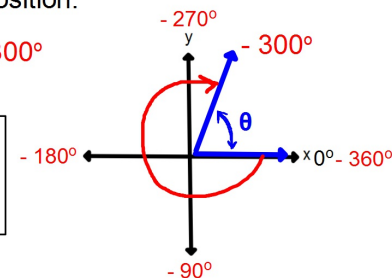
Reference angle
$\theta = 225^\circ - 180^\circ$
$\theta = 45^\circ$



State the reference angle for the given angle that is in Standard Position:

$$\theta = -300^\circ$$

Reference angle
$\theta = -300^\circ - -360^\circ $
$\theta = 60^\circ$



You can now do Practice #20.