

Tuesday, March 24, 2020

## Sec 7-2: Angles and the Unit Circle



Right triangle trigonometry involves  
the non-right angles of the triangle.

and using SOHCAHTOA

This means you were only able to  
find the Sin, Cos, and Tan of acute  
angles.

There are many other angles besides acute angles!

Angles can be bigger than  $90^\circ$  but less than  $180^\circ$ ....

bigger than  $180^\circ$  ....

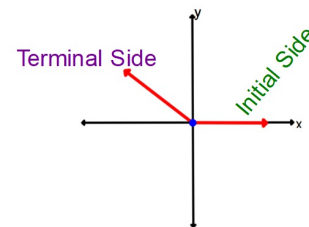
and even bigger than  $360^\circ$  !

Angles can even be negative.

Angles in Standard Position:

Vertex is at the origin.

One of the rays (sides) is on the positive x-axis.



Initial Side:

The side on the Positive x-axis.

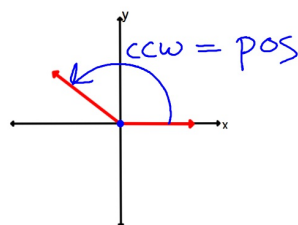
It's where the angle starts

Terminal Side:

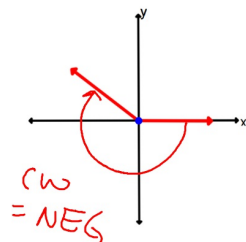
The other ray that forms the angle.

It's where the angle stops.

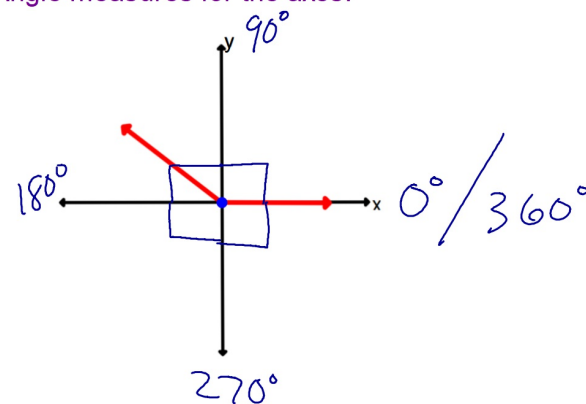
**Positive Angles** are measured starting from the positive x-axis and rotating in a **Counter-Clockwise** direction.



**Negative Angles** are measured starting from the positive x-axis and rotating in a **Clockwise** direction.



**Angle measures for the axes:**

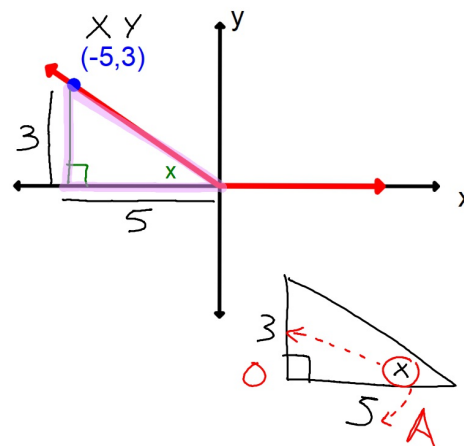
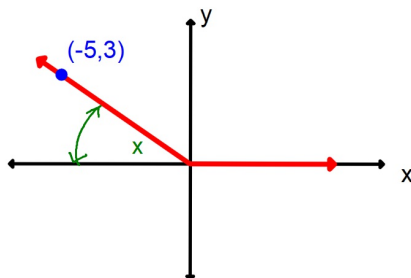


Find the measure of the angle shown.

Start by creating a **Reference Angle**

**Reference Angle:**

The acute angle formed by the terminal side and the x-axis.



1. Create a right  $\Delta$  with the terminal and the x-axis.
2. Label the sides of this  $\Delta$  using the coordinates of the given point.
3. Use an inverse trig function to find this reference angle.

SOHCAHTOA

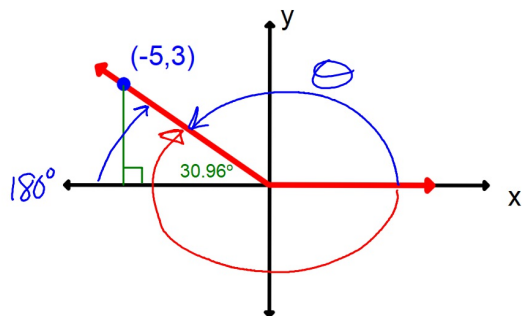
$$\tan x = \frac{3}{5}$$

$$x = \tan^{-1}\left(\frac{3}{5}\right)$$

$$x = 30.96^\circ$$



Use the reference angle to find the measure of the original given angle.



Positive measure:

$$\theta = 180^\circ - 30.96^\circ$$

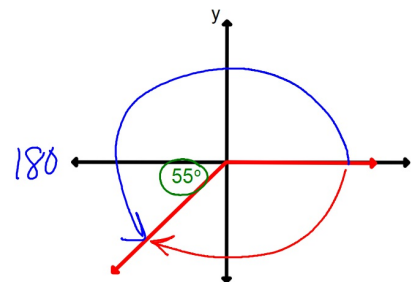
$$\theta = 149.04^\circ$$

Negative measure:

$$\theta = -(180 + 30.96)$$

$$\theta = -210.96^\circ$$

Find both a positive and negative angle measure for the angle in standard position with the given reference angle.



Positive measure:

$$\theta = 180 + 55$$

$$\theta = 235^\circ$$

Negative measure:

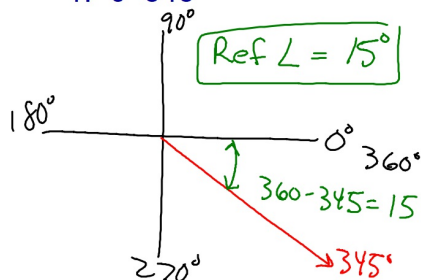
$$\theta = -(180 - 55)$$

$$\theta = -125^\circ$$

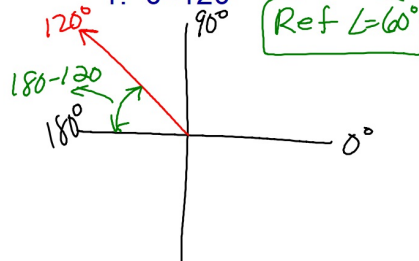


State the reference angle for each given angle that is in Standard Position:

1.  $\theta = 345^\circ$



1.  $\theta = 120^\circ$



You can now do Practice #7 which is posted on my blog.

