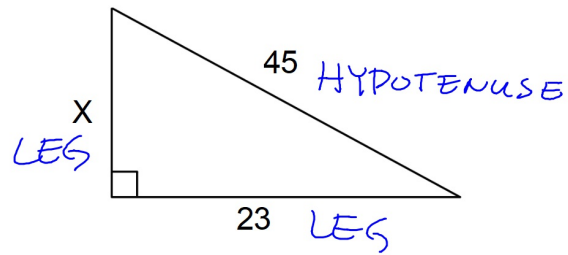


Find the value of x to the nearest hundredth.



Pythagorean Theorem:  
Hypotenuse<sup>2</sup> = Leg<sup>2</sup> + Leg<sup>2</sup>

$$45^2 = 23^2 + x^2$$

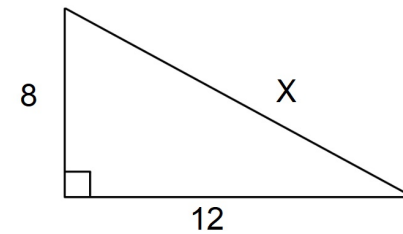
$$-23^2 \quad -23^2$$

$$x^2 = 45^2 - 23^2$$

$$x = \sqrt{45^2 - 23^2}$$

$$x = 38.68$$

Find the EXACT value of x. Give answer in simplified radical form.



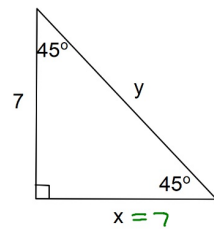
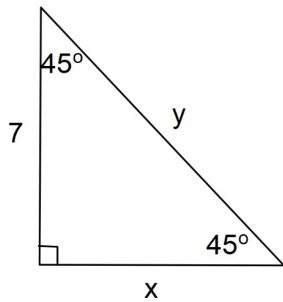
$$x^2 = 8^2 + 12^2$$

$$\sqrt{x^2} = \sqrt{208}$$

$$\sqrt{16 \cdot 13}$$

$$x = 4\sqrt{13}$$

Find the value of each missing side. Leave non-integer answers in simplified radical form.



THIS IS an  
Isosceles  $\Delta$   
so the legs  
are  $\cong$   
 $x = 7$

To find y:

$$y^2 = 7^2 + 7^2$$

$$y^2 = 49 + 49$$

$$y^2 = 98$$

$$y = \sqrt{98}$$

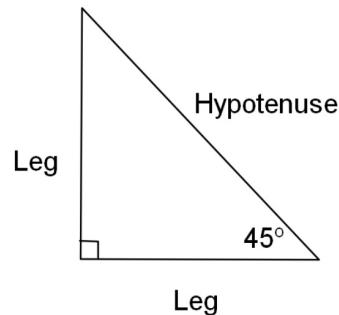
$$y = 7\sqrt{2}$$

Special Right Triangles.

# 45° - 45° - 90° Triangle:

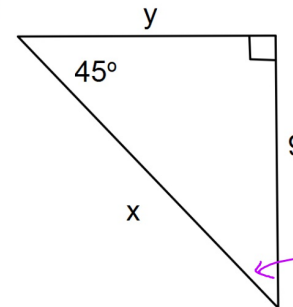
also known as an isosceles right triangle.

- Legs are congruent
- Hypotenuse =  $\text{Leg} \cdot \sqrt{2}$
- $\text{Leg} = \frac{\text{Hypotenuse}}{\sqrt{2}}$



Find the value of each missing side.  
Give answers in simplified radical form.

1.



THIS IS a 45-45-90  $\Delta$   
Legs are  $\cong$

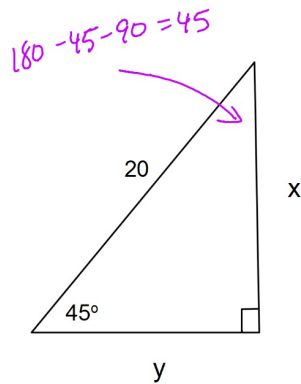
$$y = 9$$

$$\text{hypot} = \text{Leg} \cdot \sqrt{2}$$

$$x = 9\sqrt{2}$$

$$180 - 45 - 90 = 45$$

2.



THIS IS a 45-45-90  $\Delta$   
legs are  $\cong$

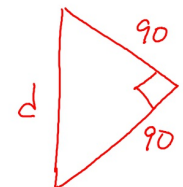
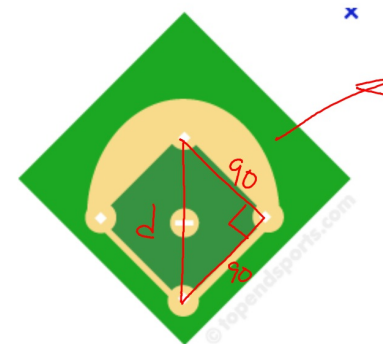
$$x = y = \frac{\text{hypot}}{\sqrt{2}}$$

$$x = y = \frac{20}{\sqrt{2}} \cdot \frac{\sqrt{2}}{\sqrt{2}}$$

$$x = y = \frac{20\sqrt{2}}{2}$$

$$x = y = 10\sqrt{2}$$

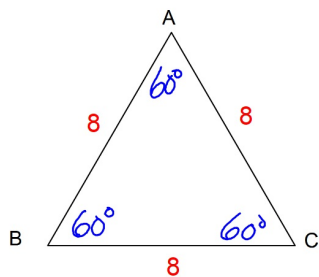
A baseball diamond is a square formed by the four bases.  
The bases are 90 feet apart. How far is it across  
the diamond from home plate to second base?



THIS IS a 45-45-90  $\Delta$   
 $\text{hypot} = \text{Leg} \cdot \sqrt{2}$

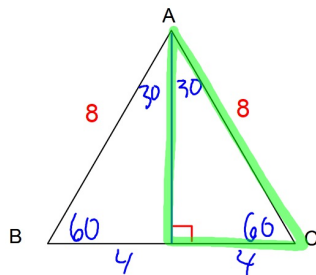
$$d = 90\sqrt{2}$$

ABC is an equilateral triangle.  
All sides have a length of 8.



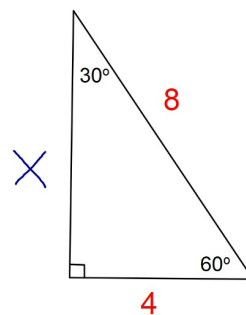
Draw an altitude from pt. A.

What does this altitude do to the triangle?



The altitude bisects  $\angle A$  and  $\overline{BC}$

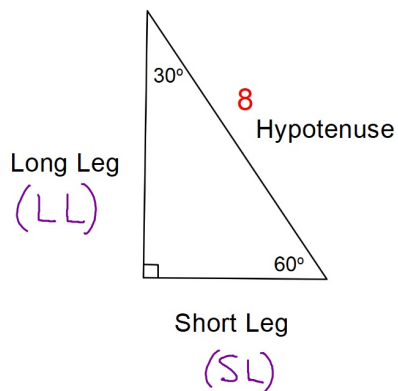
Find the length of the third side in simplified radical form.



$$\begin{aligned} 8^2 &= 4^2 + x^2 \\ 64 &= 16 + x^2 \\ \sqrt{48} &= \sqrt{x^2} \\ \sqrt{16 \cdot 3} &= x \end{aligned}$$

$$x = 4\sqrt{3}$$

30° - 60° - 90° Right Triangle:



- the Hypotenuse is always opposite the right angle.
- the Long Leg is always opposite the 60° angle.
- the Short Leg is always opposite the 30° angle.

Short Leg  $\longleftrightarrow$  Hypotenuse

$$SL = \text{Hypot} \div 2$$

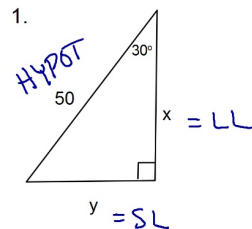
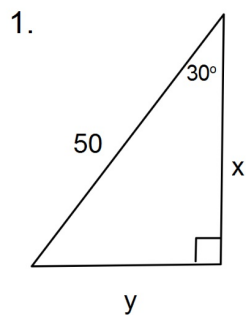
$$\text{Hypot} = SL \times 2$$

Short Leg  $\longleftrightarrow$  Long Leg

$$SL = LL \div \sqrt{3}$$

$$LL = SL \times \sqrt{3}$$

Find the **EXACT** value of  $x$  and  $y$  in each triangle. Give answers in simplified radical form.

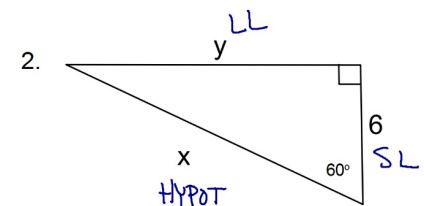
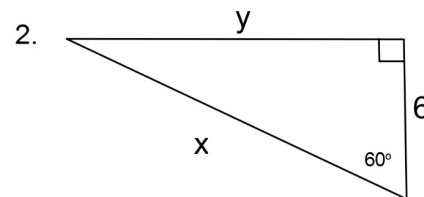


$$SL = \text{HYPOT} \div 2$$

$$y = 50 \div 2 = 25$$

$$LL = SL \cdot \sqrt{3}$$

$$x = 25 \cdot \sqrt{3}$$



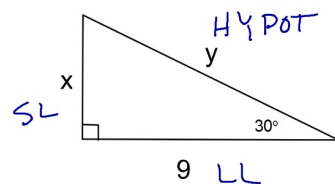
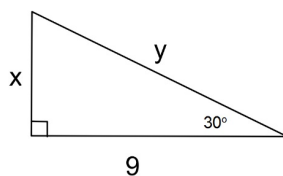
$$LL = SL \cdot \sqrt{3}$$

$$y = 6\sqrt{3}$$

$$\text{HYPOT} = SL \cdot 2$$

$$x = 6 \cdot 2 = 12$$

3.



$$SL = LL \div \sqrt{3}$$

$$x = \frac{9}{\sqrt{3}} \cdot \frac{\sqrt{3}}{\sqrt{3}} = \frac{9\sqrt{3}}{3}$$

$$x = 3\sqrt{3}$$

$$\text{HYPOT} = SL \cdot 2$$

$$y = 3\sqrt{3} \cdot 2$$

$$y = 6\sqrt{3}$$

Hwk #13

Practice Sheet: Special Right Triangles.

Find the **EXACT** value of each variable. Give answers in simplified radical form.