

The number of cells of a bacteria doubles every 40 minutes.
There was 24 cells at 10:00 am. Find the number of cells at the given times, the same day.

$a = 24$ cells $b = 2$ $x = \#$ of 40 min periods

a) Noon.

10:00 am to noon is 2 hours.
2 hours = $(2)(60) = 120$ minutes

$$x = 120 \div 40 = 3$$

$$y = 24(2)^3 = 192 \text{ cells}$$

b) 5:00 pm.

10:00 am to 5:00 pm is 7 hours.
7 hours = $(7)(60) = 420$ minutes

$$x = 420 \div 40 = 10.5$$

$$y = 24(2)^{10.5} = 34,756 \text{ cells}$$

The half-life of a certain medicine is 80 minutes. A patient was given a 200mg dose of at 6:00am. Find the amount of medicine in the patients system at the following times. Round to the nearest hundredth. $a = 200\text{mg}$ $b = 0.5$ $x = \#$ of 80 min periods

a) 11:00 am.

6:00 am to 11:00 am is 5 hours.
5 hours = $(5)(60) = 300$ minutes

$$x = 300 \div 80 = 3.75$$

$$y = 200(0.5)^{3.75} = 14.87 \text{ mg}$$

b) 3:30 pm.

6:00 am to 3:30 pm is 9.5 hours.
9.5 hours = $(9.5)(60) = 570$ minutes

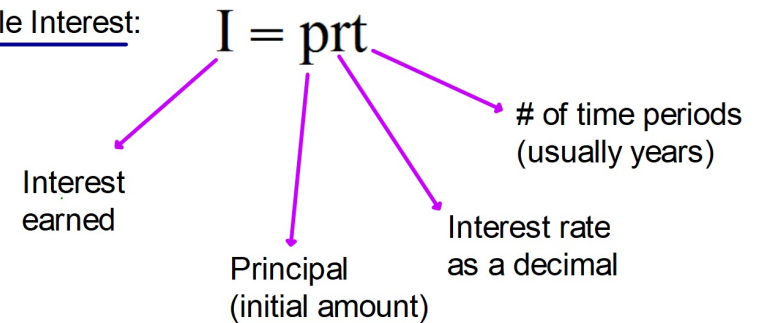
$$x = 570 \div 80 = 7.125$$

$$y = 200(0.5)^{7.125} = 1.43 \text{ mg}$$

Simple Interest:

You only earn interest in the initial amount you invested.

Simple Interest:



You invest \$10,000 in an account that pays 8% annual interest.

How much will you have after 10 years if you only get simple interest?

$$I = 10000(.08)(10)$$

Interest earned = 8000

$$\begin{aligned}\text{Total amount after 10 years} &= \text{Principal} + \text{Interest} \\ &= 10,000 + 8,000 \\ &= \$18,000\end{aligned}$$

Compounding Interest: earning interest on the interest.

You invest \$10,000 in an account that pays 8% annual interest.

How much will you have after 10 years if interest is compounded annually?

$$\begin{aligned}\text{end of 1st year you'll have:} & 10,000(1.08) \\ \text{end of 2nd year you'll have:} & 10,000(1.08)(1.08) \\ \text{end of 3rd year you'll have:} & 10,000(1.08)(1.08)(1.08)\end{aligned}$$

This is basic exponential growth. After 10 years you'll have:
 $10,000(1.08)^{10} = \$21,589.25$

You invest \$10,000 in an account that pays 8% annual interest.

How much more will you have after 20 years if interest is compounded annually versus simple interest?

Simple Interest: $10,000 + 10,000(.08)(20) = \$26,000$

Compounded Interest: $10,000(1.08)^{20} = \$46,609.57$

What if you compound interest more often than once a year (annually)?

The **compound interest formula** is an exponential model that is used to calculate the value of an investment when interest is compounded.

$$A = P\left(1 + \frac{r}{n}\right)^{nt}$$

P = the initial principal invested
 r = annual interest rate, written as a decimal
 n = number of compounding periods per year
 A = the value of the account after t years

Example 2 Try It! Understanding Continuously Compounded Interest

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2. \$3,000 is invested in an account that earns 3% annual interest, compounded monthly. $P = 3000$ $r = 0.03$ $n = 12$

a. What is the value of the account after 10 years?

$$t = 10$$

$$A = 3000(1+0.03/12)^{(12)(10)} = \$4048.06$$

b. What is the value of the account after 100 years? $t = 100$

$$A = 3000(1+0.03/12)^{(12)(100)} = \$60,031.45$$