

Bellwork Alg 2 Tuesday, January 28, 2020

Rewrite and simplify each expression using properties of exponents. Make sure your answer has no exponents that are negative or zero.

1. $\left(\frac{ab^5}{a^{\frac{1}{4}}}\right)^{\frac{4}{5}}$

2. $\left(k^{\frac{7}{6}}\right)^{-3}$

3. $\left(25^{\frac{3}{4}}m^{\frac{5}{2}}n^{-6}\right)^{\frac{2}{3}}$

Rewrite and simplify each expression using properties of exponents. Make sure your answer has no exponents that are negative or zero.

$$\begin{aligned}
 1. \quad \left(\frac{ab^5}{a^{\frac{1}{4}}} \right)^{\frac{4}{5}} &= (a^{1-\frac{1}{4}} b^5)^{\frac{4}{5}} = (a^{\frac{3}{4}} b^5)^{\frac{4}{5}} \\
 &= (a^{\frac{3}{4}})^{\frac{4}{5}} (b^5)^{\frac{4}{5}} \\
 &= a^{\frac{3}{4} \cdot \frac{4}{5}} b^{5 \cdot \frac{4}{5}} \\
 &= a^{\frac{3}{5}} b^4 \text{ or } \sqrt[5]{a^3 b^4}
 \end{aligned}$$

$$\begin{aligned}
 2. \quad \left(k^{\frac{7}{6}} \right)^{-3} &= \frac{1}{(k^{\frac{7}{6}})^3} = \frac{1}{k^{\frac{7}{6} \cdot 3}} = \frac{1}{k^{\frac{7}{2}}} \text{ or } \frac{1}{\sqrt{k^7}}
 \end{aligned}$$

$$\begin{aligned}
 3. \quad \left(25^{\frac{3}{4}} m^{\frac{5}{2}} n^{-6} \right)^{\frac{2}{3}} &= \left(\frac{25^{\frac{3}{4}} m^{\frac{5}{2}}}{n^6} \right)^{\frac{2}{3}} = \frac{(25^{\frac{3}{4}})^{\frac{2}{3}} (m^{\frac{5}{2}})^{\frac{2}{3}}}{(n^6)^{\frac{2}{3}}} \\
 &= \frac{25^{\frac{3}{4} \cdot \frac{2}{3}} m^{\frac{5}{2} \cdot \frac{2}{3}}}{n^{6 \cdot \frac{2}{3}}} \\
 &= \frac{25^{\frac{1}{2}} m^{\frac{5}{3}}}{n^4} = \frac{\sqrt{25} \sqrt[3]{m^5}}{n^4} \\
 &= \frac{5 \sqrt[3]{m^5}}{n^4} \text{ or } \frac{5 m^{\frac{5}{3}}}{n^4}
 \end{aligned}$$