

Alg 2 Problems after Topic 6 Quiz Name:

1. Factor each completely.

a) $6x^3 - 14x^2 + 9x - 21$

b) $6x^4 + 10x^3 - 24x^2 - 40x$

2. Use division to determine the linear factors of $7x^4 - 54x^3 + 138x^2 - 103x - 42$ if $x^2 - 5x + 7$ is a factor.
Then state all four solutions.

Alg 2 Problems after Topic 6 Quiz

Name:

Answers

1. Factor each completely.

a) $6x^3 - 14x^2 + 9x - 21$

No GCF

$$\begin{array}{r} 3x \quad -7 \\ \hline 2x^2 \left| \begin{array}{c|c} 6x^3 & -14x^2 \\ \hline +3 & +9x \end{array} \right. \\ \hline -21 \end{array}$$

$$(3x - 7)(2x^2 + 3)$$

b) $6x^4 + 10x^3 - 24x^2 - 40x$

GCF = 2x

$$2x \underbrace{(3x^3 + 5x^2 - 12x - 20)}$$

$$\begin{array}{r} 3x \quad +5 \\ \hline x^2 \left| \begin{array}{c|c} 3x^3 & +5x^2 \\ \hline -4 & -12x \end{array} \right. \\ \hline -20 \end{array}$$

$$2x(3x+5)(x^2-4)$$

$$2x(3x+5)(x \pm 2)$$

2. Use division to determine the linear factors of $7x^4 - 54x^3 + 138x^2 - 103x - 42$ if $x^2 - 5x + 7$ is a factor. Then state all four solutions.

$$\begin{array}{r} 7x^2 \quad -19x \quad -6 \\ \hline x^2 - 5x + 7 \left| \begin{array}{r} 7x^4 - 54x^3 + 138x^2 - 103x - 42 \\ - 7x^4 - 35x^3 + 49x^2 \\ \hline - 19x^3 + 89x^2 - 103x \\ - 19x^3 + 95x^2 - 133x \\ \hline - 6x^2 + 30x - 42 \\ - 6x^2 + 30x - 42 \\ \hline 0 \end{array} \right. \end{array}$$

$$(x^2 - 5x + 7)(7x^2 - 19x - 6)$$

0

$$b^2 - 4ac = -3$$

$$\frac{5 \pm \sqrt{-3}}{2}$$

$$= \frac{5 \pm i\sqrt{3}}{2}$$

$$(7x + 2)(x - 3)$$

$$X = -\frac{2}{7}, 3, \frac{5 \pm i\sqrt{3}}{2}$$