

## Algebra 2 Polynomial Application Problem Fall 2019

The length of a rectangle is defined by the following expression:  $7 - 2x$

The width of this rectangle is defined by the following expression:  $2x - 1$

1. Write an equation for the area of this rectangle in terms of  $x$ .

a) Write this equation factored form:

$A(x) =$

b) Give answer in Standard Form:

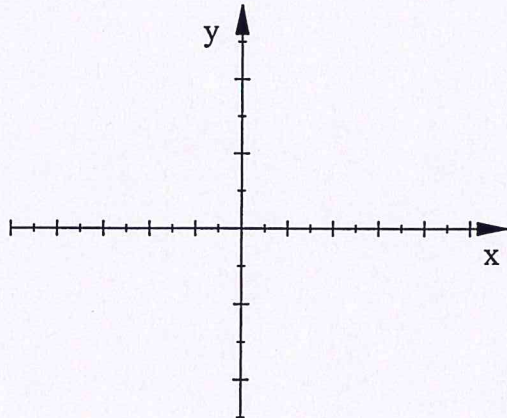
$A(x) =$

2. What is the domain of both of these equations?

3. What is the domain of these equations taking into consideration the real situation these equations represent?

(Hint: keep in mind that neither Length nor Width can be a negative value)

4. Graph one of these equations on your graphing calculator in a Standard Window. The two equations should result in the same graph. Sketch this on the graph below.



5. What value of  $x$  will lead to the maximum area? Round to the nearest hundredth.

6. What is the maximum area? Round to the nearest hundredth.

# Algebra 2 Polynomial Application Problem Fall 2019

ANSWERS

The length of a rectangle is defined by the following expression:  $7 - 2x$

The width of this rectangle is defined by the following expression:  $2x - 1$

1. Write an equation for the area of this rectangle in terms of  $x$ .

a) Write this equation factored form:

$$A(x) = (7 - 2x)(2x - 1)$$

b) Give answer in Standard Form:

$$A(x) = -4x^2 + 16x - 7$$

2. What is the domain of both of these equations?  $(-\infty, \infty)$

3. What is the domain of these equations taking into consideration the real situation these equations represent?

(Hint: keep in mind that neither Length nor Width can be a negative value)

$$\begin{aligned} L > 0 &\rightarrow 7 - 2x > 0 \\ -7 &\quad -7 \\ -2x &> -7 \\ \frac{-2x}{-2} &> \frac{-7}{-2} \\ x &< 3.5 \end{aligned}$$

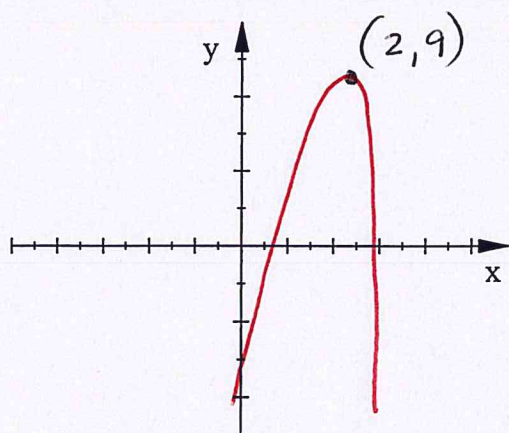
$$\begin{aligned} W > 0 &\rightarrow 2x - 1 > 0 \\ +1 &\quad +1 \\ 2x &> 1 \\ \frac{2x}{2} &> \frac{1}{2} \\ x &> \frac{1}{2} \end{aligned}$$

PUT THESE TOGETHER

$$\frac{1}{2} < x < 3.5$$

$$\left(\frac{1}{2}, 3.5\right)$$

4. Graph one of these equations on your graphing calculator in a Standard Window. The two equations should result in the same graph. Sketch this on the graph below.



line of symmetry  $x = \frac{-b}{2a} = \frac{-16}{2(-4)} = \frac{-16}{-8}$

$$y = -4x^2 + 16x - 7$$

$$x = 2$$

vertex  $(2, 9)$

$$\begin{aligned} &-4(2)^2 + 16(2) - 7 \\ &= -16 + 32 - 7 \\ &= 16 - 7 = 9 \end{aligned}$$

5. What value of  $x$  will lead to the maximum area? Round to the nearest hundredth.

2 x-coord of vertex

6. What is the maximum area? Round to the nearest hundredth.

9 y-coord of vertex