

Arithmetic Series: The sum of the terms in an
Arithmetic Sequence.
(change all commas to addition)

Sum of first n terms of an Arithmetic Sequence:

$$S_n = \frac{n}{2}(t_1 + t_n)$$

n = # of terms t_1 = First term
 t_n = Last term

Find the sum of the first 15 terms of the sequence defined by
this formula:

$$t_n = -12 + 5(n-1)$$

$\rightarrow n = 15$

$\rightarrow$ Arithmetic Sequence
where $t_1 = -12$

$$S_{15} = \frac{15}{2}(-12 + 58)$$

Last term = t_{15}

$$t_{15} = -12 + 5(15-1) = 58$$

$$S_{15} = 345$$

Find the sum of the terms in this sequence:

$9, 16, 23, 30, \dots, 93$ Arithmetic
 $d = 7$

$$S_n = \frac{n}{2}(t_1 + t_n)$$

$$= \frac{13}{2}(9 + 93)$$

$$= 6.5(102)$$

$$S_{13} = 663$$

Terms

Write the explicit formula and replace t_n with the last term. This means that n will represent the number of terms:

$$t_n = 9 + 7(n - 1)$$

$$93 = 9 + 7(n - 1)$$

$$\frac{84}{7} = \frac{7(n - 1)}{7}$$

$$12 = n - 1$$

$$n = 13 \text{ terms}$$

Σ - Uppercase Sigma - 18th letter of the Greek alphabet. represents "Sum of".

σ - lower case Sigma is used in statistics to represent Standard Deviation.

Do problem 12 on SAS2

12. Write the series represented by the sigma notation $\sum_{n=1}^5 (2 + 3n)$.

first 5 terms $\sum_{n=1}^5 (2 + 3n)$

explicit formula

n	$t_n = 2 + 3n$
1	$2 + 3(1) = 5$
2	$2 + 3(2) = 8$
3	$2 + 3(3) = 11$
4	$2 + 3(4) = 14$
5	$2 + 3(5) = 17$

$$5, 8, 11, 14, 17$$

[Play animation Panels 1 & 2](#)

Do problem 13 on SAS2

13. Represent the series $20 + 23 + 26 + 29 + 32 + 35 + 38 + 41 + 44 + 47 + 50 + 53$ using sigma notation.

Arithmetic Series $d = 3$

Explicit Formula: $t_n = 20 + 3(n-1)$

terms = 12

$$\sum_{n=1}^{12} 20 + 3(n-1)$$