

Remember in mathematics an **Identity** is

An equation that is true for EVERY value of x , in the domain.

OR

An equation where both sides are always equal, for every value of x in the domain.

When trying to verify/prove an identity you **CAN'T** do the following:

- Move terms from one side of the equation to the other side
- Multiply/divide/square/square root both sides of the equation
- Add/Subtract from both sides of the equation

You are **NOT** solving

You are trying to show the two sides of the equation are equal which means you don't know they are equal....YET.

Verifying trig identities:

Showing that the two sides of the equation really are equal.

Two basic techniques:

- Work on one side only and make it look like the other side.
- or
- Work on both sides until they look the same.

Verify this identity:

$$\begin{aligned} 1 + \cot A &= \csc A (\sin A + \cos A) \\ &= \frac{1}{\sin A} (\sin A + \cos A) \\ &= \frac{\sin A}{\sin A} + \frac{\cos A}{\sin A} \\ 1 + \cot A &= 1 + \cot A \end{aligned}$$

Verify this identity:

$$\tan \theta \cdot \sec \theta \cdot \cot \theta = \frac{\tan \theta}{\sin \theta}$$

$$\frac{\cancel{\sin}}{\cancel{\cos}} \cdot \frac{1}{\cos} \cdot \frac{\cancel{\cos}}{\cancel{\sin}} = \frac{\sin}{\cos \sin}$$

$$\frac{1}{\cos} = \frac{\sin}{\cos} \cdot \frac{1}{\sin}$$

$$\frac{1}{\cos} = \frac{1}{\cos}$$

Verify this trig identity.

$$\frac{1}{\tan x} + \tan x = \sec x \csc x$$

$$\cot + \tan = \frac{1}{\cos} \cdot \frac{1}{\sin}$$

$$\frac{\cos}{\cos} \cdot \frac{\cos}{\sin} + \frac{\sin}{\cos} \cdot \frac{\sin}{\sin} = \frac{1}{\cos \cdot \sin}$$

$$\frac{\cos^2}{\cos \cdot \sin} + \frac{\sin^2}{\cos \cdot \sin} =$$

$$\frac{\cos^2 + \sin^2}{\cos \cdot \sin} =$$

$$\frac{1}{\cos \cdot \sin} = \frac{1}{\cos \cdot \sin}$$

Verify this identity:

$$\frac{\sin x}{\tan x} + \frac{\cos x}{\cot x} = \sin x + \cos x$$

$$\frac{\sin}{\frac{\sin}{\cos}} + \frac{\cos}{\frac{\cos}{\sin}} =$$

$$\cancel{\sin} \cdot \frac{\cos}{\cancel{\sin}} + \cancel{\cos} \cdot \frac{\sin}{\cancel{\cos}} =$$

$$\cos x + \sin x = \sin x + \cos x$$