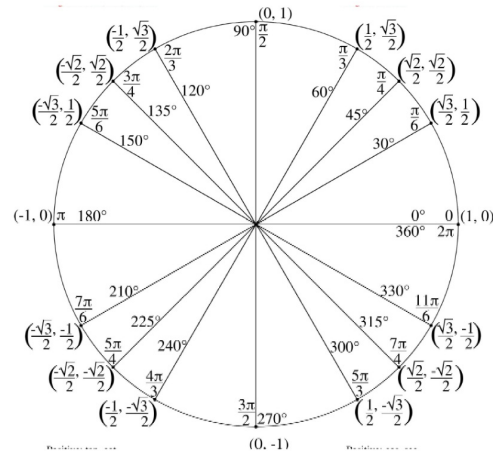


Using the Unit Circle:

How many different answers will there be for

$\sin \theta$

Since the sin of an angle on the Unit Circle is just the y-coordinate of the points on the Unit Circle this is just asking for all the DIFFERENT y-coordinates!



The different y-coordinates on the Unit Circle are:

$$0, \pm \frac{1}{2}, \pm \frac{\sqrt{2}}{2}, \pm \frac{\sqrt{3}}{2}, \pm 1$$

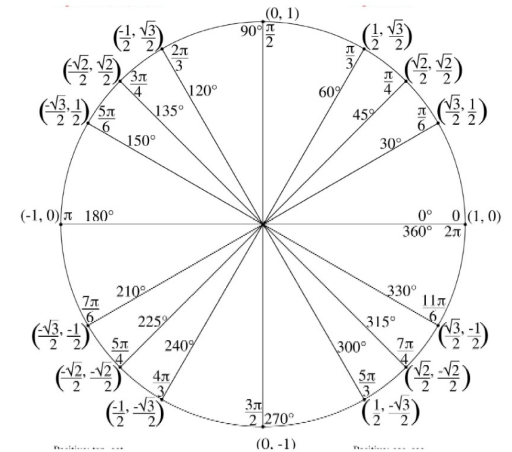
There are only 9 different answers that you will give when find the value of $\sin \theta$ using the Unit Circle.

Using the Unit Circle:

How many different answers will there be for

$\cos \theta$

Since the cos of an angle on the Unit Circle is just the x-coordinate of the points on the Unit Circle this is just asking for all the DIFFERENT x-coordinates!



The different x-coordinates on the Unit Circle are:

$$0, \pm \frac{1}{2}, \pm \frac{\sqrt{2}}{2}, \pm \frac{\sqrt{3}}{2}, \pm 1$$

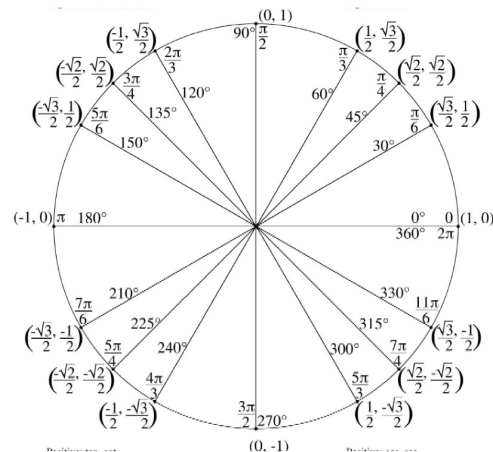
There are only 9 different answers that you will give when find the value of $\cos \theta$ using the Unit Circle. These are all the same answers that you will use to answer $\sin \theta$

Using the Unit Circle:

How many different answers will there be for

$\tan \theta$

Since the tan of an angle on the Unit Circle is just the ratio of y/x of the points on the Unit Circle this is just asking for all the DIFFERENT y/x ratios.



$$\frac{0}{\pm 1} = 0$$

$$\frac{\pm \frac{1}{2}}{\pm \frac{\sqrt{3}}{2}} = \pm \frac{1}{\sqrt{3}} \cdot \frac{\sqrt{3}}{\sqrt{3}} = \pm \frac{\sqrt{3}}{3}$$

$$\frac{\pm \frac{\sqrt{2}}{2}}{\pm \frac{\sqrt{2}}{2}} = \pm 1$$

$$\frac{\pm \frac{\sqrt{3}}{2}}{\pm \frac{1}{2}} = \pm \sqrt{3}$$

$$\pm \frac{1}{0} = \text{undefined}$$

These are the only 8 answers you'll give when finding $\tan \theta$

For the next 8 questions use these directions:

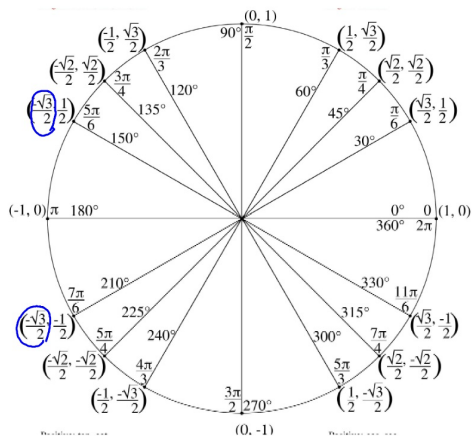
Use the given information to find the measure of all the angles θ that meet each condition.

θ in degrees ($0^\circ \leq \theta < 360^\circ$)

$$1. \cos \theta = -\frac{\sqrt{3}}{2}$$

Neg x-coord
Quad II & III

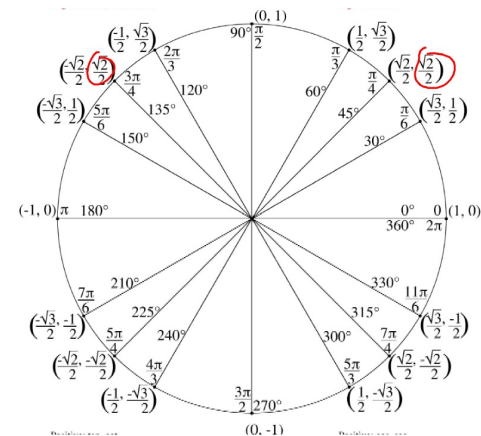
$$\theta = 150^\circ \text{ \& } 210^\circ$$



$$2. \sin \theta = \frac{\sqrt{2}}{2}$$

pos y-coord
Quad I & II

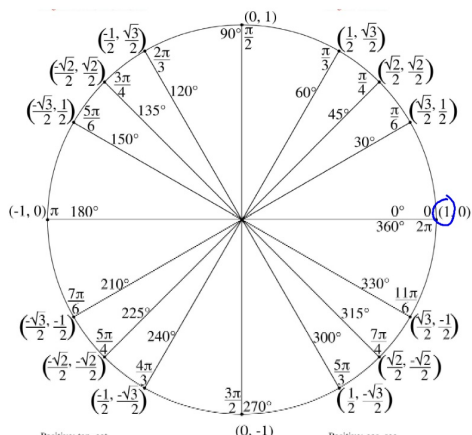
$$45^\circ \text{ \& } 135^\circ$$



$$3. \cos \theta = 1$$

x-coord = 1

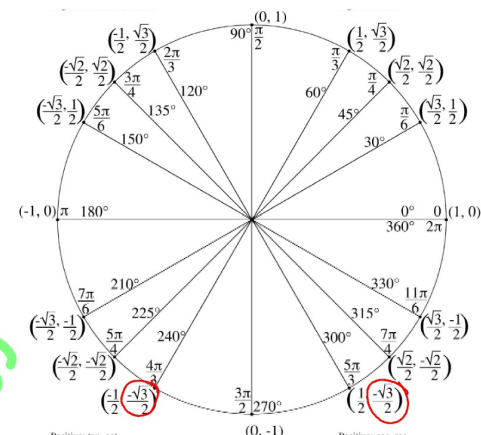
$$0^\circ, 360^\circ$$



$$4. \sin \theta = -\frac{\sqrt{3}}{2}$$

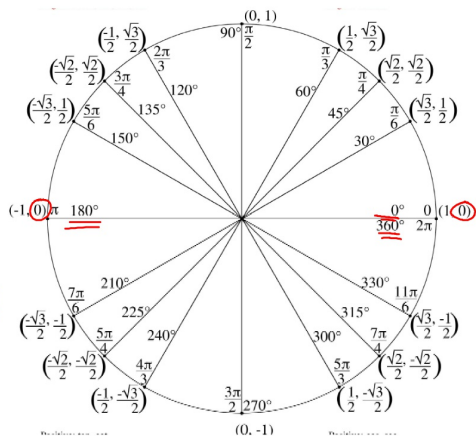
neg y-coord
Quad III & IV

$$240^\circ \text{ \& } 300^\circ$$



5. $\sin \theta = 0$
 $y=0 \rightarrow x\text{-axis}$

$0^\circ, 180^\circ, 360^\circ$

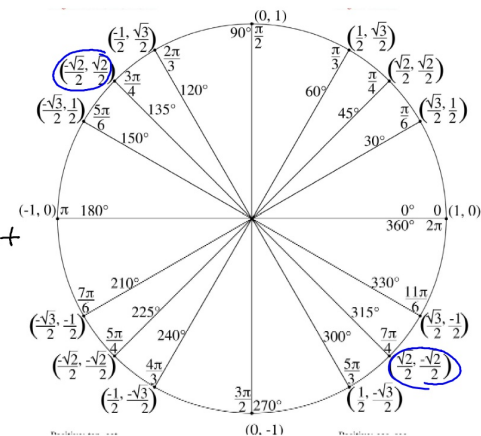


6. $\tan \theta = -1$

$\frac{y}{x}$ is neg when
 signs are different
 Quad II & IV

$\frac{y}{x} = -1$ when x & y
 are opposites

$135^\circ \text{ \& } 315^\circ$

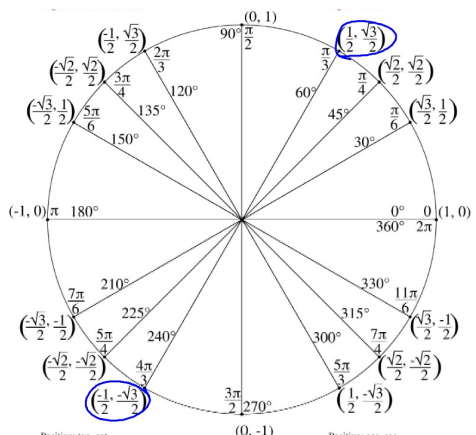


7. $\tan \theta = \sqrt{3}$

$\frac{y}{x}$ is pos when
 x & y are same sign
 Quad I & III

$\frac{y}{x} = \sqrt{3}$ when $\frac{y}{x} = \frac{\sqrt{3}}{1}$
 $x = 1$

$60^\circ \text{ \& } 240^\circ$

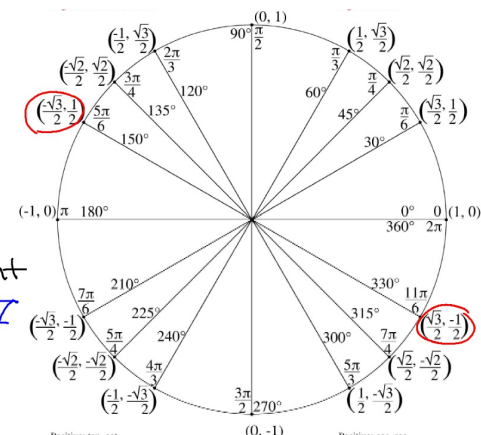


8. $\tan \theta = -\frac{\sqrt{3}}{3}$

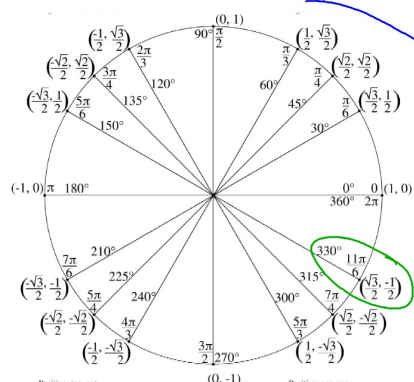
$\frac{y}{x}$ is neg when
 x & y have different
 signs Quad II & IV

$\frac{y}{x} = \frac{\sqrt{3}}{3}$ when $\frac{y}{x} = \frac{1}{\sqrt{3}}$
 $y = \frac{1}{\sqrt{3}}$
 $x = \frac{\sqrt{3}}{3}$

$150^\circ \text{ \& } 330^\circ$



9. Given $\cos\theta > 0$ and $\sin\theta = -\frac{1}{2}$ find θ



x is pos y is neg
(+, -) Quad IV

y -coord = $-\frac{1}{2}$

330°

10. Given $90^\circ \leq \theta \leq 180^\circ$

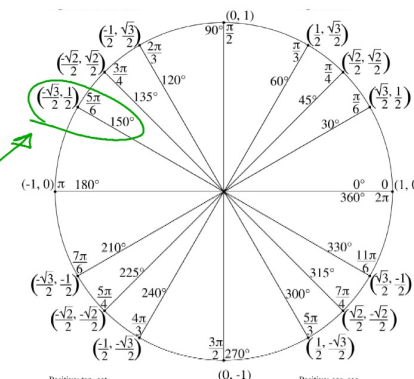
If $\cos\theta = -\frac{\sqrt{3}}{2}$ find $\sin\theta$

Quadrant II

x -coord is $-\frac{\sqrt{3}}{2}$

$\sin\theta = \frac{1}{2}$

y -coord at this same point

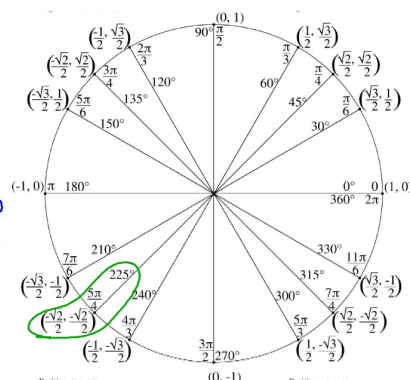


Given $\tan\theta > 0$ and $\sin\theta = -\frac{\sqrt{2}}{2}$,
find $\cos\theta$.

$\tan > 0 \rightarrow$ $\tan$ is pos when x & y have the same sign.
Quad I & III

$\sin\theta = -\frac{\sqrt{2}}{2}$ in Quad III

$\cos\theta = -\frac{\sqrt{2}}{2} \rightarrow$ x -coord at this same point.



You can now finish Hwk #17.

Practice Sheet: Using the Unit Circle

Due Monday, April 15, 2019

Suppose the you get on a Ferris Wheel at the spot marked with the star. Sketch the graph of your height above/below the spot marked with the star as the Ferris Wheel turns.

