

## Classwork from yesterday

1. What is the general form of the Reciprocal Family of functions:

page 495  $y = \frac{a}{x-h} + k$   $y = a \cdot \frac{1}{x-h} + k$

Previously studied functions:

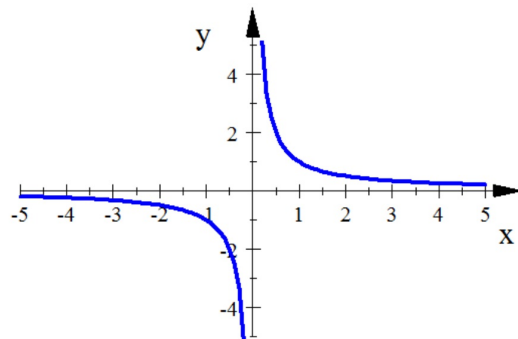
$$y = a|x-h| + k \quad y = a(x-h)^2 + k$$

$$y = a\sqrt{x-h} + k$$

$a$ ,  $h$ , and  $k$  represent the same thing in all of these equations!

2. a) Graph the Parent Reciprocal Function:  $Y_1 = \frac{1}{x}$  using the following window:

$$X_{\min} = -5 \quad X_{\max} = 5 \quad Y_{\min} = -5 \quad Y_{\max} = 5$$

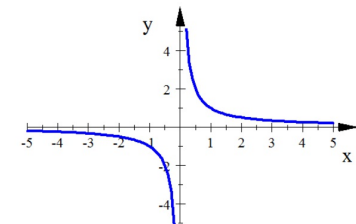


b) The graph has two parts. Explain why there is a break in the graph when  $x=0$ .

$$Y_1 = \frac{1}{x}$$

The equation is undefined when  $x=0$ , therefore, you are never allowed to use this value and the graph can't exist there.

$x=0$  is a restriction

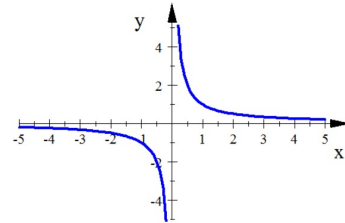


c)  $x = 0$  is called a Vertical Asymptote (VA).

i. Describe what the graph does as you get closer to the VA from the left side.

As  $x$  approaches zero from the left,  $y$  becomes very big negative.

The graph goes down as you get close to the  $y$ -axis on the left side.



ii. Describe what the graph does as you get closer to the VA from the right side.

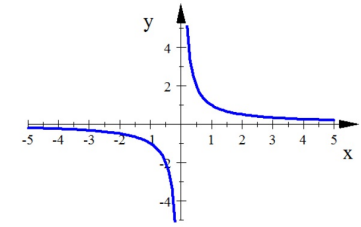
As  $x$  approaches zero from the right,  $y$  becomes very big positive.

The graph goes up as you get close to the  $y$ -axis on the right side.

3. a) What is each part of the graph called?

page 495

Branches



b) Where are these two parts of the graph located?

Quadrants I and III

Given this equation  $y = \frac{1}{x}$  explain why the branches are in these quadrants.

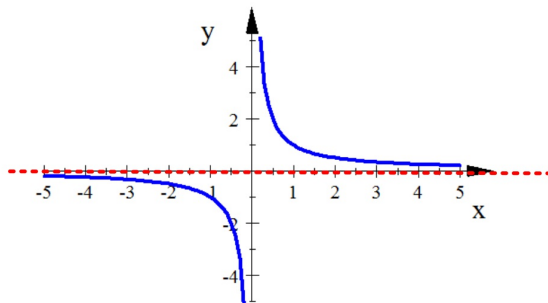
Substituting different values for  $x$  into the equation leads to the following:

When  $x$  is positive  $y$  is also positive - 1st Quadrant

When  $x$  is negative  $y$  is also negative - 4th Quadrant

4. What is the equation of the Horizontal Asymptote?

HA:  $y=0$  ( $x$ -axis)



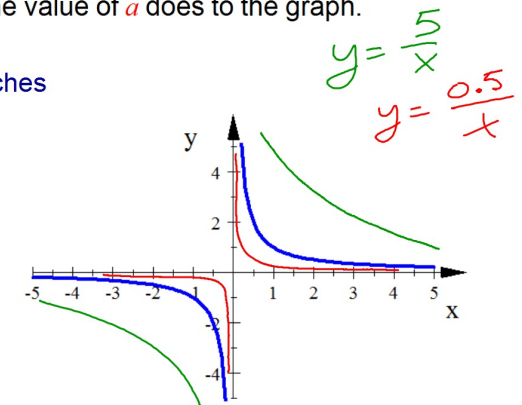
As you move farther left and right on the graph (bigger positive and bigger negative values for  $x$ )  $y$  becomes smaller and smaller but will never actually equal zero.

This means at the left and right ends of the graph it will get really close to the line  $y=0$  ( $x$ -axis) but never reach it.

5. Keep  $Y_1 = \frac{1}{x}$ . Now graph  $Y_2 = \frac{a}{x}$  trying different values of  $a$ , but keeping it positive. Explain what changing the value of  $a$  does to the graph.

Larger values of  $a$  push the branches "farther" from the origin.

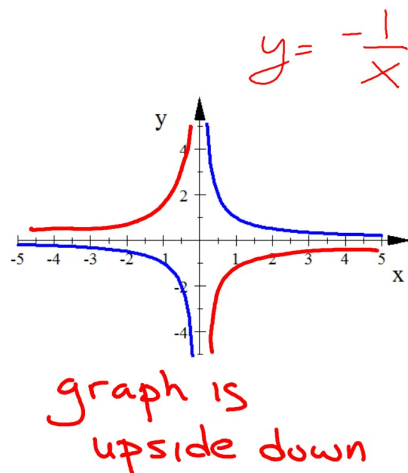
Smaller value of  $a$  bring the branches "closer" to the origin.



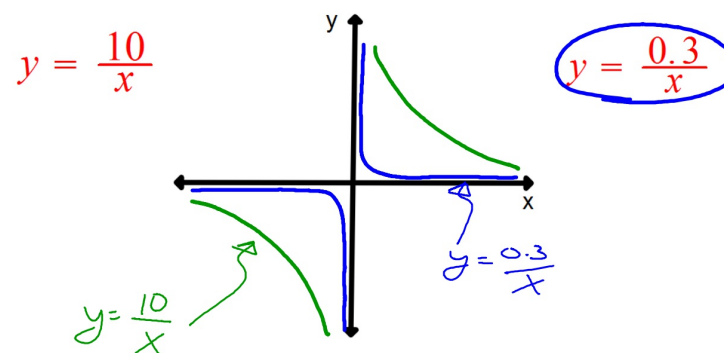
6. Keep  $Y_1 = \frac{1}{x}$ . Now graph  $Y_2 = \frac{a}{x}$  using a negative value of  $a$ . What happens to the graph when  $a$  is negative?

Negative values of  $a$  make the graph upside down (x-axis reflection).

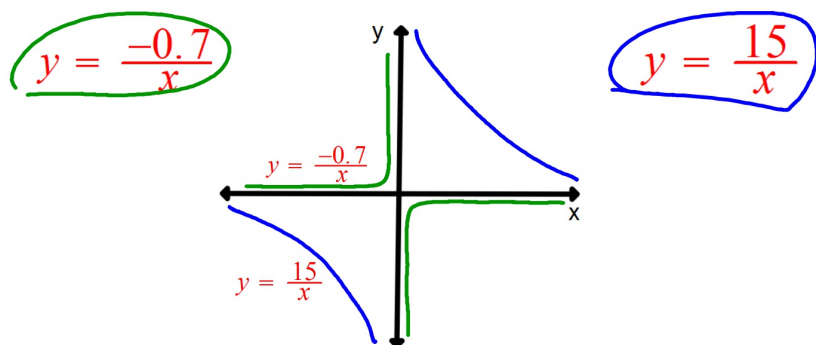
The branches are in Quadrants II and IV.



Without using a graphing calculator sketch the graph of each in the same x-y plane. Label the graphs with their equations.



Without using a graphing calculator sketch the graph of each in the same x-y plane. Label the graphs with their equations.

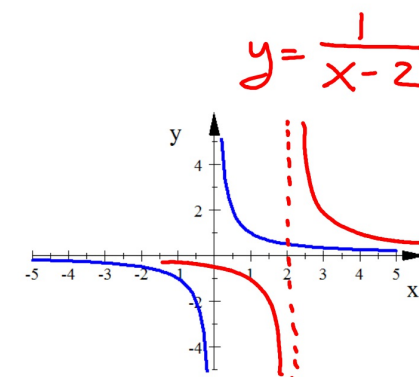


7. Keep  $Y_1 = \frac{1}{x}$  but graph using a Standard Window. Now graph  $Y_2 = \frac{1}{x-h}$ , trying different values of  $h$ , both positive and negative. Explain what changing the value of  $h$  does to the graph.

$h$  represents Horizontal Translation.

This changes the location of the Vertical Asymptote.

VA:  $x = h$



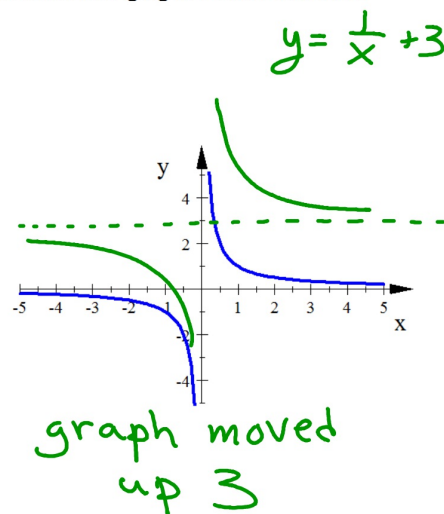
Graph moved 2 right

8. Keep  $Y_1 = \frac{1}{x}$  with a Standard Window. Now graph  $Y_2 = \frac{1}{x} + k$ , trying different values of  $k$ , both positive and negative. Explain what changing the value of  $k$  does to the graph.

$k$  represents Vertical Translation.

This changes the location of the Horizontal Asymptote.

HA:  $y = k$



What do you think the Vertical and Horizontal Asymptotes of this function are?

$$Y_1 = \frac{28.6}{x - 47} + 73$$

47 right      73 up

VA:  $x = 47$

HA:  $y = 73$

$$y = a(x - h)^2 + k \quad y = a|x - h| + k$$

$$y = a\sqrt{x - h} + k$$

a: Vertical Stretch or Shrink Factor  
if  $a < 0$  there is an x-axis reflection (Upside Down)

h: Horizontal Translation

Vertex for the Quadratic and Absolute Value functions is  $(h, k)$ .

k: Vertical Translation

The starting point for the Square Root function is  $(h, k)$

$$y = \frac{a}{x - h} + k$$

a: Vertical Stretch or Shrink Factor  
if  $a < 0$  there is an x-axis reflection (Upside Down)

The larger  $a$  is... the farther the branches are from the origin  
The smaller  $a$  is... the closer the branches are to the origin

h: Horizontal Translation

Vertical Asymptote becomes:  $x = h$

k: Vertical Translation

Horizontal Asymptote becomes:  $y = k$

$a > 0$ : branches are in Quadrants I & III  
 $a < 0$ : branches are in Quadrants II & IV

the Asymptotes will cross at the point  $(h, k)$

What are the two asymptotes for each reciprocal function?

1.  $y = \frac{30}{x-7} + 2$

HA:  $y = 2$

VA:  $x = 7$

2.  $y = \frac{-0.3}{x+5} - 8$

HA:  $y = -8$

VA:  $x = -5$

Write an equation for the translation of  $y = \frac{3}{x}$  that has the given asymptotes.

1.  $y = 4$  and  $x = -3$

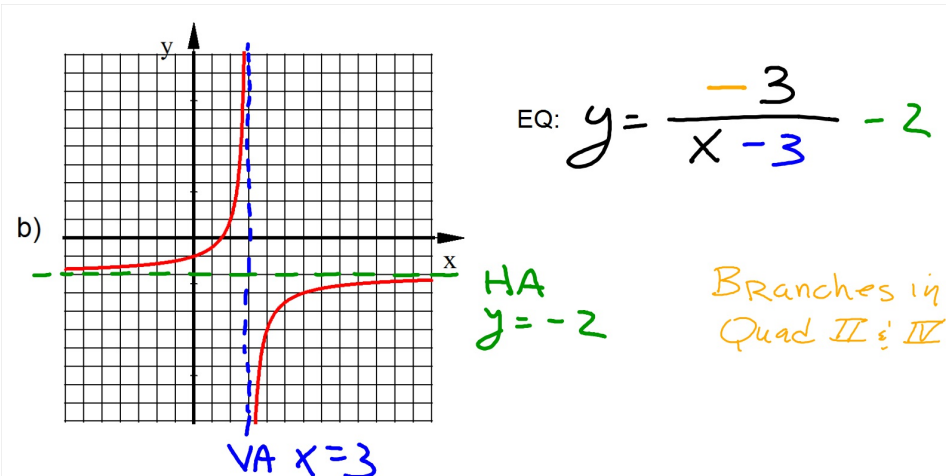
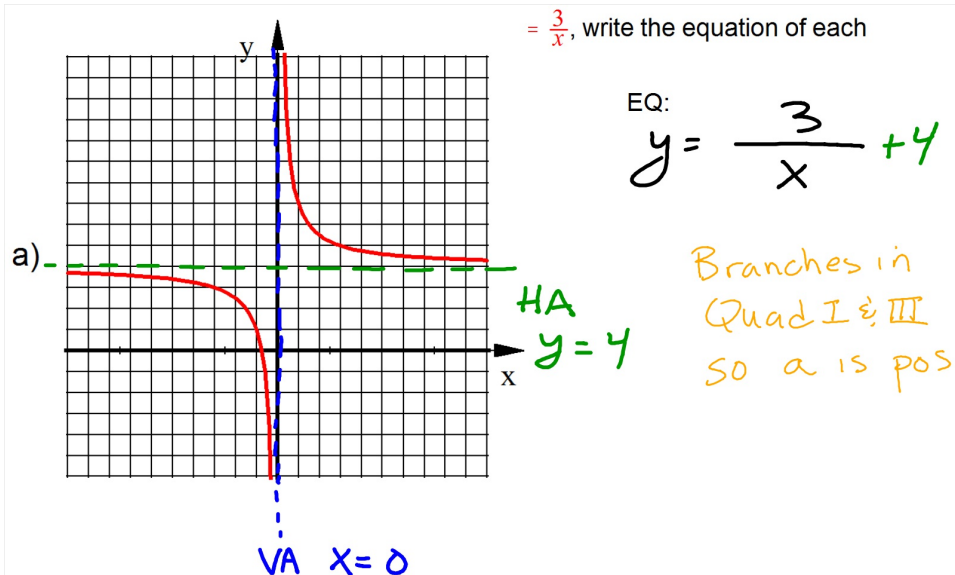
$y = \frac{3}{x+3} + 4$

2.  $y = 0$  and  $x = 9$

$y = \frac{3}{x-9}$

3.  $y = -5$  and  $x = 0$

$y = \frac{3}{x} - 5$

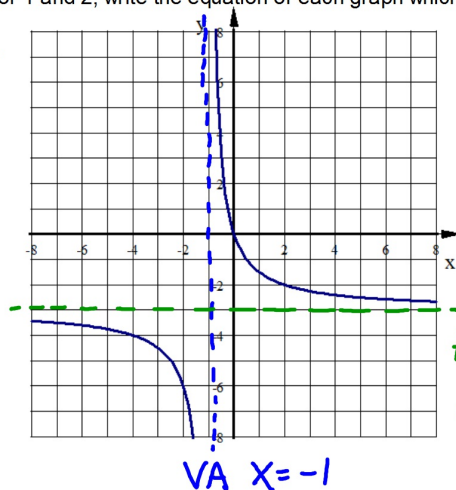




For 1 and 2, write the equation of each graph which are transformations of

the equation:  $y = \frac{3}{x}$

1.



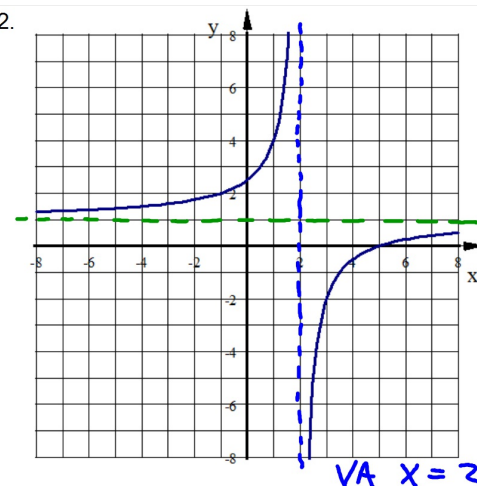
EQ:  $y = \frac{3}{x+1} - 3$

Branches are in Quad I & III so  $a$  is pos

HA  $y = -3$

VA  $x = -1$

2.



EQ:  $y = \frac{-3}{x-2} + 1$

HA  $y = 1$

Branches in Quad II & IV

VA  $x = 2$

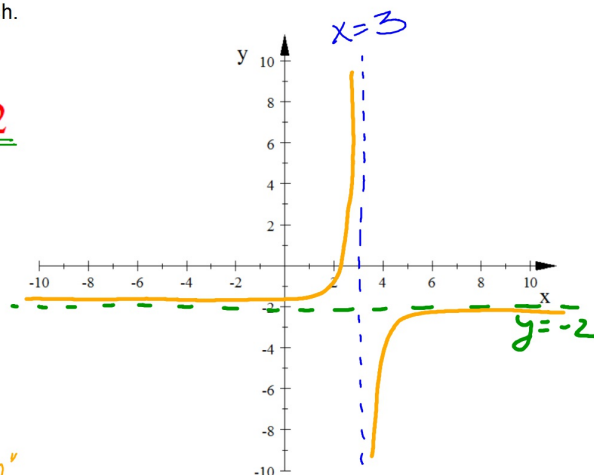
For 3 and 4, sketch the graph of each. Show asymptotes as dashed lines.

3.  $y = \frac{-0.1}{x-3} - 2$

VA  $x = 3$

HA  $y = -2$

Branches in Quad II & IV are close to the "origin"

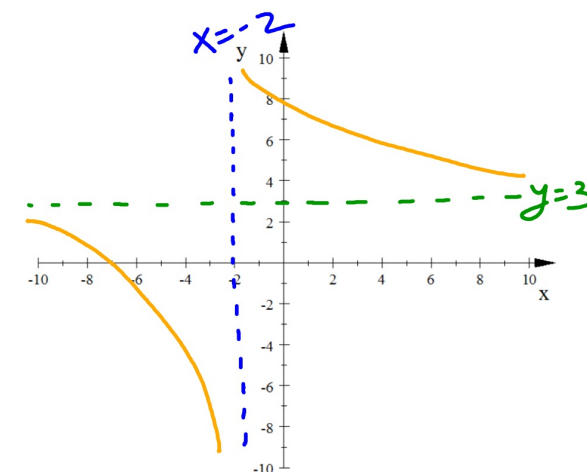


4.  $y = \frac{15}{x+2} + 3$

VA  $x = -2$

HA  $y = 3$

Branches far from "origin" in Quad I & III



Write the equation of each transformation  
of the reciprocal function:

1. 5 units left, twice as tall, branches are in quadrants  
I and III

$$y = \frac{2}{x+5}$$

2. 8 units up, half as tall, branches are in quadrants  
II and IV

$$y = \frac{-0.5}{x} + 8$$

3. 3 units right, 2 units down, branches are in quadrants  
II and IV

$$y = \frac{-1}{x-3} - 2$$

You can now finish Hwk #3

Practice Sheet      Sec 9-2

Graphs of Reciprocal Functions

Due tomorrow.