

Sec 9-5: Adding and Subtracting Rational Expressions

Simplify. $\frac{5}{x^2 + 4x - 21} + \frac{2}{x^2 + 10x + 24}$

$(x+7)(x-3) \quad (x+4)(x+6)$

Instead of multiplying by the denominators in factored form

$$\frac{(x+4)(x+6)}{(x+4)(x+6)} \cdot \frac{5}{x^2 + 4x - 21} + \frac{2}{x^2 + 10x + 24} \cdot \frac{(x+7)(x-3)}{(x+7)(x-3)}$$

It might be easier to just use their expanded form

$$\frac{(x^2 + 10x + 24)}{x^2 + 10x + 24} \cdot \frac{5}{x^2 + 4x - 21} + \frac{2}{x^2 + 10x + 24} \cdot \frac{(x^2 + 4x - 21)}{x^2 + 4x - 21}$$

$$\frac{5x^2 + 50x + 120 + 2x^2 + 8x - 42}{(x^2 + 10x + 24)(x^2 + 4x - 21)}$$

$$= \frac{7x^2 + 58x + 78}{(x^2 + 10x + 24)(x^2 + 4x - 21)}$$

Your denominator could be the for separate factor instead:
 $(x+7)(x-3)(x+4)(x+6)$

Simplify. $\frac{x}{x^2 + 12x + 36} + \frac{4}{x^2 - x - 42}$

$$\frac{x}{x^2 + 12x + 36} + \frac{4}{x^2 - x - 42}$$

$(x+6)(x+6) \quad (x+6)(x-7)$

$$\frac{(x-7)}{(x-7)} \cdot \frac{x}{(x+6)(x+6)} + \frac{4}{(x+6)(x-7)} \cdot \frac{(x+6)}{(x+6)}$$

$$= \frac{x^2 - 7x + 4x + 24}{(x+6)^2(x-7)} = \frac{x^2 - 3x + 24}{(x+6)^2(x-7)}$$

Simplify. $\frac{3}{4x^3 - 16x^2 - 20x} + \frac{7}{6x^2 - 150}$

$$\frac{3}{4x^3 - 16x^2 - 20x} + \frac{7}{6x^2 - 150}$$

$4x(x^2 + 4x - 5) \quad 6(x^2 - 25)$

$$\frac{3(x+5)}{3(x+5)} \cdot \frac{9(x+5)}{4x(x-5)(x+1)} + \frac{7}{6(x+5)(x-5)} \cdot \frac{14x(x+1)}{2x(x+1)}$$

$$= \frac{9x + 45 + 14x^2 + 14x}{12x(x+5)(x+1)}$$

$$= \frac{14x^2 + 23x + 45}{12x(x+5)(x+1)}$$

Simplify. $\frac{8}{x-3} - \frac{4}{x^2 + 2x - 15} + \frac{3}{x+5}$

$$\frac{(x+5)}{(x+5)} \cdot \frac{8}{x-3} - \frac{4}{x^2 + 2x - 15} + \frac{3}{x+5} \cdot \frac{(x-3)}{(x-3)}$$

$(x+5)(x-3)$

$$\frac{8x + 40 - 4 + 3x - 9}{(x+5)(x-3)} = \frac{11x + 27}{(x+5)(x-3)}$$

Hwk #8 Sec 9-5

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Problems 12, 14, 15, 21, 34, 37, 40

You must show work to get credit