

Find all EXACT Complex solutions by factoring or using square roots. You must use each method twice.

1. $16x^2 - 216 = 24x$

2. $12 - 7x^2 + 3 = 71$

3. $9 + 2(2x - 1)^2 = 107$

4. $6x^4 + 18x^2 - 63x = 21x^3$

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1. $16x^2 - 216 = 24x$
 $-24x$ $-24x$ FACTOR

$$16x^2 - 24x - 216 = 0$$

$$8(2x^2 - 3x - 27) = 0$$

$$\begin{array}{r} \begin{array}{cc} -54 & 6 \\ -9 & -3 \end{array} \\ \begin{array}{cc} x & +3 \\ 2x & 2x^2 & +6x \\ -9 & -9x & -27 \end{array} \end{array}$$

$$8(x+3)(2x-9) = 0$$

$$x = -3, 9/2$$

3. $9 + 2(2x-1)^2 = 107$
 -9 -9 SQ ROOTS

$$\frac{2(2x-1)^2}{2} = \frac{98}{2}$$

$$\sqrt{(2x-1)^2} = \sqrt{49}$$

$$2x-1 = \pm 7$$

$$2x-1 = 7$$

$$+1 \quad +1$$

$$\frac{2x = 8}{2}$$

$$2x-1 = -7$$

$$+1 \quad +1$$

$$\frac{2x = -6}{2}$$

$$x = -3, 4$$

2. $12 - 7x^2 + 3 = 71$ SQ ROOTS

$$\begin{array}{cc} -7x^2 + 15 = 71 \\ -15 & -15 \end{array}$$

$$\begin{array}{cc} -7x^2 = 56 \\ -7 & -7 \end{array}$$

$$\sqrt{x^2} = \sqrt{-8} \rightarrow \sqrt{-1 \cdot 4 \cdot 2}$$

$$x = \pm 2i\sqrt{2}$$

4. $6x^4 + 18x^2 - 63x = 21x^3$ FACTOR
 $-21x^3$ $-21x^3$

$$6x^4 - 21x^3 + 18x^2 - 63x = 0$$

$$3x(2x^3 - 7x^2 + 6x - 21) = 0$$

$$\begin{array}{r} \begin{array}{cc} 2x & -7 \\ x^2 & 2x^3 & -7x^2 \\ +3 & +6x & -21 \end{array} \end{array}$$

$$3x(2x-7)(x^2+3) = 0$$

$$3x = 0$$

$$x = 0$$

$$2x-7 = 0$$

$$x = 7/2$$

$$x^2+3 = 0$$

$$-3 \quad -3$$

$$\sqrt{x^2} = \sqrt{-3}$$

$$x = 0, 7/2, \pm i\sqrt{3}$$