

1. Find ALL EXACT COMPLEX solutions.

a) $4x^5 + 52x^3 + 144x = 0$

b) $3(x - 6)^2 + 43 = 7$

Simplify each.

2. $(5 - 3\sqrt{-16}) - (6 + 2\sqrt{-49})$

3. $|4 - 6i|$

1. Find ALL EXACT COMPLEX solutions.

a) $4x^5 + 52x^3 + 144x = 0$

$$4x(x^4 + 13x^2 + 36) = 0$$

$$\begin{array}{c} 36 \\ +9 \quad +4 \\ 13 \end{array}$$

$$4x(x^2 + 9)(x^2 + 4) = 0$$

$$4x = 0$$

$$x^2 + 9 = 0$$

$$x^2 + 4 = 0$$

$$x = 0$$

$$\sqrt{x^2} = \sqrt{-9}$$

$$\sqrt{x^2} = \sqrt{-4}$$

$$x = 0, \pm 3i, \pm 2i$$

b) $3(x-6)^2 + 43 = 7$
 $-43 \quad -43$

$$\frac{3(x-6)^2}{3} = \frac{-36}{3}$$

$$\sqrt{(x-6)^2} = \sqrt{-12} = \sqrt{-1 \cdot 4 \cdot 3}$$

$$x-6 = \pm 2i\sqrt{3}$$

$$x = 6 \pm 2i\sqrt{3}$$

ANSWERS

Simplify each.

2. $(5 - 3\sqrt{-16}) - (6 + 2\sqrt{-49})$

$$= (5 - 3 \cdot 4i) - (6 + 2 \cdot 7i)$$

$$= (5 - 12i) - (6 + 14i)$$

$$= -1 - 26i$$

3. $|4 - 6i| = \sqrt{4^2 + 6^2}$

$$= \sqrt{16 + 36}$$

$$= \sqrt{52}$$

$$= \sqrt{4 \cdot 13}$$

$$= 2\sqrt{13}$$

