

What are the real square roots of 144?

$$\pm 12$$

What are the real square roots of -16?

No Real square roots

There are two real square roots of every positive number.

What does each ask for?

$\pm \sqrt{25}$ both positive and negative square roots of 25

$-\sqrt{36}$ only the negative square root of 36

$\sqrt{49}$ only the positive square root of 49

Simplify. $\sqrt{49} = 7$

When there are two roots of a number the radical symbol $\sqrt{\quad}$ without anything in front means

The Principal Square Root
(the positive square roots)

Solve.

$$x^2 = 225$$

$$\sqrt{x^2} = \sqrt{225}$$

$$x = \pm 15$$

Simplify.

$$\begin{aligned} &\sqrt{48} \\ &= \sqrt{16 \cdot 3} \\ &= 4\sqrt{3} \end{aligned}$$

Solving Quadratic Equations using square roots.

Steps:

- rearrange the equation so that what ever is being squared is by itself. (Isolate the quadratic term)
- Take the square roots of both sides.
- Finish solving for x if necessary.

Which of these equations can you solve using square roots?

1. $2x^2 - 13 = 37$ ✓

You can get $x^2 =$ then square root both sides to get $x =$

2. $x^2 - 3x = 10$ ✗

If you moved the $3x$ to get $x^2 = 3x + 10$ then took the square root of both sides your answer for x would have an x in it!

3. $(x + 2)^2 - 1 = 8$ ✓

You can get $(x+2)^2 =$, square root both sides, then subtract 2 to get $x =$

When can you solve using square roots?

1.

When equation is in Standard Form and $b=0$.

2.

When equation is in Vertex Form.

Find all **REAL EXACT** solutions.

REAL solutions

vs.

Imaginary solutions

$x = \sqrt{7}$ Real Sol.

vs.

$x = \sqrt{-9}$

imaginary Sol.

EXACT solutions

vs.

Approximate solutions

$x = \sqrt{12} = 2\sqrt{3}$ exact

vs.

$x = \sqrt{2} = 1.4142$ approximate

Find all REAL EXACT solutions using square roots.

1. $3x^2 - 13 = 62$

2. $31 + 5x^2 = 11$

3. $2x^2 - 33 = 67$

1. $3x^2 - 13 = 62$

$$+13 \quad +13$$

$$\frac{3x^2}{3} = \frac{75}{3}$$

$$\sqrt{x^2} = \sqrt{25}$$

$$x = \pm 5$$

2. $31 + 5x^2 = 11$

$$-31 \quad -31$$

$$\frac{5x^2}{5} = \frac{-20}{5}$$

$$\sqrt{x^2} = \sqrt{-4}$$

NO Real Solution

3. $2x^2 - 33 = 67$

$$+33 \quad +33$$

$$\frac{2x^2}{2} = \frac{100}{2}$$

$$\sqrt{x^2} = \sqrt{50} = \sqrt{25 \cdot 2}$$

$$x = \pm 5\sqrt{2}$$

Find all REAL EXACT solutions using square roots.

4. $2(x-1)^2 + 3 = 35$ 5. $-3(x-8)^2 + 31 = 10$

6. $6(x+5)^2 - 1 = 71$

4. $2(x-1)^2 + 3 = 35$

$$\begin{array}{r} -3 \quad -3 \\ \frac{2(x-1)^2}{2} = \frac{32}{2} \end{array}$$

$$\sqrt{(x-1)^2} = \sqrt{16}$$

$$\begin{array}{c} x-1 = \pm 4 \\ +1 \end{array} \begin{array}{l} +4+1 \\ -4+1 \end{array}$$

$$x = -3, 5$$

5. $-3(x-8)^2 + 31 = 10$

$$\begin{array}{r} -3/ \quad -3/ \\ \frac{-3(x-8)^2}{-3} = \frac{-21}{-3} \end{array}$$

$$\sqrt{(x-8)^2} = \sqrt{7}$$

$$\begin{array}{c} x-8 = \pm \sqrt{7} \\ +8 \quad +8 \end{array}$$

$$\Rightarrow x = 8 \pm \sqrt{7}$$

6. $6(x+5)^2 - 1 = 71$

$$\begin{array}{r} +1 \quad +1 \\ \frac{6(x+5)^2}{6} = \frac{72}{6} \end{array}$$

$$\sqrt{(x+5)^2} = \sqrt{12}$$

$$\begin{array}{c} x+5 = \pm \sqrt{12} = \pm \sqrt{4 \cdot 3} = \pm 2\sqrt{3} \\ -5 \quad -5 \end{array}$$

$$x = -5 \pm 2\sqrt{3}$$

If you are to solve quadratic equations using these methods:

- Factoring
- Square Roots

Which method should you try first?

Look to use Square Roots first because:
you can only solve using square roots if
Equation is in Standard Form and $b=0$
or
Equation is in Vertex Form

You are now ready to finish Hwk #14.

Practice Sheet

Sec 5-5

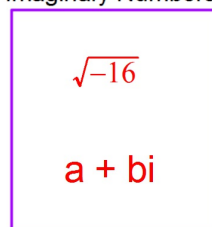
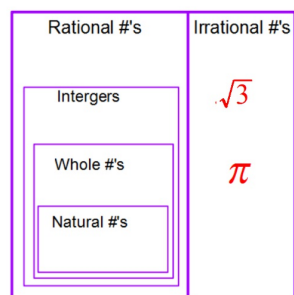
Solve quadratics using square roots and factoring.

Sec 5-6

Complex Numbers

Real Numbers

Imaginary Numbers



Find all Real Solutions.

1. $x^2 - 11 = 14$
 $+11 \quad +11$
 $\sqrt{x^2} = \sqrt{25}$
 $x = \pm 5$

2. $x^2 + 53 = 17$
 $-53 \quad -53$
 $\sqrt{x^2} = \sqrt{-36}$
NO Real Solution

Imaginary Numbers:

$$\sqrt{-1} = i$$

i is called the imaginary unit.

Simplify each.

1. $\sqrt{20}$
 $= \sqrt{4 \cdot 5}$
 $= 2\sqrt{5}$

2. $\sqrt{-16}$
 $= \sqrt{-1 \cdot 16}$
 $= 4i$

Find ALL solutions.

$$7x^2 + 104 = 41$$

$$\begin{array}{r} -104 \quad -104 \\ \hline \end{array}$$

$$\frac{7x^2}{7} = \frac{-63}{7}$$

$$\sqrt{x^2} = \sqrt{-9}$$

$$x = \pm 3i$$