

Graphs of Quadratic Equations:

Vertex Form: $y = a(x - h)^2 + k$

The graph of this equation is:

- a Parabola
- Vertex at (h,k)
- Opens up if $a > 0$
- Opens down if $a < 0$
- a is the Vertical Stretch/Shrink Factor

There is **NO** slope for Parabolas!

$|a| > 1$
 $0 < |a| < 1$

Describe all the transformations of $y = x^2$ each equation represents.

$$y = -\frac{1}{3}(x - 8)^2 + 1$$

- opens down
 - $\frac{1}{3}$ as tall
 - 8 RT
 - 1 up
- } Vertex (8, 1)

Write the equation of this transformation of $y = x^2$.

Translated 9 units up, 3 units right, four times taller,
opens down.

$$y = -4(x - 3)^2 + 9$$

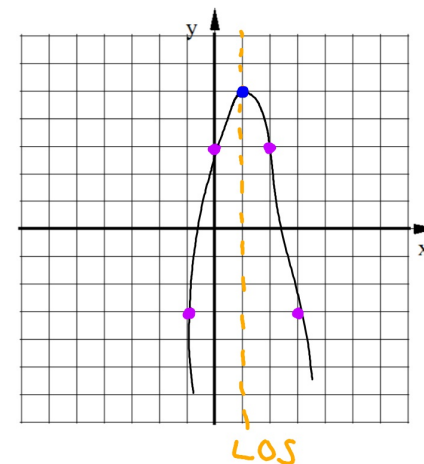
Graph with at least 5 points.

$$y = -2(x - 1)^2 + 5$$

Vertical Vertex (1, 5)
Stretch factor $\frac{1}{2}$ opens down

Parent 1st PT $(1, -2)$ this graph

Parent 2nd PT $(4, -2)$ this graph



Graph with at least 5 points.

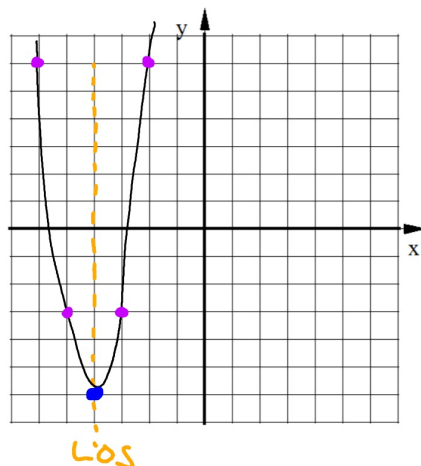
$y = 3(x+4)^2 - 6$
 4 left 6 down
 Vert stretch factor
 Vertex $(-4, -6)$

Parent 1st PT this graph

$\downarrow 1 \times 3 \rightarrow \downarrow 3$

Parent 2nd PT this graph

$\downarrow 4 \times 3 \rightarrow \downarrow 12$



Write the equation of this graph.

1st method:

- Use vertex to fill in h and k

Vertex $(1, 8)$

$y = a(x-h)^2 + k$
 $y = a(x-1)^2 + 8$

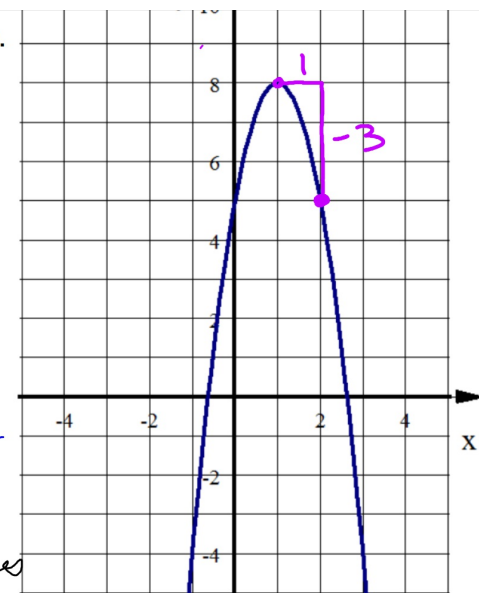
- Use the 1st "good" pt to find a .

this graph parent func

$\downarrow -3$ $\downarrow 8$

this graph is 3 times taller & opens down

$a = -3$



EQ: $y = -3(x-1)^2 + 8$

Write the equation of this graph.

2nd method:

- Use vertex to fill in h and k

$y = a(x-h)^2 + k$
 $y = a(x-1)^2 + 8$

- After using the Vertex, find any other point on the parabola and replace x and y with those coordinates. Then solve for a

The point $(0, 5)$ is on the graph. Replace x with 0 and y with 5. Then solve for a .

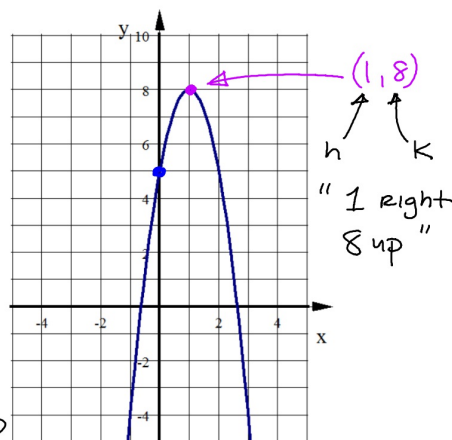
$5 = a(0-1)^2 + 8$

$5 = a(-1)^2 + 8$

$5 = a + 8$

$a = -3$

EQ: $y = -3(x-1)^2 + 8$



Write the equation of this graph.

The vertex is $(-3, -1)$

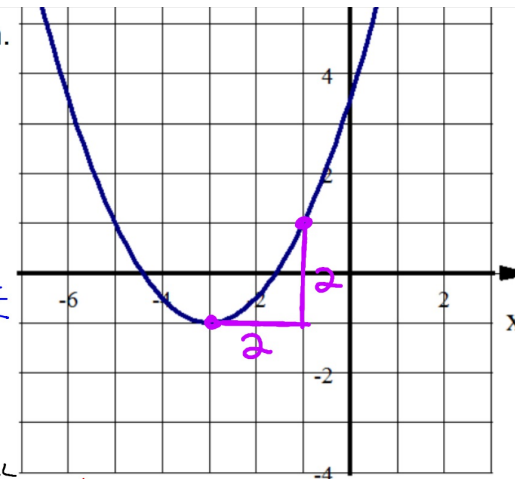
$y = a(x-h)^2 + k$
 $y = a(x+3)^2 - 1$

THIS GRAPH Parent Func

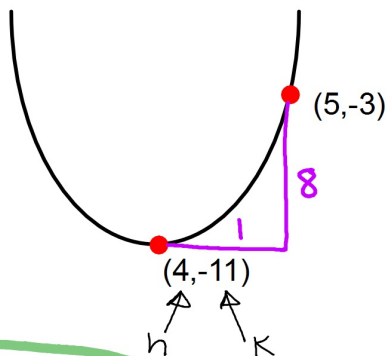
$\downarrow 2$ $\downarrow 4$

THIS GRAPH IS HALF AS TALL
Therefore $a = 1/2$


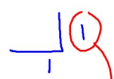
EQ: $y = 1/2(x+3)^2 - 1$



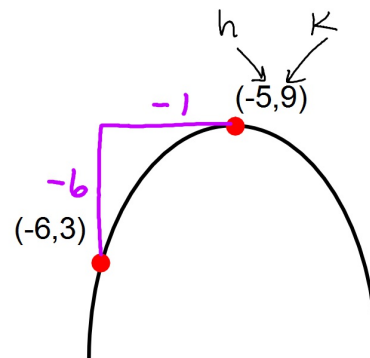
Write the equation of this graph.



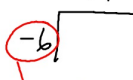

EQ: $y = 8(x-4)^2 - 11$

This graph

 parent func

 this graph is
 8 times taller,
 $a=8$

Write the equation of this graph.



EQ: $y = -6(x+5)^2 + 9$

This graph

 parent func


This graph is
 6 times taller but
 opens down.
 $a=-6$