

Given these functions:

$$g(x) = 3x - 2$$

$$h(x) = 2x + 1$$

Find  $h(g(h(5)))$ .

1st  $h(5) = 2(5) + 1 = 11$

$h(g(h(5)))$  is now  $h(g(11))$

2nd  $g(11) = 3(11) - 2 = 31$

$h(g(11))$  is now  $h(31)$

3rd  $h(31) = 2(31) + 1 = 63$

$$h(g(h(5))) = 63$$

Given these functions:

$$g(x) = 3x - 2$$

$$h(x) = 2x + 1$$

Find  $g(h(g(x)))$ .

1st  $h(g(x)) = 2(3x - 2) + 1 = 6x - 4 + 1 = 6x - 3$

$g(h(g(x)))$  is now  $g(6x - 3)$

$$\begin{aligned} g(6x - 3) &= 3(6x - 3) - 2 \\ &= 18x - 9 - 2 = 18x - 11 \end{aligned}$$

$$g(h(g(x))) = 18x - 11$$

Another way to write a composite is:

$$f(g(x)) \rightarrow (f \circ g)(x)$$

Use these two functions:

$$f(x) = x + 5 \quad g(x) = 3x - 2$$

1. Find  $g(f(-1))$

1st:  $f(-1) = -1 + 5 = 4$

$g(f(-1))$  is now  $g(4)$

2nd:  $g(4) = 3(4) - 2 = 10$

$$g(f(-1)) = 10$$

Use these two functions:

$$f(x) = x + 5$$

$$g(x) = 3x - 2$$

2. Find  $(g \circ f)(5) \Rightarrow g(f(5))$

1st  $f(5) = (5) + 5 = 10$

$(g \circ f)(5) = g(f(5))$  which is now  $g(10)$

2nd  $g(10) = 3(10) - 2 = 30 - 2 = 28$

$$(g \circ f)(5) = 28$$

Use these two functions:

$$f(x) = x + 4 \quad g(x) = 3x^2 - 2x + 5$$

1. Find  $f(g(x))$

$$\begin{aligned} & (3x^2 - 2x + 5) + 4 \\ &= \boxed{3x^2 - 2x + 9} \end{aligned}$$

Use these two functions:

$$f(x) = x + 4 \quad g(x) = 3x^2 - 2x + 5$$

2. Find  $(g \circ f)(x) = g(f(x))$

$$\begin{aligned} &= 3(\boxed{x+4})^2 - 2(x+4) + 5 \\ &= 3(x^2 + 8x + 16) - 2(x+4) + 5 \\ &= \underline{3x^2} + \underline{24x} + \underline{48} - \underline{2x} - \underline{8} + \underline{5} \end{aligned}$$

$$\boxed{3x^2 + 22x + 45}$$

$$\begin{aligned} & (x+4)^2 = (x+4)(x+4) \\ &= \begin{array}{cc} x & +4 \\ x^2 & +4x \\ +4 & +16 \end{array} \\ &= x^2 + 8x + 16 \end{aligned}$$

Use these two functions:  $f(x) = 2x + 1$   $g(x) = \frac{5x}{6x-8}$

1. Find  $f(g(x))$ . Simplify.

$$\begin{aligned} &= 2\left(\frac{5x}{6x-8}\right) + 1 \\ &= \frac{10x}{6x-8} + 1 = \frac{5x}{3x-4} + 1 \\ &= \frac{5x}{3x-4} + \frac{3x-4}{3x-4} \\ &= \boxed{\frac{8x-4}{3x-4}} \end{aligned}$$

Use these two functions:  $f(x) = 2x + 1$   $g(x) = \frac{5x}{6x-8}$

2. Find  $g(f(x))$ . Simplify.

$$\begin{aligned} & \frac{5(2x+1)}{6(2x+1)-8} = \frac{10x+5}{12x+6-8} \\ &= \boxed{\frac{10x+5}{12x-2}} \end{aligned}$$