

Section 13-8: The Reciprocal Trig Functions

Cotangent: $\text{Cot}\theta = \frac{1}{\tan\theta} = \frac{1}{\frac{y}{x}} = \frac{x}{y} = \frac{\cos\theta}{\sin\theta}$

Secant: $\sec\theta = \frac{1}{\cos\theta} = \frac{1}{x}$

Cosecant: $\csc\theta = \frac{1}{\sin\theta} = \frac{1}{y}$

Use your calculator to find the value of each to the nearest hundredth.

$$\cos(131^\circ) = -0.66$$

$$\tan \frac{8\pi}{27} = 1.34$$

$$\csc(-75^\circ) = -1.04$$

$$= \frac{1}{\sin(-75^\circ)}$$

$$\sec 14^\circ = 7.31$$

radians (no degree symbol)

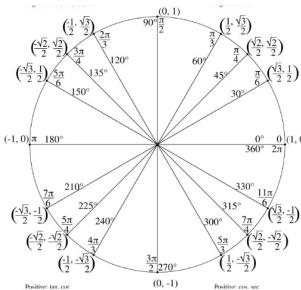
$$= \frac{1}{\cos 14^\circ}$$

$$\cot \frac{-4\pi}{13} = -0.69$$

$$= \frac{1}{\tan \frac{-4\pi}{13}}$$

Use the Unit Circle to find the EXACT value of each.

$$1. \sec 60^\circ = \frac{1}{\cos 60^\circ} = \frac{1}{\frac{1}{2}} = 2$$



$$2. \csc \frac{7\pi}{4}$$

$$= \frac{1}{\sin \frac{7\pi}{4}} = \frac{1}{-\frac{\sqrt{2}}{2}} = -\frac{2}{\sqrt{2}} \cdot \frac{\sqrt{2}}{\sqrt{2}} = -\frac{2\sqrt{2}}{2} = -\sqrt{2}$$

$$3. \cot 16\pi$$

$$= \frac{1}{\tan 16\pi} = \frac{1}{\frac{0}{1}} = \frac{1}{0} = \text{undefined}$$

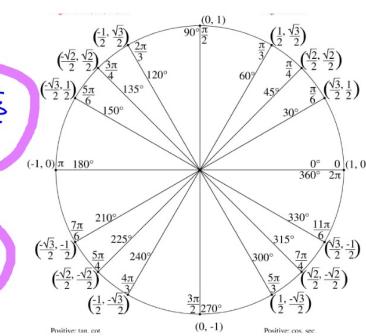
Use the Unit Circle to find the EXACT value of each.

$$4. \sec \left(-\frac{17\pi}{6}\right)$$

$$= \frac{1}{\cos \frac{17\pi}{6}} = \frac{1}{-\frac{\sqrt{3}}{2}} = -\frac{2}{\sqrt{3}} = -\frac{2\sqrt{3}}{3}$$

$$5. \csc 1620^\circ$$

$$\frac{1}{\sin 1620^\circ} = \frac{1}{0} = \text{undefined}$$



$$6. \cot \frac{29\pi}{3}$$

$$\frac{1}{\tan \frac{29\pi}{3}} = \frac{1}{-\frac{\sqrt{3}}{2}} = \frac{1}{-\frac{\sqrt{3}}{2}} = -\frac{1}{\sqrt{3}} = -\frac{\sqrt{3}}{3}$$

Given that $\cos x = \frac{11}{61}$ ADJ
HYP

Evaluate the other five trig functions. Rationalize all denominators as needed and simplify fractions.

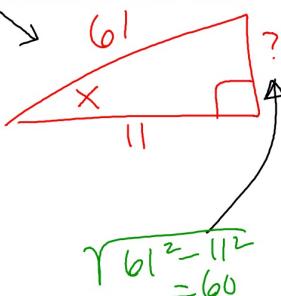
$$\sin x = \frac{60}{61}$$

$$\tan x = \frac{60}{11}$$

$$\csc x = \frac{61}{60}$$

$$\sec x = \frac{61}{11}$$

$$\cot x = \frac{11}{60}$$



Given that $\csc x = \frac{7}{5}$

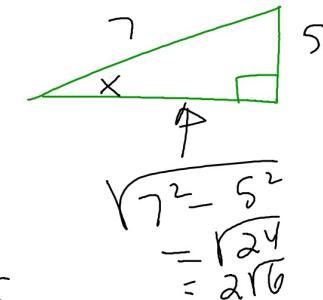
Evaluate the other five trig functions. Rationalize all denominators as needed and simplify fractions.

$$\sin x = \frac{5}{7}$$

$$\cos x = \frac{2\sqrt{6}}{7}$$

$$\begin{aligned}\tan x &= \frac{5}{2\sqrt{6}} \cdot \frac{\sqrt{6}}{\sqrt{6}} \\ &= \frac{5\sqrt{6}}{12}\end{aligned}$$

$$\cot x = \frac{2\sqrt{6}}{5}$$



You can now finish Hwk #22 Sec 13-8

Page 766 Problems 2-4, 9-14

AND

Page 797 Problems 28, 30