

Find exact solutions.

$$4\sin^2\theta - 1 = 2$$

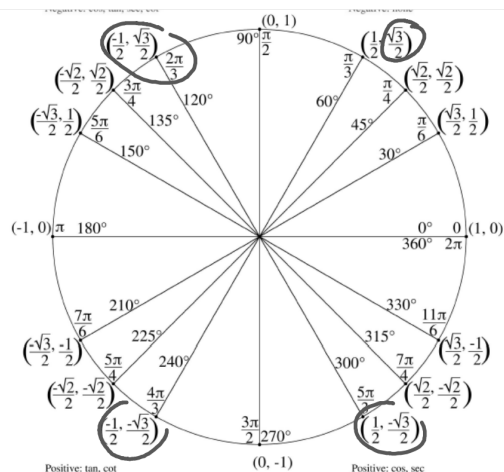
+1   +1

$$\frac{4\sin^2\theta}{4} = \frac{3}{4}$$

$$\sqrt{\sin^2\theta} = \sqrt{\frac{3}{4}}$$

$$\sin\theta = \pm \frac{\sqrt{3}}{2}$$

$$\theta = 60^\circ, 120^\circ, 240^\circ, 300^\circ$$



Using the unit circle find two angles that have the same Sine value.

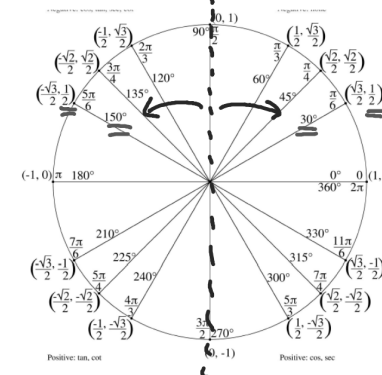
What is the relationship between these two angles?

- They are reflections over the y-axis

- They are Supplementary:

$$\sin\theta = \sin(180^\circ - \theta)$$

$$\sin(\pi - \theta)$$



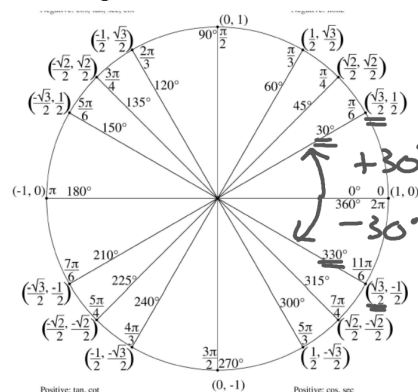
Using the unit circle find two angles that have the same Cosine value.

What is the relationship between these two angles?

- They are reflections over the x-axis

- They are opposites of each other

$$\cos\theta = \cos(-\theta)$$

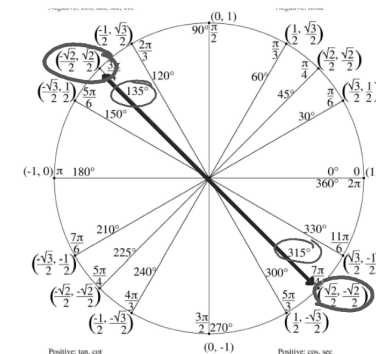


Using the unit circle find two angles that have the same Tangent value.

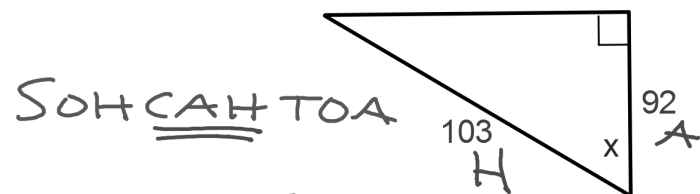
What is the relationship between these two angles?

- The angles are half a circle away from each other

- $\tan\theta = \tan(\theta \pm 180^\circ) = \tan(\theta \pm \pi)$



Find the value of  $x$  to the nearest tenth of a degree.



$$\cos X = \frac{92}{103}$$

$$X = \cos^{-1}\left(\frac{92}{103}\right) = 26.7^\circ$$

Find all values of  $\theta$  for  $0 \leq \theta \leq 360^\circ$  that makes this equation true. Round to the nearest hundredth.

$$5 \tan \theta - 6 = 1$$

$$\frac{5 \tan \theta}{5} = \frac{7}{5}$$

$$\tan \theta = 1.4$$

$$\theta = \tan^{-1}(1.4)$$

$$\theta = 54.46^\circ$$

$$\hat{\epsilon} \quad \theta + 180$$

$$54.46 + 180$$

$$234.46^\circ$$

Find all values of  $\theta$  for  $0 \leq \theta \leq 360^\circ$  that makes this equation true. Round to the nearest hundredth.

$$10 \sin \theta + 2 = 6$$

$$\frac{10 \sin \theta}{10} = \frac{4}{10}$$

$$\sin \theta = .4$$

$$\theta = \sin^{-1}(.4) = 23.58^\circ$$

$$\hat{\epsilon} \quad 180 - \theta$$

$$180 - 23.58$$

$$156.42^\circ$$

Find all values of  $\theta$  for  $0 \leq \theta \leq 360^\circ$  that makes this equation true. Round to the nearest hundredth.

$$8 \cos \theta + 4 = 3$$

$$\frac{8 \cos \theta}{8} = \frac{-1}{8}$$

$$\cos \theta = -1/8$$

$$\theta = \cos^{-1}(-1/8) = 97.18^\circ$$

$$\hat{\epsilon} \quad -\theta$$

$$\downarrow$$
  

$$-97.18^\circ$$

$$+ 360$$

$$262.82^\circ$$

Find all values of  $\theta$  for  $0 \leq \theta \leq 2\pi$  that makes this equation true. Round to the nearest hundredth.

$$\begin{aligned}
 8\sin\theta + 5 &= 3 \\
 -5 &\quad -5 \\
 \hline
 8\sin\theta &= -2 \\
 8 &\quad 8 \\
 \hline
 \sin\theta &= -.25
 \end{aligned}$$

$$\begin{aligned}
 \rightarrow \sin^{-1}(-.25) &= -.25 \\
 &\quad + 2\pi \\
 &\quad \hline
 &\quad 6.03
 \end{aligned}$$

$$\begin{aligned}
 \therefore \pi - \theta \\
 = \pi - .25 \\
 = 3.39
 \end{aligned}$$

Find all values of  $\theta$  for  $0 \leq \theta \leq 2\pi$  that makes this equation true. Round to the nearest hundredth.

$$\begin{aligned}
 -2\cos\theta - 1.5 &= .25 \\
 +1.5 &\quad +1.5 \\
 \hline
 -2\cos\theta &= 1.75 \\
 -2 &\quad -2 \\
 \hline
 \cos\theta &= -.875
 \end{aligned}$$

$$\begin{aligned}
 \rightarrow \theta &= \cos^{-1}(-.875) \\
 &= 2.64 \\
 \therefore -\theta \\
 &\quad \downarrow \\
 &\quad -2.64 \\
 &\quad + 2\pi \\
 &\quad \hline
 &\quad 3.65
 \end{aligned}$$

Find all values of  $\theta$  for  $0 \leq \theta \leq 2\pi$  that makes this equation true. Round to the nearest hundredth.

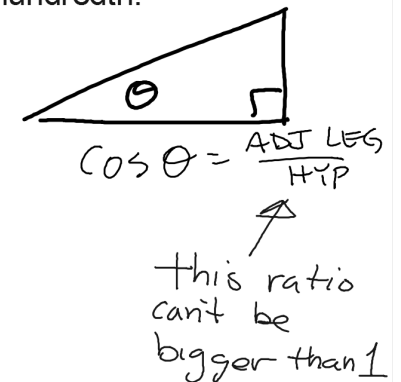
$$\begin{aligned}
 10\tan\theta + 13 &= 52 \\
 -13 &\quad -13 \\
 \hline
 10\tan\theta &= 39 \\
 10 &\quad 10 \\
 \hline
 \tan\theta &= 3.9
 \end{aligned}$$

$$\begin{aligned}
 \rightarrow \theta &= \tan^{-1}(3.9) = 1.32 \\
 \therefore \theta + \pi \\
 &= 1.32 + \pi \\
 &= 4.46
 \end{aligned}$$

Find all values of  $\theta$  for  $0 \leq \theta \leq 2\pi$  that makes this equation true. Round to the nearest hundredth.

$$\begin{aligned}
 3\cos\theta + 2 &= 11 \\
 -2 &\quad -2 \\
 \hline
 3\cos\theta &= 9 \\
 3 &\quad 3 \\
 \hline
 \cos\theta &= 3
 \end{aligned}$$

$$\begin{aligned}
 \cos\theta &= 3 \\
 \text{NO SOL}
 \end{aligned}$$



You can now finish Hwk #27

Sec 14-2

Page 787

Due tomorrow

Problems:

17-19, 22, 25 Use Unit Circle for exact answers.

20, 21, 23 Round to nearest hundredth.