

Simplify each trigonometric expression into a single trigonometric function or constant.

1. $\csc x(1 - \cos^2 x)$

2. $(\sec^2 y)(\cot^2 y)(\sin y)$

3. $\cot \theta (\tan \theta + \cot \theta)$

4. $\frac{\sin^2 \theta}{\cos \theta} + \cos \theta$

5. $\frac{\sin \theta \cdot \cos \theta}{\cot \theta}$

6. $\frac{\cot \theta}{\csc \theta - \sin \theta}$

Simplify each trigonometric expression into a single trigonometric function or constant.

1. $\csc x (1 - \cos^2 x)$

$$= \frac{1}{\sin} (\sin^2)$$

$$= \boxed{\sin x}$$

2. $(\sec^2 y)(\cot^2 y)(\sin y)$

$$= \left(\frac{1}{\cos^2} \right) \left(\frac{\cos^2}{\sin^2} \right) (\sin)$$

$$= \frac{1}{\sin} = \boxed{\csc y}$$

3. $\cot \theta (\tan \theta + \cot \theta)$

$$\cot \cdot \tan + \cot^2$$

$$= 1 + \cot^2$$

$$= \boxed{\csc^2 \theta}$$

4. $\frac{\sin^2 \theta}{\cos \theta} + \cos \theta \cdot \frac{\cos}{\cos}$

$$= \frac{\sin^2}{\cos} + \frac{\cos^2}{\cos}$$

$$= \frac{\sin^2 + \cos^2}{\cos}$$

$$= \frac{1}{\cos} = \boxed{\sec \theta}$$

5. $\frac{\sin \theta \cdot \cos \theta}{\cot \theta}$

$$= \frac{\sin \cdot \cos}{\frac{\cos}{\sin}}$$

$$= \sin \cdot \cos \cdot \frac{\sin}{\cos}$$

$$= \boxed{\sin^2 \theta}$$

6. $\frac{\cot \theta}{\csc \theta - \sin \theta}$

$$= \frac{\frac{\cos}{\sin}}{\frac{1}{\sin} - \sin \cdot \frac{\sin}{\sin}}$$

$$= \frac{\frac{\cos}{\sin}}{\frac{1}{\sin} - \frac{\sin^2}{\sin}}$$

$$= \frac{\frac{\cos}{\sin}}{\frac{1 - \sin^2}{\sin}} = \frac{\frac{\cos}{\sin}}{\frac{\cos^2}{\sin}} = \frac{\cos}{\sin} \cdot \frac{\sin}{\cos^2}$$

$$= \frac{1}{\cos} = \boxed{\sec \theta}$$