Simplify each trigonometric expression.

$$\frac{\sec x - \cos x}{\sec x}$$

$$\frac{\frac{1}{\cos} - \cos}{\frac{1}{\cos}}$$

$$= \left(\frac{1}{\cos} - \cos\right)\cos$$

$$= 1 - \cos^2$$

$$= \sin^2 x$$

$$\frac{\sin x}{1 - \cos^2 x}$$

$$= \frac{\sin}{\sin^2}$$

$$= \frac{1}{\sin} = \csc x$$

$$\cos x(1 + \tan^2 x)$$

$$= \cos(\sec^2)$$

$$= \cos \frac{1}{\cos^2}$$

$$= \frac{1}{\cos} = \sec x$$

$$\frac{\sin^2 x}{\cos x \cdot \tan x}$$

$$\frac{\sin^2}{\frac{\cos}{1} \cdot \frac{\sin}{\cos}} = \frac{\sin^2}{\sin} = \sin$$

You can now finish Hwk #24: Sec 14-1

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Problems: 18, 20-23, 28, 30, 32-34

No work = No credit

$$\frac{\sec x}{\cos x} - \frac{\tan x}{\cot x}$$

$$= \frac{\frac{1}{\cos}}{\cos} - \frac{\frac{\sin}{\cos}}{\frac{\cos}{\sin}}$$

$$= \frac{1}{\cos}\cdot\frac{1}{\cos} - \frac{\sin}{\cos}\cdot\frac{\sin}{\cos}$$

$$= \frac{1}{\cos^2} - \frac{\sin^2}{\cos^2}$$

$$= \frac{1-\sin^2}{\cos^2}$$

$$= \frac{\cos^2}{\cos^2} = 1$$

$$\frac{\sec\theta}{\cot\theta + \tan\theta}$$

$$\frac{\frac{1}{\cos}}{\frac{\cos}{\cos}\cdot\frac{\cos}{\sin} + \frac{\sin}{\cos}\cdot\frac{\sin}{\sin}} = \frac{\frac{1}{\cos}}{\frac{\cos^2+\sin^2}{\sin\cdot\cos}}$$

$$= \frac{\frac{1}{\cos}}{\frac{1}{\sin\cos}}$$

$$= \frac{1}{\cos}\cdot\frac{\sin\cdot\cos}{1}$$

$$= \sin x$$

this factors using difference of perfect squares

$$\frac{\sin^4(x) - \cos^4(x)}{\sin^2(x) - \cos^2(x)} = \frac{(\sin^2+\cos^2)(\sin^2-\cos^2)}{\sin^2-\cos^2}$$

$$= \sin^2 + \cos^2$$

$$= 1$$

You can now finish Hwk #25:

Practice Sheet: Sec 14-1

Simplifying Trigonometric Expressions

## Verifying trig identities:

Showing that the two sides of the equation really are equal.

Two basic techniques:

- Work on one side only and make it look like the other side.

or

- Work on both sides until they look the same.

When trying to verify/prove an identity you CAN'T do the following:

- Move terms from one side of the equation to the other side
- Multiply/divide/square/square root both sides of the equation
- Add/Subtract from both sides of the equation

You are NOT solving

You are trying to show the two sides of the equation are equal which means you don't know they are equal....YET.

Verify this identity:

$1 + \cot A = \csc A(\sin A + \cos A)$