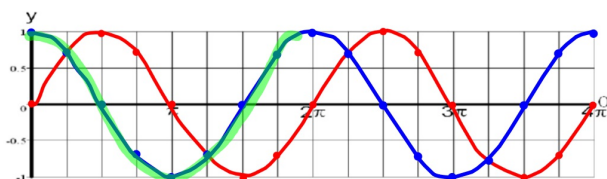


2. Fill out the table for Cos (round decimals to the nearest hundredth) and plot.

θ	0	$\frac{\pi}{4}$	$\frac{\pi}{2}$	$\frac{3\pi}{4}$	π	$\frac{5\pi}{4}$	$\frac{3\pi}{2}$	$\frac{7\pi}{4}$	2π	$\frac{9\pi}{4}$	$\frac{5\pi}{2}$	$\frac{11\pi}{4}$	3π	$\frac{13\pi}{4}$	$\frac{7\pi}{2}$	$\frac{15\pi}{4}$	4π
$\cos \theta$	1	0.71	0	-0.71	-1	-0.71	0	0.71	1	0.71	0	-0.71	-1	-0.71	0	0.71	1



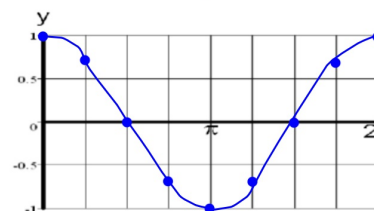
$$y = \cos \theta$$

Period = 2π Amplitude = 1 Eq Midline: $y = 0$

These are all the same as for $y = \sin x$!

One cycle of the parent Sine function looks like a sideways "S".

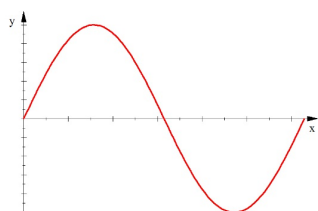
What does one period of the parent Cosine function look like?



The "first" period of a Cosine looks like a "U"-shape or similar to a parabola.

Where does Cosine "start"? Cosine "starts" at a **MAXIMUM**.

The Parent Function: $y = \sin x$

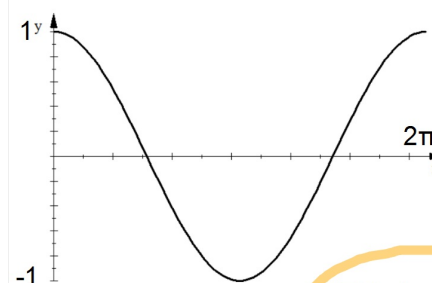


Period = 2π

Amplitude = 1

Eq of Midline: $y = 0$

The Parent Function: $y = \cos x$

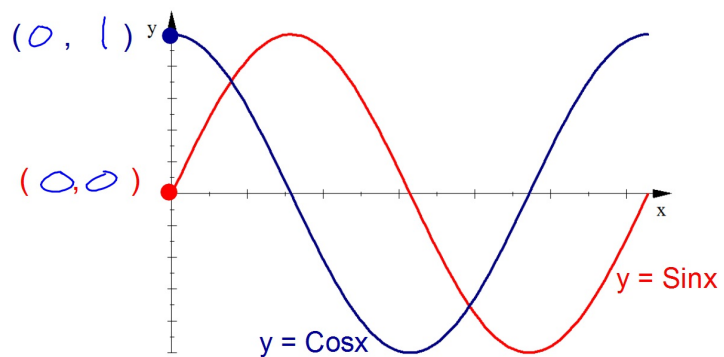


Period = 2π

Amplitude = 1

Eq of Midline: $y = 0$

This is all the SAME as Sine!!!



How are the graphs of $\text{Cos}x$ and $\text{Sin}x$ the **SAME**?

They have the same **Period, Amplitude, and Midline**.

Both "start" on the y-axis ($x=0$)

How are the graphs of $\text{Cos}x$ and $\text{Sin}x$ **DIFFERENT**?

Where they start.

Starting points and direction for the Parent Functions.

$y = \text{Sin}x$

Starts on the midline then goes up.

$y = \text{Cos}x$

Starts at a maximum.

Starting points for

$y = a\text{Sin}/\text{Cos}x$

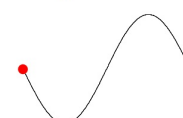
Sine Graphs

Positive a



Starts
on the Midline
and goes UP

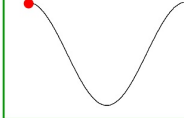
Negative a



Starts
on the Midline
and goes
DOWN

Cosine Graphs

Positive a

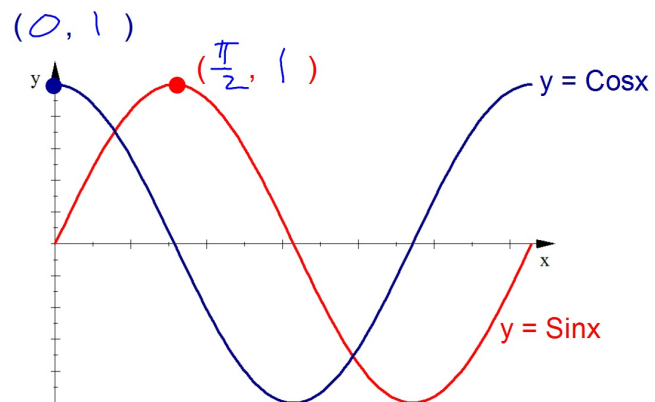


Starts
at a Max

Negative a



Starts
at a Min



ALSO

How else is the graph of $\cos x$ related to the graph of $\sin x$?

They are horizontal translations of each other.

To get the $\sin x$ you translate $\cos x$ 90° to the right
 $\sin x = \cos(x - 90^\circ)$

To get the $\cos x$ you translate $\sin x$ 90° to the left
 $\cos x = \sin(x + 90^\circ)$

$$y = a \sin bx$$

a = Amplitude (vertical Stretch or Shrink factor)

$a < 0$ is an x-axis reflection (upside down)

$$\text{Period} = \frac{2\pi}{b} \quad \longrightarrow \quad b = \frac{2\pi}{\text{Period}}$$

$$y = a \cos bx$$

a = Amplitude (vertical Stretch or Shrink factor)

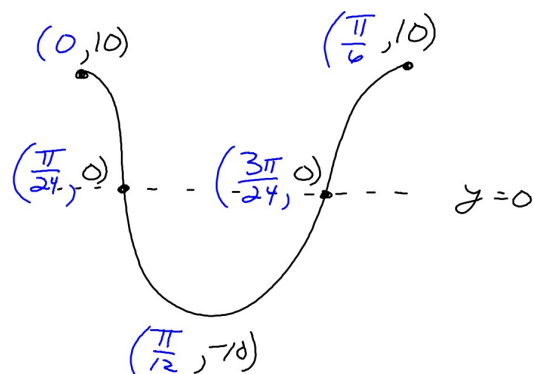
$a < 0$ is an x-axis reflection (upside down)

$$\text{Period} = \frac{2\pi}{b} \quad \longrightarrow \quad b = \frac{2\pi}{\text{Period}}$$

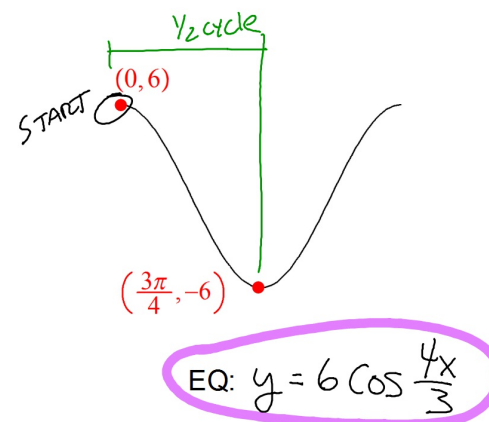
This is all the same as Sine!!!

Graph one period of this Cosine Function. Label the coordinates of all maximums, minimums, and pts on the midline.

$y = 10 \cos 12x$
 amplitude = 10
 period = $\frac{2\pi}{12} = \frac{\pi}{6}$
 midline: $y = 0$
 STARTS AT A max

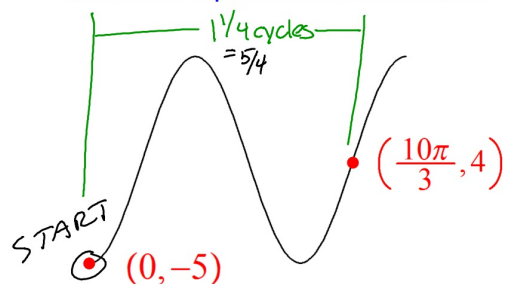


Write the equation of this Cosine Function.



midline: $y = \frac{6 + -6}{2} = 0$
 $k = 0$
 Amplitude = 6
 $a = 6$
 period = $\frac{3\pi}{4} \cdot \frac{2}{1/2} = \frac{3\pi}{2}$
 $b = \frac{2\pi}{\frac{3\pi}{2}} = 2\pi \cdot \frac{2}{3\pi}$
 $b = \frac{4}{3}$

Write the equation of this Cosine Function.



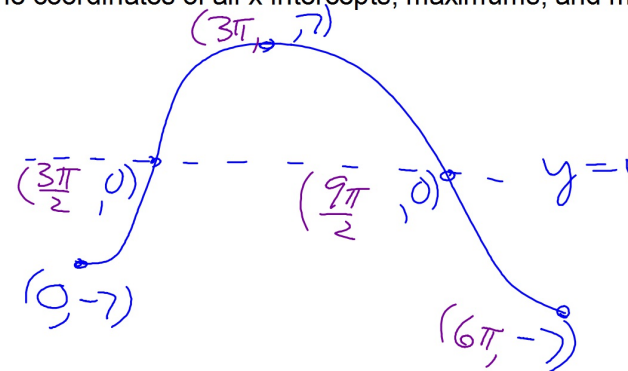
midline: $y = 4$
 $k = 4$
 Amplitude = $4 - -5 = 9$
 $a = -9$
 period = $\frac{10\pi}{\frac{3}{5/4}} = \frac{10\pi \cdot 4}{3 \cdot 5} = \frac{8\pi}{3}$
 $b = \frac{2\pi}{\frac{8\pi}{3}} = 2\pi \cdot \frac{3}{8\pi}$
 $b = \frac{3}{4}$

$b = \frac{2\pi}{\frac{8\pi}{3}} = 2\pi \cdot \frac{3}{8\pi} = \frac{3}{4}$

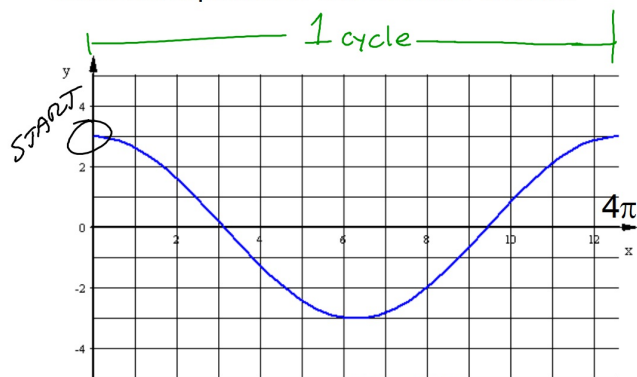
Graph one period of: $y = -7 \cos \left(\frac{x}{3}\right)$

period = $\frac{2\pi}{1/3} = 6\pi$

Label the coordinates of all x-intercepts, maximums, and minimums.



Write the equation of this Cosine Function.



midline: $y=0$

$k=0$

Amp = 3

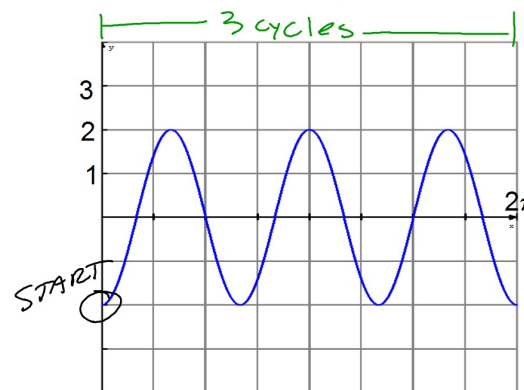
$a=3$

period = 4π

$b = \frac{2\pi}{4\pi} = \frac{1}{2}$

$y = 3\cos(x/2)$

Write the equation of this Cosine Function.



midline: $y=0$

$k=0$

Amplitude = 2

$a=-2$

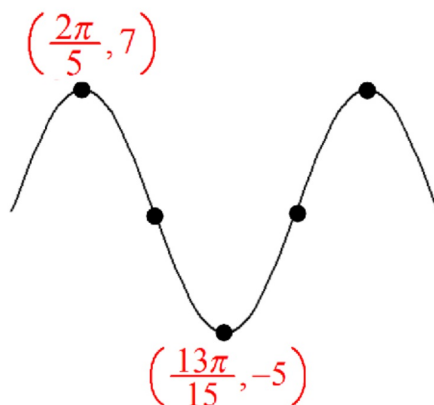
period = $\frac{2\pi}{3}$

$b = \frac{2\pi}{\frac{2\pi}{3}} = 2\pi \cdot \frac{3}{2\pi}$

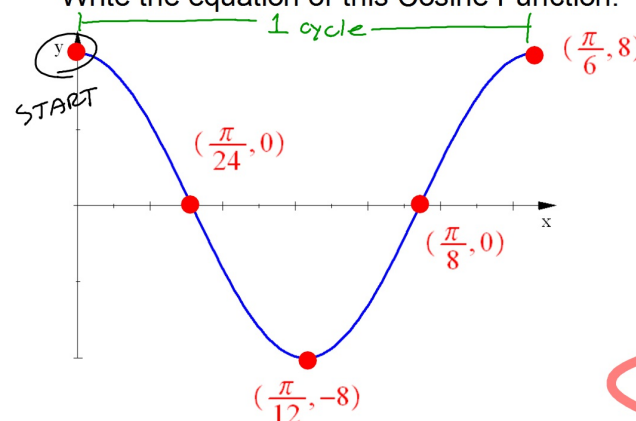
$b=3$

$y = -2\cos(3x)$

1. Fill in the missing coordinates and write the equation of this Cosine Function



Write the equation of this Cosine Function:



midline: $y=0$

$k=0$

amplitude = 8

$a=8$

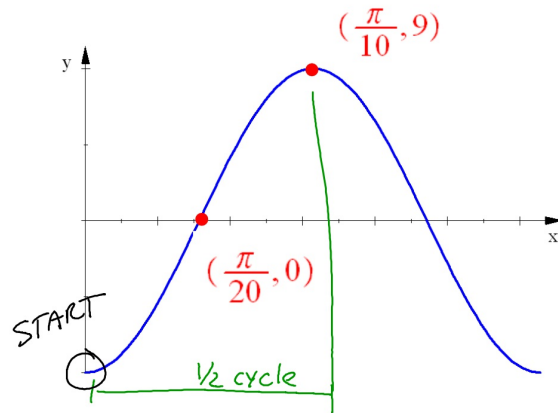
period = $\frac{\pi}{6}$

$b = \frac{2\pi}{\frac{\pi}{6}} = 2\pi \cdot \frac{6}{\pi}$

$b=12$

$y = 8\cos(12x)$

Write the equation of this Cosine Function:



$$\begin{aligned} \text{Amp} &= 9 \\ a &= -9 \\ \text{midline: } y &= 0 \\ k &= 0 \\ \text{period} &= \frac{\pi}{10} \cdot 2 = \frac{\pi}{5} \\ b &= \frac{2\pi}{\frac{\pi}{5}} = 2\pi \cdot \frac{5}{\pi} \\ b &= 10 \end{aligned}$$

$$y = -9\cos 10x$$

You can now do Hwk #10

Sec 13-5

Practice Sheet