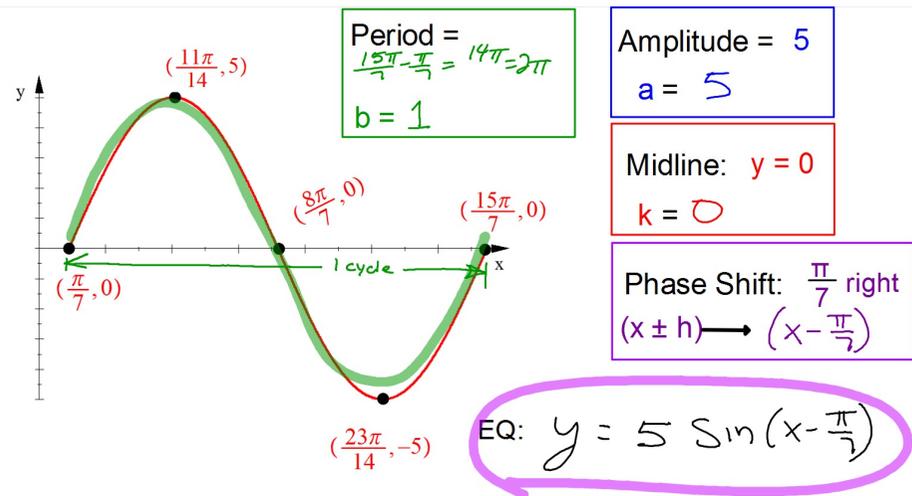


$$y = a\sin(x-h) + k$$

h: Horizontal Shift: Phase Shift

h gives you x-coord of start point.



$$y = \sin bx$$

$$y = \sin(x - h)$$

b affects the period
(horiz stretch or shrink)

h affects the horizontal position.
(horiz translation left or right)

How do you write an equation that has both
a **b** and an **h**?

$$y = \sin(b(x-h))$$

Write the equation of this function.

Parent function: $\sin x$

Phase Shift: $\frac{\pi}{6}$ left

Period = 8π

Graph is upside-down

$$b = \frac{2\pi}{8\pi} = \frac{1}{4}$$

Midline: $y = -3$

Amplitude = 10

$$y = -10 \sin\left(\frac{1}{4}\left(x + \frac{\pi}{6}\right)\right) - 3$$

$$y = -12 \sin\left(3\left(x + \frac{7\pi}{10}\right)\right)$$

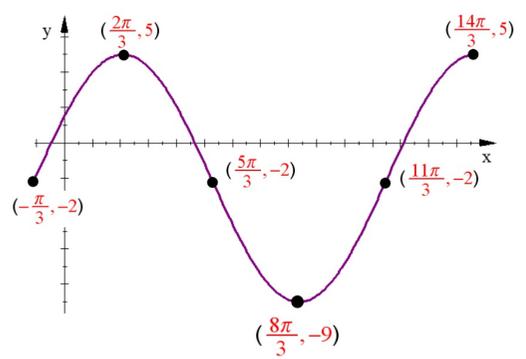
Period = $\frac{2\pi}{3}$ Amplitude = 12

Phase Shift: $\frac{7\pi}{10}$ Left Eq of Midline: $y = 0$

$$y = a \sin(b(x \pm h)) \pm k$$

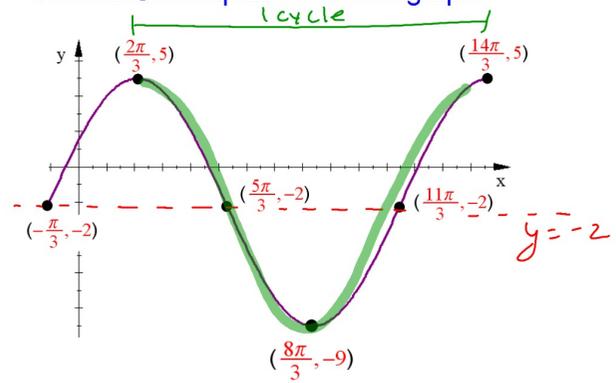
- a → Vert stretch or shrink - Amplitude
Also x-axis reflection if negative
- b → Horiz stretch or shrink Period = $2\pi/b$ and $b = 2\pi/\text{Period}$
- h → Phase Shift - Horiz translation - the x-coord of start point
- k → Vertical translation - Equation of the Midline
gives you y-coord of start pt (and pts on midline)

Write a Sine equation for this graph.



EQ:

Write a Sine equation for this graph.



EQ: $y = 7 \sin\left(\frac{1}{2}\left(x + \frac{\pi}{3}\right)\right) - 2$

Amplitude = $5 - (-2) = 7$
 $a = 7$ if START AT $(-\pi/3, -2)$
 Eq of Midline: $y = -2$
 $k = -2$
 Phase Shift: $\frac{\pi}{3}$ Left
 if start at $(-\pi/3, -2)$
 Period = $\frac{14\pi}{3} - \frac{2\pi}{3} = \frac{12\pi}{3} = 4\pi$
 $b = \frac{2\pi}{4\pi} = \frac{1}{2}$

Write a Sine equation for this graph.

