

1. Find the sum of the first 30 terms of this series: 21, 17, 13, 9, ...

2. Find the sum of the terms of this series: 19, 33, 47, 61, ..., 285

4. Solve each equation.

a) $\sqrt{x + 39} + 3 = x$

b) $\log_7 x - \log_7 (x - 5) = 2$

5. An object hangs from a spring. The formula $l = 30 + 2w$ relates the length l , in centimeters, of the spring to the weight, w , in newtons, of the object. Which of the following describes the meaning of the 2 in this context?

- A. The length, in cm, of the spring with no weight attached.
- B. The weight, in newtons, of an object that will stretch the spring 30 cm
- C. The increase in the weight, in newtons, of the object for each one-cm increase in the length of the spring.
- D. The increase in the length, in cm, of the spring for each one-newton increase in the weight of the object.

1. Find the sum of the first 30 terms of this series:

Answers

21, 17, 13, 9, ...
 Arithmetic $d = -4$
 Last term: $a_{30} = (21) + (-4)(30-1) = -95$
 $S_{30} = \frac{30}{2}(21 + -95) = -1110$

2. Find the sum of the terms of this series: 19, 33, 47, 61, ..., 285

Arithmetic $d = 14$
 # of terms $\rightarrow a_n = 19 + 14(n-1)$
 $285 = 19 + 14(n-1)$
 $266 = 14(n-1)$
 $19 = n-1$
 $n = 20$ terms

$S_{20} = \frac{20}{2}(19 + 285)$
 $S_{20} = 3040$

4. Solve each equation.

a) $\sqrt{x+39} + 3 = x$
 $\sqrt{x+39} = x-3$
 $(\sqrt{x+39})^2 = (x-3)^2$
 $x+39 = x^2 - 6x + 9$
 $0 = x^2 - 7x - 30$
 $0 = (x-10)(x+3)$
 $x = -3, 10$
 $x = 10$

b) $\log_7 x - \log_7(x-5) = 2$

$\log_7\left(\frac{x}{x-5}\right) = 2$
 $7^2 = \frac{x}{x-5}$
 $49 = \frac{x}{x-5}$
 $49(x-5) = x$
 $49x - 245 = x$
 $48x = 245$
 $x = \frac{245}{48}$

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- ☒ D. The increase in the length, in cm, of the spring for each one-newton increase in the weight of the object.

$y = mx + b$
 \uparrow rate of change
 \uparrow initial amount

$l = 30 + 2w$
 \uparrow rate of change:
 how fast the length is increasing when weight is added
 2 cm/newton