

State the number of terms in each sequence.

1. Arithmetic Sequence: $a_4 = 32$ $a_7 = 53$
last term is 137

2. Geometric Sequence: $a_3 = 36$ $a_6 = 972$
last term is 2125764

3. Write the recursive formula for this sequence:
13, 38, 68, 103, ...

4. Write the explicit formula for this sequence:
0, 1, 4, 9, 16, ...

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1. Arithmetic Sequence: $a_4 = 32$ $a_7 = 53$
last term is 137

1st: Find Common difference

$$d = \frac{53 - 32}{7 - 4} = \frac{21}{3} = 7$$

2nd: Find 1st Term

$$a_1 = a_4 - 3(7) = 32 - 21 = 11$$

3rd: write Explicit Formula

$$a_n = 11 + 7(n-1)$$

4th: Replace a_n with last term
and solve for n

$$137 = 11 + 7(n-1)$$

$$126 = 7(n-1)$$

$$18 = n-1$$

$$n = 19$$

19 terms

2. Geometric Sequence: $a_3 = 36$ $a_6 = 972$
last term is 2125764

1st: Find Common Ratio

$$r = \sqrt[3]{\frac{972}{36}} = \sqrt[3]{27} = 3$$

2nd: Find 1st Term

$$a_1 = \frac{a_3}{r \cdot r} = \frac{36}{3 \cdot 3} = 4$$

3rd: write explicit Formula

$$a_n = 4(3)^{n-1}$$

4th: Replace a_n with last term
and solve for n .

$$2125764 = 4(3)^{n-1}$$

$$531441 = 3^{n-1}$$

$$\log_3 531441 = n-1$$

$$12 = n-1$$

$$n = 13$$

13 Terms

3. Write the recursive formula for this sequence:
13, 38, 68, 103, ...

$$\begin{array}{cccc} n = & 1 & 2 & 3 & 4 \\ & 13 & 38 & 68 & 103 \\ & \vee & \vee & \vee & \\ & +25 & +30 & +35 & \\ & 5(5) & 5(6) & 5(7) & \end{array}$$

$$a_1 = 13$$

$$a_n = a_{n-1} + 5(n+3)$$

4. Write the explicit formula for this sequence:
0, 1, 4, 9, 16, ...

$$n = \begin{array}{ccccc} 1 & 2 & 3 & 4 & 5 \\ (0)^2 & (1)^2 & (2)^2 & (3)^2 & (4)^2 \end{array}$$

$$a_n = (n-1)^2$$