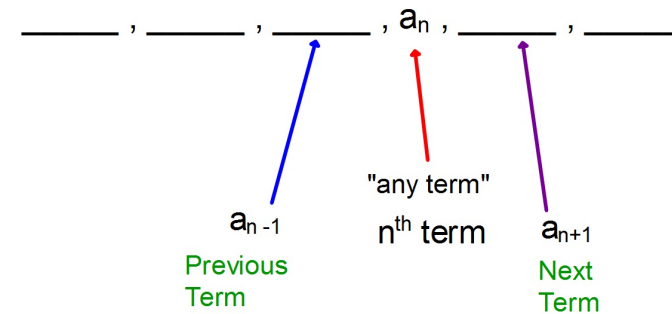


You can use a variable, such as a , with positive integer subscripts to represent the terms in a sequence.

1st term 2nd term 3rd term ...
 \downarrow \downarrow \downarrow \downarrow
 a_1 a_2 a_3 ...

What notation identifies ANY term in a sequence?



Formulas used to generate Sequences:

Recursive Formula

A formula that gives any term by relating it to the previous term or terms.

Explicit Formula

A formula that allows you to find any term by using its term #.

For example if I want to find the 20th term I can plug 20 into a formula and get just that term.

Recursive Formula Examples:

Find the first 5 terms in this sequence:

$$a_1 = 20$$

$$a_n = (a_{n-1}) \div 2 + 1$$

previous term
divided by 2 then add
+1

$$20, \frac{11}{2}, 6.5, 4.25, 3.125$$

Handwritten calculations for the sequence terms:

- $20 \div 2 + 1 = 11$
- $11 \div 2 + 1 = 6.5$
- $6.5 \div 2 + 1 = 4.25$
- $4.25 \div 2 + 1 = 3.125$

Write the first 5 terms of this sequence.

$$a_1 = 1$$

$$a_2 = 8$$

$$a_n = (a_{n-1}) - (a_{n-2})$$

any term is the difference of the previous two

$$1, 8, 7, -1, -8$$

$a_3 = a_2 - a_1 = 8 - 1$
 $a_4 = a_3 - a_2 = 7 - 8$
 $a_5 = a_4 - a_3 = -1 - 7$

Write a recursive formula for this sequence.

1. $13, 17, 21, 25, \dots$

$$a_1 = 13$$

$$a_n = a_{n-1} + 4$$

Write a recursive formula for this sequence.

2. $50, 43, 36, 29, \dots$

$$a_1 = 50$$

$$a_n = a_{n-1} - 7$$

Write a recursive formula for each sequence.

1. $1664, -416, 104, -26, \dots$

$\div -4 \quad \div -4 \quad \div -4$

$$a_1 = 1664$$

$$a_n = (a_{n-1}) \cdot \left(-\frac{1}{4}\right)$$

2. $13.5, 16, 18.5, 21, \dots$

$+2.5 \quad +2.5 \quad +2.5$

$$a_1 = 13.5$$

$$a_n = a_{n-1} + 2.5$$

Explicit Formula

A formula that allows you to find any term (a_n) by using it's term # (n).

The formula must use

$n=1$ to find the 1st term

$n=2$ to find the 2nd term

$n=3$ to find the 3rd term....

Explicit Formula Example:

Find the 1st, 5th, and 10th term in this sequence.

$$a_n = 2n^2 - 1$$

$$a_1 = 2(1)^2 - 1 = 1$$

$$a_5 = 2(5)^2 - 1 = 49$$

$$a_{10} = 2(10)^2 - 1 = 199$$

Find the 1st, 5th, and 10th term in this sequence.

$$a_n = (n + 1)(3)^{n-1}$$

$$a_1 = (1+1)(3)^{1-1} = 2 \cdot 3^0 = 2 \cdot 1 = 2$$

$$a_5 = (5+1)(3)^{5-1} = 6(3)^4 = 486$$

$$a_{10} = (10+1)(3)^{10-1} = 11(3)^9 = 216513$$

Write an explicit formula for this sequence.

$$n = 1 \quad 2 \quad 3 \quad 4$$
$$1. \quad 3, 9, 27, 81, \dots$$
$$3^1 \quad 3^2 \quad 3^3 \quad 3^4$$

$$a_n = 3^n$$

Write an explicit formula for this sequence.

$n = 1 \ 2 \ 3 \ 4$
2. $2, 4, 6, 8, \dots$

$$a_n = 2n$$

Write an explicit formula for this sequence.

$n = 1 \ 2 \ 3 \ 4$
3. $20, 30, 40, 50, \dots$
 $2(10) \ 3(10) \ 4(10) \ 5(10)$

$$a_n = (10)(n+1)$$

Write an explicit formula for this sequence.

$n = 1 \ 2 \ 3 \ 4$
4. $10, 40, 90, 160 \dots$
 $1(10) \ 4(10) \ 9(10) \ 16(10)$

$$a_n = (10)(n^2)$$

You can now finish Hwk #29

Sec 11-1

~~Due Monday~~ Tomorrow for you!

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Problems 4-7, 13, 14, 18, 19, 34, 35, 46, 47