

Standard Form of the Equation for Hyperbolas with center at (h,k):

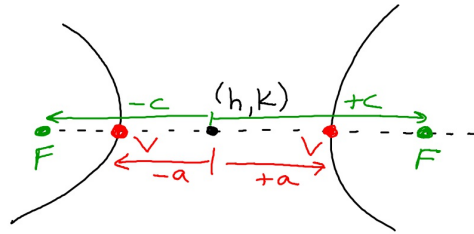
Horizontal Transverse Axis:

$$\frac{(x-h)^2}{a^2} - \frac{(y-k)^2}{b^2} = 1$$

Vertices: $(h \pm a, k)$

Foci: $(h \pm c, k)$

Asymptotes: $m = \pm \frac{b}{a}$



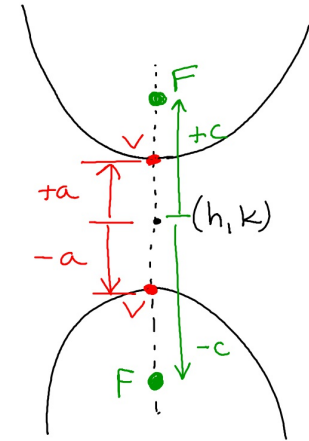
Vertical Transverse Axis:

$$\frac{(y-k)^2}{a^2} - \frac{(x-h)^2}{b^2} = 1$$

Vertices: $(h, k \pm a)$

Foci: $(h, k \pm c)$

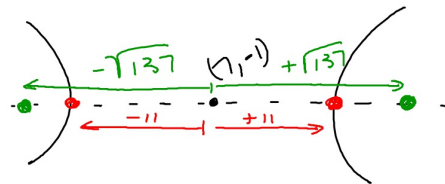
Asymptotes: $m = \pm \frac{a}{b}$



$$\frac{(x-7)^2}{121} - \frac{(y+1)^2}{16} = 1 \quad a^2=121 \quad a=11 \quad b^2=16 \quad b=4$$

Find each of the following:

- Center $(7, -1)$
- Vertices $(-4, -1)$ $(18, -1)$
- Foci $(7 \pm \sqrt{137}, -1)$
- Transverse Axis length
 $2a = 2(11) = 22$
- Slope of Asymptotes
 $m = \pm \frac{b}{a} = \pm \frac{4}{11}$

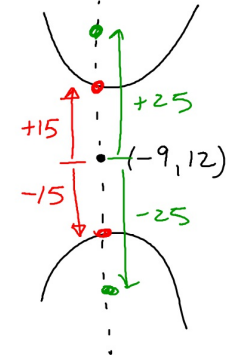


$$\begin{aligned} c^2 &= a^2 + b^2 \\ c^2 &= 121 + 16 \\ c^2 &= 137 \\ c &= \sqrt{137} \end{aligned}$$

$$\frac{(y-12)^2}{225} - \frac{(x+9)^2}{400} = 1 \quad a^2=225 \quad a=15 \quad b^2=400 \quad b=20$$

Find each of the following:

- Center $(-9, 12)$
- Vertices $(-9, 27)$ $(-9, -3)$
- Foci $(-9, 37)$ $(-9, -13)$
- Transverse Axis length
 $2(15) = 30$
- Slope of Asymptotes
 $m = \pm \frac{a}{b} = \pm \frac{15}{20}$



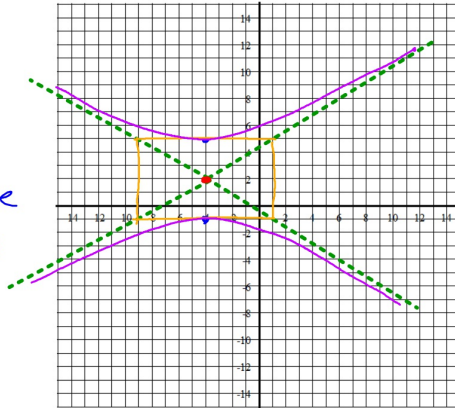
$$\begin{aligned} c^2 &= a^2 + b^2 \\ c^2 &= 225 + 400 \\ c^2 &= 625 \\ c &= 25 \end{aligned}$$

Graph this Hyperbola showing the Vertices and Asymptotes.

$$\frac{(y-2)^2}{9} - \frac{(x+4)^2}{25} = 1$$

Center
(-4, 2)

$a^2=9$
 $a=3$ vertices are 3 above & below the center
 $m = \pm \frac{3}{5}$



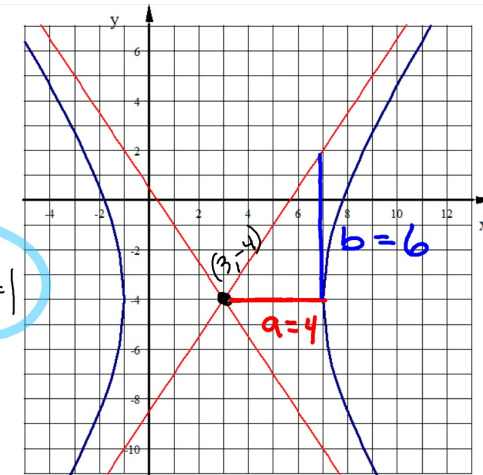
Write the equation of this Hyperbola:

center = (3, -4)
branches open in x-direction

$$\frac{(x-3)^2}{16} - \frac{(y+4)^2}{36} = 1$$

$\uparrow$
 a^2

$\uparrow$
 b^2

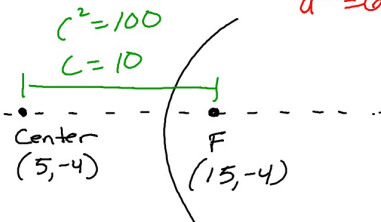


The center is (5, -4), the Transverse Axis has a length of 16. $\rightarrow 2a=16$
One Focus is (15, -4). Write the equation of this Hyperbola.
 $a=8$
 $a^2=64$

$$\frac{(x-5)^2}{64} - \frac{(y+4)^2}{36} = 1$$

$\uparrow$
 a^2

$\uparrow$
 b^2



$$c^2 = a^2 + b^2$$

$$100 = 64 + b^2$$

$$36 = b^2$$

The Foci are (3, 10) and (3, -8) and one Vertex is (3, -6).
Write the equation of this Hyperbola.

$$\frac{(y-1)^2}{49} - \frac{(x-3)^2}{32} = 1$$

$\uparrow$
 a^2

$\uparrow$
 b^2

