

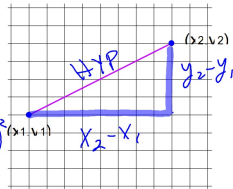
The distance form

The distance between the two points (x_1, y_1) & (x_2, y_2) is found by using the following formula

$$d = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$

$$\text{Hyp}^2 = \text{Leg}^2 + \text{Leg}^2$$

$$\text{Hyp} = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$



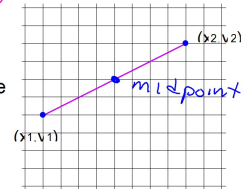
The distance formula is actually the hypotenuse of a right triangle. Therefore, the distance formula is actually a variation of the Pythagorean Theorem.

Midpoint Form

The midpoint of a segment whose endpoints are (x_1, y_1) and (x_2, y_2) is found using the following formula

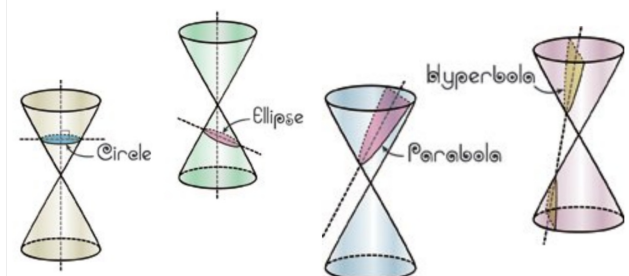
$$\text{midpoint} : \left(\frac{x_1 + x_2}{2}, \frac{y_1 + y_2}{2} \right)$$

The midpoint is the point whose coordinates are the averages of the x and y coordinates of the endpoints.

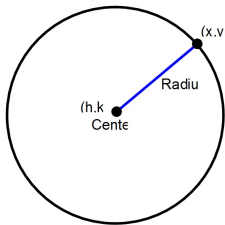


The four Conic Sect

- Circle
- Ellipse
- Hyperbola
- Parabola



Use the distance formula to find an expression for the length of the radius



$$r = \sqrt{(x-h)^2 + (y-k)^2}$$

If you square both sides

$$(r)^2 = \left(\sqrt{(x-h)^2 + (y-k)^2} \right)^2$$

$$r^2 = (x-h)^2 + (y-k)^2$$

This is the equation of a circle whose center is at (h, k) and whose radius is r .

Equation of a circle whose center is at (h, k) and radius r

$$(x-h)^2 + (y-k)^2 = r^2$$

Equation of a circle whose center is at the origin $(0, 0)$ and radius r

$$x^2 + y^2 = r^2$$

Find the equation of the circle that is a translation of the circle $x^2 + y^2 = 36$ 5 units right and 7 units up

$$x^2 + y^2 = 36$$

center (h, k)

$$(x-5)^2 + (y+7)^2 = 36$$

The circle $x^2 + y^2 = 100$ was translated 4 units left and 9 units up. Write the new equation of the circle.

original center $(3, -2)$

4 left 9 up

$$3-4 \quad -2+9$$

new center $(-1, 7)$

$$(x+1)^2 + (y-7)^2 = 100$$

Given the equation of a circle $x^2 + y^2 = 32$;
state the coordinates of the center and the radius.

Center:

$(0, 0)$

Radius =

$$\sqrt{32} < 5.66$$

$$r^2 = 32$$

Given the equation of a circle is $(x+4)^2 + (y-7)^2 = 81$
state the coordinates of the center and the radius.

Center:

$(-4, 7)$

Radius

$$\sqrt{r^2} = \sqrt{81}$$

$$r = 9$$

Given the equation of a circle is $(x-5)^2 + (y+7)^2 = 441$
State the coordinates of the center of the circle and
find the length of the diameter.

Center:

$(5, -7)$

Diameter =

$$r^2 = 441$$

$$r = \sqrt{441} = 21$$

$$d = 2 \cdot r = 2(21)$$

The equation of a circle is $(x-3)^2 + y^2 = 45$

State the coordinates of the center of the circle
find the length of the diameter

Center:

$(3, 0)$

Diameter =

$$r = \sqrt{45} = 3\sqrt{5}$$

$$d = 2 \cdot r = 2(3\sqrt{5}) = 6\sqrt{5}$$

The center of a circle is (-4,9) and the radius is 5
equation of this circle

$$(x+4)^2 + (y-9)^2 = 25$$

4 left 9 up $r^2 = (5)^2$

The center of a circle is (0,0) and the point (5,-8) is on the circle.
Write the equation of this circle.

$$x^2 + y^2 = 89$$

$$d = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$

The radius is the distance from the center to any point on the circle.

$$\begin{aligned} & \sqrt{(5-0)^2 + (-8-0)^2} \\ & \sqrt{25 + 64} \\ r = \sqrt{89} & \rightarrow r^2 = (\sqrt{89})^2 \\ & r^2 = 89 \end{aligned}$$

The center of a circle is (21,9) and the point (16,-1) is on the circle.
Write the equation of the circle.

$$(x-21)^2 + (y-9)^2 = 125$$

$$d = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$

The radius is the distance from the center to any point on the circle.

$$\begin{aligned} & \sqrt{(5)^2 + (10)^2} \\ r = \sqrt{125} & \rightarrow r^2 = 125 \end{aligned}$$