

1. Given the Ellipse: $4(x - 3)^2 + (y + 7)^2 = 1$. Find the coordinates of the following:

Vertices:

Co-Vertices:

Foci:

2. Given a Co-Vertex at $(20, 45)$ and a Focus at $(23, 52)$, write the two possible equations of this ellipse.

3. If x and y are integers, and $3x + 2y = 13$, which of the following could be the value of y ?

A. 0

B. 1

C. 2

D. 3

E. 4

1. Given the Ellipse: $4(x-3)^2 + (y+7)^2 = 1$. Find the coordinates of the following:

Vertices: $(3, -6)$ & $(3, -8)$ Co-Vertices: $(\frac{5}{2}, -7)$ & $(\frac{7}{2}, -7)$ Foci: $(3, -7 \pm \frac{\sqrt{3}}{2})$

$$4(x-3)^2 + (y+7)^2 = 1$$

$$\frac{(x-3)^2}{\frac{1}{4}} + \frac{(y+7)^2}{1} = 1$$

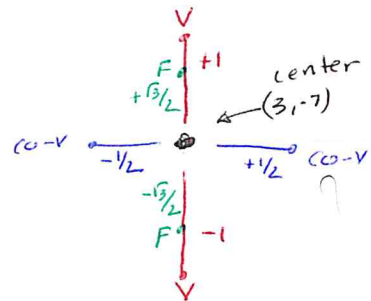
center $(3, -7)$

major axis is vertical

$$a^2 = 1 \rightarrow a = \pm 1$$

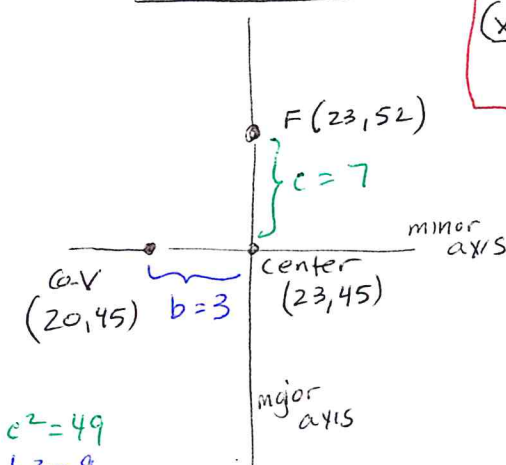
$$b^2 = \frac{1}{4} \rightarrow b = \pm \frac{1}{2}$$

$$c^2 = 1 - \frac{1}{4} = \frac{3}{4} \quad c = \pm \frac{\sqrt{3}}{2}$$



2. Given a Co-Vertex at $(20, 45)$ and a Focus at $(23, 52)$, write the two possible equations of this ellipse.

1st Possibility



$$c^2 = 49$$

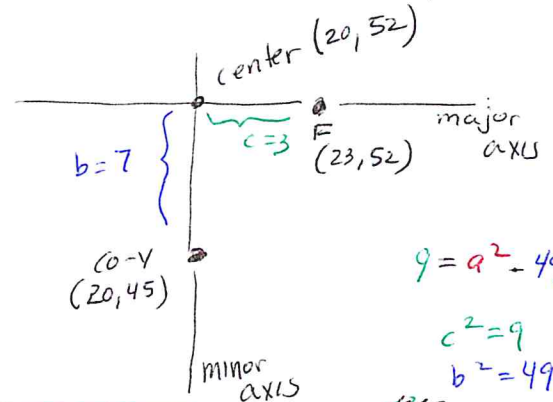
$$b^2 = 9$$

$$49 = a^2 - 9$$

$$a^2 = 58$$

$$\frac{(x-23)^2}{9} + \frac{(y-45)^2}{58} = 1$$

2nd Possibility



$$9 = a^2 - 49$$

$$c^2 = 9$$

$$b^2 = 49$$

$$a^2 = 58$$

$$\frac{(x-20)^2}{58} + \frac{(y-52)^2}{49} = 1$$

3. If x and y are integers, and $3x + 2y = 13$, which of the following could be the value of y ?

- A. 0 B. 1 C. 2 D. 3 E. 4

$$3x + 2y = 13$$

$x = \frac{13 - 2y}{3}$ Now replace y with the above choices & find the value that makes x an integer

X A. 0 $\rightarrow x = \frac{13 - 2(0)}{3} = \frac{13}{3}$ NOT an integer

X B. 1 $\rightarrow x = \frac{13 - 2(1)}{3} = \frac{11}{3}$ NOT an integer

✓ C. 2 $\rightarrow x = \frac{13 - 2(2)}{3} = \frac{9}{3} = 3$ This is an integer