

1. Find the coordinates of the center and the EXACT length of the radius of the given circle.

$$(x + 7)^2 + (y - 13)^2 = \sqrt{37}$$

Center:

Radius =

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2. Write the equation of each circle.

a) The center is  $(2, 5)$  and the diameter is  $\sqrt{17}$

b) The center is  $(8, -3)$  and  $(14, 2)$  is on the circle.

c) The endpoints of a diameter are  $(5, -1)$  &  $(-2, 2)$ .

3. How many times do these two circles intersect?

$$(x + 4)^2 + (y - 1)^2 = 144 \quad \text{and} \quad (x - 11)^2 + (y + 7)^2 = 64$$

1. Find the coordinates of the center and the EXACT length of the radius of the given circle.

$$(x+7)^2 + (y-13)^2 = \sqrt{37}$$

-7 Left 13 up

$$r^2 = \sqrt{37}$$

Center:

$$(-7, 13)$$

$$\text{Radius} = \sqrt[4]{37}$$

$$r = \sqrt{\sqrt{37}} = (37^{1/2})^{1/2} = 37^{1/4} = \sqrt[4]{37}$$

2. Write the equation of each circle.

a) The center is (2,5) and the diameter is  $\sqrt{17}$

$$d = \sqrt{17}$$

$$r = \frac{\sqrt{17}}{2}$$

$$r^2 = \left(\frac{\sqrt{17}}{2}\right)^2 = \frac{17}{4}$$

$$(x-2)^2 + (y-5)^2 = \frac{17}{4}$$

b) The center is (8,-3) and (14,2) is on the circle.

$$r = \sqrt{(14-8)^2 + (2-(-3))^2}$$

$$= \sqrt{6^2 + 5^2} = \sqrt{36+25}$$

$$r = \sqrt{61}$$

$$(x-8)^2 + (y+3)^2 = 61$$

c) The endpoints of a diameter are (5,-1) & (-2,2).

$$\text{center is midpoint of } (5,-1) \text{ \& } (-2,2) \rightarrow \left(\frac{5+(-2)}{2}, \frac{-1+2}{2}\right) = \left(\frac{3}{2}, \frac{1}{2}\right)$$

For radius use distance formula from center to either endpoint

$$r = \sqrt{\left(\frac{3}{2} - (-2)\right)^2 + \left(\frac{1}{2} - 2\right)^2} =$$

$$= \sqrt{\left(\frac{7}{2}\right)^2 + \left(-\frac{3}{2}\right)^2}$$

$$= \sqrt{\frac{49}{4} + \frac{9}{4}} = \sqrt{\frac{58}{4}} = \sqrt{\frac{29}{2}}$$

$$\left(x - \frac{3}{2}\right)^2 + \left(y - \frac{1}{2}\right)^2 = \frac{29}{2}$$

3. How many times do these two circles intersect?

$$(x+4)^2 + (y-1)^2 = 144 \quad \text{and} \quad (x-11)^2 + (y+7)^2 = 64$$

$$\text{center } (-4, 1)$$

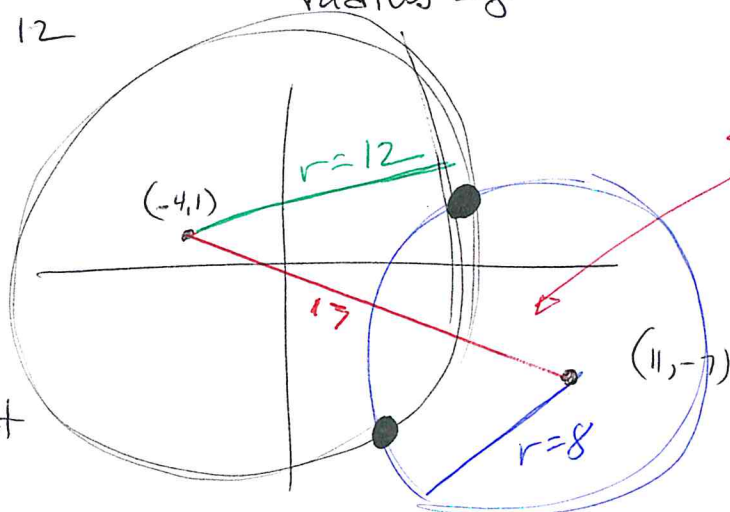
$$\text{radius} = 12$$

$$\text{center } (11, -7)$$

$$\text{radius} = 8$$

2 points of intersection

Since the two radii have a sum greater than the distance between the centers, the circles intersect twice



DISTANCE BETWEEN CENTERS:

$$\begin{aligned} &= \sqrt{(11-(-4))^2 + (-7-1)^2} \\ &= \sqrt{15^2 + 8^2} \\ &= \sqrt{225 + 64} \\ &= \sqrt{289} \\ &= 17 \end{aligned}$$