

Use the two formulas and the points given to answer the questions.

Distance Formula: $d = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$

Midpoint Formula: $Midpoint : \left(\frac{x_1 + x_2}{2}, \frac{y_1 + y_2}{2} \right)$

Points: $A(12, -7)$ $B(-3, 4)$ $C(5, 7)$ $D(-8, -2)$ $E(13, 1)$

Find the EXACT length of each segment.

1. AC

2. AD

3. CE

4. BD

Find the midpoint of each segment.

5. CD

6. DE

7. AC

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Find the EXACT length of each segment.

1. AC

$$\begin{aligned} d &= \sqrt{(12 - 5)^2 + (-7 - 7)^2} \\ &= \sqrt{7^2 + 14^2} \\ &= \sqrt{49 + 196} \\ &= \sqrt{245} \\ &= \sqrt{49 \cdot 5} \\ &= 7\sqrt{5} \end{aligned}$$

2. AD

$$\begin{aligned} d &= \sqrt{(12 - -8)^2 + (-7 - -2)^2} \\ &= \sqrt{20^2 + 5^2} \\ &= \sqrt{400 + 25} \\ &= \sqrt{425} \\ &= \sqrt{25 \cdot 17} \\ &= 5\sqrt{17} \end{aligned}$$

3. CE

$$\begin{aligned} d &= \sqrt{(13 - 5)^2 + (7 - 1)^2} \\ &= \sqrt{8^2 + 6^2} \\ &= \sqrt{64 + 36} \\ &= \sqrt{100} \\ &= 10 \end{aligned}$$

4. BD

$$\begin{aligned} d &= \sqrt{(-3 - -8)^2 + (4 - -2)^2} \\ &= \sqrt{5^2 + 6^2} \\ &= \sqrt{25 + 36} \\ &= \sqrt{61} \end{aligned}$$

Find the midpoint of each segment.

5. CD

$$\begin{aligned} &\left(\frac{5 + -8}{2}, \frac{7 + -2}{2} \right) \\ &\left(\frac{-3}{2}, \frac{5}{2} \right) \\ &\text{or} \\ &(-1.5, 2.5) \end{aligned}$$

6. DE

$$\begin{aligned} &\left(\frac{13 + -8}{2}, \frac{-2 + 1}{2} \right) \\ &\left(\frac{5}{2}, \frac{-1}{2} \right) \\ &\text{or} \\ &(2.5, -0.5) \end{aligned}$$

7. AC

$$\begin{aligned} &\left(\frac{12 + 5}{2}, \frac{7 + -7}{2} \right) \\ &\left(\frac{17}{2}, \frac{0}{2} \right) \\ &\text{or} \\ &\left(\frac{17}{2}, 0 \right) \\ &\text{or} \\ &(8.5, 0) \end{aligned}$$