

1. Rationalize the denominator.

Simplify your answer.

$$\frac{12}{7 + \sqrt{5}}$$

2. Solve each.

a) $\sqrt{x+1} + 5 = x$

b) $5(2x - 1)^{\frac{3}{2}} + 9 = 144$

3. Simplify. Make sure you leave answers with whole number exponents and no decimal coefficients.

$$\left(\frac{9P^{-10}Q^8}{9^{-1}P^{-2}Q^{-7}} \right)^{-\frac{3}{4}}$$

4. Simplify. $(6 - 2\sqrt{3})(5 + 8\sqrt{3})$

1. Rationalize the denominator.

Simplify your answer.

$$\frac{12}{7+\sqrt{5}} \cdot \frac{7-\sqrt{5}}{7-\sqrt{5}} = \frac{12(7-\sqrt{5})}{49-5} = \frac{12(7-\sqrt{5})}{44} = \frac{3(7-\sqrt{5})}{11} \text{ or } \frac{21-3\sqrt{5}}{11}$$

2. Solve each.

a) $\sqrt{x+1} + 5 = x$
 $\quad \quad \quad -5 \quad -5$

$$(\sqrt{x+1})^2 = (x-5)^2$$

$$\begin{array}{rcl} x+1 & = & x^2-10x+25 \\ -x & -1 & -x \quad -1 \end{array}$$

$$0 = x^2 - 11x + 24$$

$$0 = (x-8)(x-3)$$

$$x = \cancel{3}, 8$$

$$x = 8$$

b) $5(2x-1)^{\frac{3}{2}} + 9 = 144$
 $\quad \quad \quad -9 \quad -9$

$$\frac{5(2x-1)^{\frac{3}{2}}}{5} = \frac{135}{5}$$

$$[(2x-1)^{\frac{3}{2}}]^{\frac{2}{3}} = (27)^{\frac{2}{3}}$$

$$\begin{array}{rcl} 2x-1 & = & 9 \\ +1 & +1 & \end{array}$$

→

$$\frac{2x-10}{2} = \frac{10}{2}$$

$$x = 5$$

3. Simplify. Make sure you leave answers with whole number exponents and no decimal coefficients.

$$\left(\frac{9p^{-10}q^8}{9^{-1}p^{-2}q^{-7}}\right)^{-\frac{3}{4}} = \left(\frac{9 \cdot 9 q^{15}}{p^8}\right)^{-3/4} = \left(\frac{p^8}{81 q^{15}}\right)^{3/4}$$

$$\frac{p^{8 \cdot 3/4}}{81^{3/4} q^{15 \cdot 3/4}} = \frac{p^6}{27 q^{45/4}}$$

$$(\sqrt[4]{81})^3 = (3)^3 = 27$$

4. Simplify.

$$(6-2\sqrt{3})(5+8\sqrt{3})$$

	6	-2√3
5	30	-10√3
+8√3	+48√3	-48

→

$$-18 + 38\sqrt{3}$$