

Solve each.

1. $(2x - 1)^{\frac{1}{3}} = (x + 1)^{\frac{1}{6}}$

2. $\sqrt{24 - 4x} - x = -3$

3. $2 + \sqrt{3x^2 - 11} = x^2 - 3$

4. $(x^2y^3)^{\frac{1}{2}}(x^2y^3)^{\frac{1}{2}} = x^{\frac{a}{3}}y^{\frac{a}{2}}$

If the equation above, where a is a constant, is true for all positive values of x and y , what is the value of a ?

- A. 2 B. 3 C. 5 D. 6

Solve each.

1. $(2x-1)^{\frac{1}{3}} = (x+1)^{\frac{1}{6}}$

$$(2x-1)^2 = x+1$$

$$4x^2 - 4x + 1 = x + 1$$

$$4x^2 - 5x = 0$$

$$x(4x-5) = 0$$

$$x = 0, 5/4$$

$$x = \frac{5}{4}$$

$$\begin{array}{r|rr} 2x & 4x^2 & -4x \\ -1 & -4x & +1 \end{array}$$

2. $\sqrt{24-4x} - x = -3$
 $\quad \quad \quad +x \quad +x$

$$(\sqrt{24-4x})^2 = (x-3)^2$$

$$24-4x = x^2-6x+9$$

$$0 = x^2 - 2x - 15$$

$$0 = (x-5)(x+3)$$

$$x = 5, -3$$

$$x = 5$$

$$\begin{array}{r|rr} -15 & & \\ -5 & +3 & \\ -2 & & \end{array}$$

3. $2 + \sqrt{3x^2-11} = x^2-3$
 $\quad \quad \quad -2 \quad \quad \quad -2$

$$(\sqrt{3x^2-11})^2 = (x^2-5)^2$$

$$3x^2-11 = x^4-10x^2+25$$

$$0 = x^4 - 13x^2 + 36$$

$$0 = (x^2-9)(x^2-4)$$

$$0 = (x \pm 3)(x \pm 2)$$

$$x = \pm 3, \pm 2$$

$$x = \pm 3$$

$$\begin{array}{r|rr} x^2-5 & & \\ x^2 & x^4 & -5x^2 \\ -5 & -5x^2 & +25 \end{array}$$

$$\begin{array}{r|rr} 36 & & \\ -9 & -4 & \\ -13 & & \end{array}$$

4. $(x^2y^3)^{\frac{1}{2}}(x^2y^3)^{\frac{1}{2}} = x^{\frac{a}{3}}y^{\frac{a}{2}}$

If the equation above, where a is a constant, is true for all positive values of x and y , what is the value of a ?

A. 2

B. 3

C. 5

D. 6

$$(x^2y^3)^{\frac{1}{2}}(x^2y^3)^{\frac{1}{2}} = x^{\frac{a}{3}}y^{\frac{a}{2}}$$

$$(x^1y^{\frac{3}{2}})(x^1y^{\frac{3}{2}}) = x^{\frac{a}{3}}y^{\frac{a}{2}}$$

$$3 = \frac{a}{2}$$

$$a = 6$$

$$x^2y^3 = x^{\frac{a}{3}}y^{\frac{a}{2}}$$

$$2 = \frac{a}{3}$$

$$a = 6$$