

Suppose  $f$  is a periodic function with a period of 10

Given  $f(12)=23$  and  $f(51)=2$

This represents  
the point (12,23)

This represents  
the point (51,2)

The period of 10 means  
that if you start at any  $x$ -value  
and move a multiple of 10 in  
any direction you will get the  
same  $y$ -value.

Find  $f(32) = 23$

Since 32 is 20 units away from  
12 (2 periods) it must have the  
same  $y$ -value.

Find  $f(41) = 2$

Since 41 is 10 units away from  
51 (1 period) it must have the  
same  $y$ -value.

Suppose  $f$  is a periodic function with a period of 18

Given  $f(5) = -9$  and  $f(16) = 27$

every 18 units  $y$ -values  
repeat.

Find  $f(-49) = -9$

-49 is 54 units away from  
5 (3 periods). Therefore,  
it must have the same  
 $y$ -value.

Find  $f(106) = 27$

106 is 90 units away from 16 (5 periods).  
Therefore, it must have the same  $y$ -value.

What is the measure of an angle?

The size of an angle

or

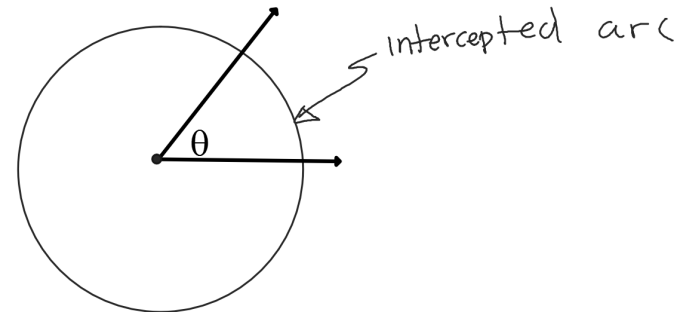
The amount of turn to move from one side the other side.

Units used to measure angles:

- Degrees
- Radians

Central Angle:

An angle whose vertex is at  
the center of a circle.

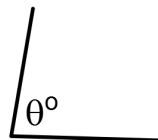


# Θ

Greek letter Theta

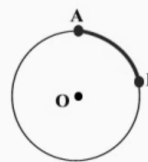
Variable often used to represent an angle

Sinθ



What is an Arc ?

What is Arc Length ?

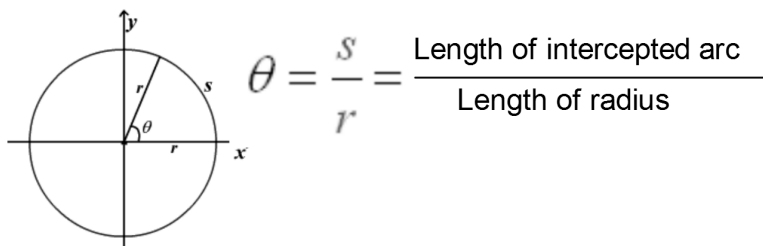


An **arc** of a circle is a "portion" of the circumference of the circle.

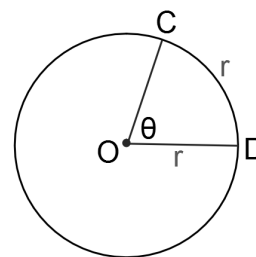
The **length of an arc** is simply the length of its "portion" of the circumference. Actually, the circumference itself can be considered an arc length.

Radian Measure of an angle:

Ratio of the length of the arc intercepted by a central angle to the radius of the circle.



One radian is the measure of an angle that intercepts an arc whose length is equal to the radius of the circle.



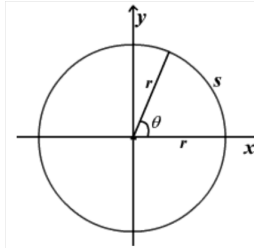
$m\angle COD = 1 \text{ radian}$

$$\theta = \frac{s}{r} = \frac{r}{r} = 1$$

Using this formula:  $\theta = \frac{s}{r}$

You can write this as:  $S = \theta r$

Length of an arc equals the measure of the angle, in radians, times the radius.



If the arc length equals the entire circle then  $S$  is the entire circumference  $S=2\pi r$

$S = \theta r$  becomes  $2\pi r = \theta r$

If you divide both sides by  $r$  you get:

$$2\pi = \theta$$

This means a full circle is equal to  $2\pi$  radians.

So the relationship between degrees and radians is:

$$2\pi = 360^\circ$$

This can be simplified into:  $\pi = 180^\circ$