

-1 and 2 are solutions of the equation below.

$$x^4 - x^3 + 2x^2 - 4x - 8 = 0$$

The other two solutions are imaginary.

How could you find the other two?

Divide this polynomial by the factors $(x+1)$ and $(x-2)$. This will leave you a Quadratic which you can then either factor or use Quadratic Formula to find the remaining two solutions.

$$\begin{array}{r} 15 \text{ --- quotient} \\ 8 \overline{) 120} \\ \text{divisor} \quad \text{dividend} \end{array}$$

Polynomial Long Division:

$$\frac{x^2 + 9x + 20}{x + 4} = x + 4 \overline{) x^2 + 9x + 20} = \boxed{x + 5}$$

$$\begin{array}{r} x + 5 \\ \textcircled{x+4} \overline{) \textcircled{x^2} + 9x + 20} \\ - x^2 + 4x \\ \hline 5x + 20 \\ - 5x + 20 \\ \hline 0 \end{array}$$

Find this quotient.

$$\frac{2x^3 - 7x^2 + x - 9}{x + 3} = \boxed{2x^2 - 13x + 40 \quad R = -129}$$

$$\begin{array}{r} 2x^2 - 13x + 40 \\ x+3 \overline{) 2x^3 - 7x^2 + x - 9} \\ - 2x^3 + 6x^2 \\ \hline -13x^2 + x - 9 \\ - -13x^2 - 39x \\ \hline +40x - 9 \\ - 40x + 120 \\ \hline -129 \end{array}$$

Ways to leave a remainder.

$$\frac{2x^3 - 7x^2 + x - 9}{x + 3} = 2x^2 - 13x + 40 \quad R = -129$$

$$\frac{2x^3 - 7x^2 + x - 9}{x + 3} = 2x^2 - 13x + 40 - \frac{129}{x+3}$$

Find this quotient.

$$\frac{4x^3 + 2x^2 - 15x - 17}{x - 9} = 4x^2 + 38x + 327 \quad R = 2926$$

$$\begin{array}{r} 4x^2 + 38x + 327 \\ (x-9) \overline{) 4x^3 + 2x^2 - 15x - 17} \\ \underline{4x^3 - 36x^2} \\ 38x^2 - 15x \\ \underline{38x^2 - 342x} \\ 327x - 17 \\ \underline{327x - 2943} \\ 2926 \end{array}$$

Find this quotient.

$$\frac{2x^3 + x^2 - 19x + 10}{2x - 5} = x^2 + 3x - 2$$

$$\begin{array}{r} x^2 + 3x - 2 \\ 2x-5 \overline{) 2x^3 + x^2 - 19x + 10} \\ \underline{2x^3 - 5x^2} \\ 6x^2 - 19x \\ \underline{6x^2 - 15x} \\ -4x + 10 \\ \underline{-4x + 10} \\ 0 \end{array}$$

Find this quotient.

$$\frac{2x^3 - 7x + 8}{x - 3} = 2x^2 + 6x + 11 \quad R = 41$$

$$\begin{array}{r} 2x^2 + 6x + 11 \\ x-3 \overline{) 2x^3 + 0x^2 - 7x + 8} \\ \underline{2x^3 - 6x^2} \\ 6x^2 - 7x \\ \underline{6x^2 - 18x} \\ 11x + 8 \\ \underline{11x - 33} \\ 41 \end{array}$$