

1. Monomial:

A real number, a variable,  
or the product of a real  
number and variables.

a Term

Give three examples of a monomial:

-12,  $x^2$ ,  $9.3a^3b^5$

2. Polynomial:

A monomial or the  
sum of monomials

A monomial is a polynomial  
with just one term

Give two examples of a polynomial:

$7w$ ,  $x + 9$ ,  $3y^2 - 8y + 1$

$y = (3x + 1)(x - 8)$  This is called factored form

$y = 3x^2 - 23x - 8$  This is called expanded form

3. a. The exponents of monomials and polynomials must be what kind of numbers?

Whole Numbers

b. The coefficients of a polynomial must be what kind of numbers?

Real Numbers

Definition

Polynomial Function

$P(x) = a_nx^n + a_{n-1}x^{n-1} + \dots + a_1x + a_0$  where  $n$  is a nonnegative integer  
and the coefficients  $a_n, \dots, a_0$   
are real numbers.

4. What does a polynomial in standard form look like?

Terms are put in descending order using the degree(exponents)  
with the term having the largest exponent first.

5. The leading coefficient of a polynomial is

The coefficient of the term with the largest exponent.

If it's in Standard Form it will be the first coefficient.

6. The degree of a polynomial is

The largest degree(exponent) of any term after expanding.

If it's in Standard Form it will be the first exponent.

**standard form of a polynomial.** A one-variable polynomial in standard form has no two terms with the same degree, since all like terms have been combined.

$P(x) = 2x^3 - 5x^2 - 2x + 5$

Degree (points to  $x^3$ )  
 Leading coefficient (points to 2)  
 Cubic term (points to  $x^3$ )  
 Quadratic term (points to  $x^2$ )  
 Linear term (points to  $x$ )  
 Constant term (points to 5)  
 Polynomial (points to the entire expression)

7. Complete these two tables by filling in the blanks.

Degree of Polynomial	Name by Degree
0	Constant
1	Linear
2	Quadratic
3	Cubic

# of terms in polynomial	Name by # of terms
1	Monomial
2	Binomial
3	Trinomial

8. Is each of the below a polynomial? If not give a reason.

a)  $y = \frac{3}{7}x^2 + 3x - 14x^4 + 4$   
Yes

b)  $y = 4x^{-2} + x^3 - \frac{8}{x}$   
No, There is a neg exponent and the last term has a variable in the denominator which indicates a negative exponent.

c)  $y = 9\sqrt{x} + 3x^7 - x^{\frac{2}{3}}$   
No, there is a fractional exponent and the first term has a variable under the radical which indicates a fractional exponent.

d)  $y = 9^x + 10ix^4 - 15$   
No, there is an imaginary number as a coefficient and a variable as an exponent which means that an exponent may not be a whole number.

9. a)  $9x + 2 - x^2$

Standard Form:  $-x^2 + 9x + 2$

Degree: 2

Leading Coefficient: -1

Name by Degree: Quadratic

Name by # of terms: Trinomial

b)  $15 + 8x^3 - 3(x + 5) = 15 + 8x^3 - 3x - 15 = 8x^3 - 3x$

Standard Form:  $8x^3 - 3x$

Degree: 3

Leading Coefficient: 8

Name by Degree: Cubic

Name by # of terms: Binomial

10. State the degree of each polynomial.

Polynomials in Expanded Form:

a)  $7x^2 + 12 - 13x^4 + 8x$

Degree: 4

b)  $9x + 1$

Degree: 1

c) 6

Degree: 0

Polynomials in Factored Form:

d)  $(x + 3)(2x - 1) = 2x^2 \dots$

Degree: 2

e)  $(x - 7)^2(x - 5)$   
 $(x^2) \cdot (x) = x^3$   
 Degree: 3