

Now you try this one.

Solve.

$$(x+7)^{\frac{2}{3}} + 2 = 18$$

$$\left[(x+7)^{\frac{2}{3}} \right]^{\frac{3}{2}} = (16)^{\frac{3}{2}} = (\sqrt{16})^3 = (\pm 4)^3 = \pm 64$$

$$x+7 = 64-7 = 57$$

$$x+7 = -64-7 = -71$$

$$x = -71, 57$$

Solve.

$$(\sqrt{x^2+5})^2 = (\sqrt{x+11})^2$$

$$x^2+5 = x+11$$

$$x = 3, -2$$

$$x^2 - x - 6 = 0$$

$$(x-3)(x+2) = 0$$

What is different about this one? There is an x outside of the radical.

$$\sqrt{3x-5} + 1 = x$$

$$(\sqrt{3x-5})^2 = (x-1)^2$$

$$3x-5 = x^2-2x+1$$

$$0 = x^2-5x+6$$

$$0 = (x-2)(x-3)$$

$$x = 2, 3$$

Solve.

$$\sqrt{3x+13} - 5 = x$$

$$(\sqrt{3x+13})^2 = (x+5)^2$$

$$3x+13 = x^2+10x+25$$

$$0 = x^2+7x+12$$

$$0 = (x+3)(x+4)$$

$$x = -3, -4$$

es

Solve. $\sqrt{24-4x} + 3 = x$

$$\begin{aligned} (\sqrt{24-4x})^2 &= (x-3)^2 \\ 24-4x &= x^2-6x+9 \\ 0 &= x^2-2x-15 = (x-5)(x+3) \end{aligned}$$

The last step in any solving process is to:

CHECK YOUR ANSWERS!

$$\begin{array}{r} -5 \\ -2 \end{array} \begin{array}{r} -15 \\ +3 \end{array} \quad x = 5, -3$$

↑
Extraneous

$$x = 5$$

Solve.

$$\sqrt{5x+10} - 2 = x$$

$$(\sqrt{5x+10})^2 = (x+2)^2$$

$$5x+10 = x^2+4x+4$$

$$\begin{array}{r} -6 \\ -3 \end{array} \begin{array}{r} 2 \\ -1 \end{array}$$

$$\begin{aligned} 0 &= x^2 - x - 6 \\ 0 &= (x-3)(x+2) \end{aligned}$$

$$x = 3, -2$$

Solve.

$$(2x-1)^{\frac{3}{4}} - 10 = 17$$

$$\begin{aligned} [(2x-1)^{\frac{3}{4}}]^{\frac{4}{3}} &= (27)^{\frac{4}{3}} \rightarrow (3\sqrt[3]{27})^4 \\ &\quad (3)^4 = 81 \end{aligned}$$

$$\begin{aligned} 2x-1 &= 81 \\ 2x &= 82 \\ x &= 41 \end{aligned}$$

Do you think that there could be extraneous solutions for this equation?

No, since this is an odd radical you can get both a positive and negative number out of that, unlike even radicals which only leads to positive values.

$$(\sqrt[3]{x^2-7})^3 = (\sqrt[3]{x-1})^3$$

Solve.

$$x^2-7 = x-1$$

$$x^2-x-6 = 0$$

$$(x-3)(x+2) = 0$$

$$x = 3, -2$$

$$\begin{array}{r} -6 \\ -3 \end{array} \begin{array}{r} 2 \\ -1 \end{array}$$