

Simplify.

$$2\sqrt{6}(5\sqrt{3} - 4\sqrt{10})$$

$$2\sqrt{6} \cdot 5\sqrt{3} - 2\sqrt{6} \cdot 4\sqrt{10}$$

$$\begin{array}{c} 10 \sqrt{18} \\ \sqrt{9 \cdot 2} \\ 10 \cdot 3\sqrt{2} \end{array} - \begin{array}{c} 8 \sqrt{60} \\ \sqrt{4 \cdot 15} \\ -8 \cdot 2\sqrt{15} \end{array}$$

$$\boxed{30\sqrt{2} - 16\sqrt{15}}$$

Sec 7-3: Binomial Radical Expressions.

Simplify. $(3 + \sqrt{10})(4 - \sqrt{10})$

	$3 + \sqrt{10}$	
4	12	$+4\sqrt{10}$
$-\sqrt{10}$	$-3\sqrt{10}$	-10

 $\Rightarrow \boxed{2 + \sqrt{10}}$

Simplify.

$$(6 - 2\sqrt{7})(5 - 4\sqrt{7})$$

	6	$-2\sqrt{7}$	
5	30	$-10\sqrt{7}$	
$-4\sqrt{7}$	$-24\sqrt{7}$	$8 \cdot 7 = 56$	

 $= \boxed{86 - 34\sqrt{7}}$

Multiply.

$$(5 - \sqrt{2})(6 + \sqrt{3})$$

	5	$-\sqrt{2}$	
6	30	$-6\sqrt{2}$	
$+\sqrt{3}$	$+5\sqrt{3}$	$-\sqrt{6}$	

 $= \boxed{30 - 6\sqrt{2} + 5\sqrt{3} - \sqrt{6}}$

since the radicals are different there are no like terms

Multiply.

$$(3 - 7\sqrt{2})^2$$

$$\begin{array}{r}
 3 \quad -7\sqrt{2} \\
 3 \quad \begin{array}{|c|c|} \hline 9 & -21\sqrt{2} \\ \hline \end{array} \\
 -7\sqrt{2} \quad \begin{array}{|c|c|} \hline -21\sqrt{2} & +49 \cdot 2 \\ \hline \end{array} \\
 = \boxed{107 - 42\sqrt{2}}
 \end{array}$$

$$(3 - 7\sqrt{2})^2$$

$$\begin{aligned}
 & \xrightarrow{(a+b)^2} \\
 & = a^2 + 2ab + b^2 \\
 & = 3^2 - 2(3)(7\sqrt{2}) + (-7\sqrt{2})^2 \\
 & = 9 - 42\sqrt{2} + 49 \cdot 2 \\
 & = 9 - 42\sqrt{2} + 98 \\
 & = \boxed{107 - 42\sqrt{2}}
 \end{aligned}$$

Simplify.

$$(\sqrt{6} - \sqrt{7})^2$$

$$\begin{aligned}
 & \xrightarrow{\begin{array}{c} \uparrow \quad \downarrow \\ a \quad b \end{array}} \\
 & (\sqrt{6})^2 - 2(\sqrt{6})(\sqrt{7}) + (\sqrt{7})^2 \\
 & = 6 - 2\sqrt{42} + 7 \\
 & = \boxed{13 - 2\sqrt{42}}
 \end{aligned}$$

Remember the result when you expand
 $(a + b)(a - b)$ is ALWAYS $= a^2 - b^2$

These factors are called conjugates

Expand and simplify.

$$\begin{aligned}
 & \xrightarrow{\begin{array}{c} a \quad b \end{array}} \\
 & (7 + \sqrt{5})(7 - \sqrt{5}) = (7)^2 - (\sqrt{5})^2 \\
 & = \boxed{49 - 5 = 44}
 \end{aligned}$$

Simplify.

$$(\sqrt{11} + 9)(\sqrt{11} - 9)$$

$$\begin{aligned}
 & = (\sqrt{11})^2 - (9)^2 \\
 & = 11 - 81 \\
 & = \boxed{-70}
 \end{aligned}$$

Simplify.

$$(3\sqrt{2} - 8)(3\sqrt{2} + 8)$$

$a \quad b$

$$= (3\sqrt{2})^2 - (8)^2$$

$$= 9 \cdot 2 - 64$$

$$= 18 - 64$$

$$= \boxed{-46}$$

Simplify.

$$(7\sqrt{2} - 5\sqrt{6})(7\sqrt{2} + 5\sqrt{6})$$

$a \quad b$

$$= (7\sqrt{2})^2 - (5\sqrt{6})^2$$

$$= 49 \cdot 2 - 25 \cdot 6$$

$$= 98 - 150 = \boxed{-52}$$

Rationalize this denominator:

$$\frac{(8 - \sqrt[3]{5})}{\sqrt[3]{5}} \cdot \frac{\sqrt[3]{5^2}}{\sqrt[3]{5^2}} = \frac{8\sqrt[3]{5^2} - \sqrt[3]{5^3}}{\sqrt[3]{5^3}}$$

$$= \boxed{\frac{8\sqrt[3]{5^2} - 5}{5}}$$

Rationalize the denominator.

$$\frac{24}{2 - \sqrt{7}} \cdot \frac{(2 + \sqrt{7})}{2 + \sqrt{7}}$$

$2^2 - (\sqrt{7})^2 = 4 - 7 = -3$

To rationalize a denominator involving a sum or difference involving square roots you multiply the numerator and denominator by the

Conjugate of the Denominator.

$$= \frac{48 + 24\sqrt{7}}{-3} = \boxed{-16 - 8\sqrt{7}}$$

Rationalize the denominator.

$$\frac{11 + \sqrt{5}}{3 - 4\sqrt{5}} \cdot \frac{3 + 4\sqrt{5}}{3 + 4\sqrt{5}} = \frac{53 + 47\sqrt{5}}{-71}$$

$3^2 - (4\sqrt{5})^2$
 $= 9 - 16 \cdot 5$
 $= 9 - 80 = -71$

A purple box shows the FOIL method for the numerator:

	11	+	$\sqrt{5}$
3	33		$3\sqrt{5}$
$4\sqrt{5}$	$44\sqrt{5}$		$4 \cdot 5 = 20$

 An arrow points from the purple box to the numerator of the final result.

You can now finish Hwk #19

Sec 7-3

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Problems 15, 16, 21, 22, 24, 25, 30, 32, 36, 40