

Rationalize each denominator.

1. $\frac{8c}{\sqrt[4]{9a^3b^9c^{14}}}$

2. $\frac{12}{\sqrt[3]{40m^7n^{16}}}$

Simplify each. Assume that all variables are positive. Rationalize denominators.

3. $\sqrt{63g^4h^7} \cdot \sqrt{15g^6h^4}$

4. $\sqrt[3]{49m^5n^{13}} \cdot \sqrt[3]{21m^7n^4}$

5. $\frac{\sqrt{48x^9y^3}}{\sqrt{10x^6y^8}}$

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$$\begin{aligned} \textcircled{1} \quad \frac{8c}{\sqrt[4]{9a^3b^9c^{14}}} &= \frac{8c}{\sqrt[4]{3^2a^3b^9c^{14}}} \cdot \frac{\sqrt[4]{3^2ab^3c^2}}{\sqrt[4]{3^2ab^3c^2}} = \frac{8c\sqrt[4]{9ab^3c^2}}{\sqrt[4]{3^4a^4b^{12}c^{16}}} \\ &= \frac{8c\sqrt[4]{9ab^3c^2}}{3ab^3c^4} \\ &= \boxed{\frac{8\sqrt[4]{9ab^3c^2}}{3ab^3c^3}} \end{aligned}$$

$$\begin{aligned} \textcircled{2} \quad \frac{12}{\sqrt[3]{40m^7n^{16}}} &= \frac{12}{\sqrt[3]{8 \cdot 5m^7n^{16}}} \cdot \frac{\sqrt[3]{5^2m^2n^2}}{\sqrt[3]{5^2m^2n^2}} = \frac{12\sqrt[3]{25m^2n^2}}{\sqrt[3]{8 \cdot 5^3m^9n^{18}}} \\ &= \frac{12\sqrt[3]{25m^2n^2}}{2 \cdot 5 \cdot m^3 \cdot n^6} \\ &= \boxed{\frac{6\sqrt[3]{25m^2n^2}}{5m^3n^6}} \end{aligned}$$

$$\begin{aligned}
 (3) \quad \sqrt[3]{63 g^4 h^7} \cdot \sqrt[3]{15 g^6 h^4} &= \sqrt[3]{3^2 \cdot 105 g^{10} h^{11}} \\
 &= \boxed{3 g^5 h^5 \sqrt[3]{105 h}}
 \end{aligned}$$

$$\begin{aligned}
 (4) \quad \sqrt[3]{49 m^5 n^{13}} \cdot \sqrt[3]{21 m^7 n^4} &= \sqrt[3]{7^3 \cdot 3 m^{12} n^{17}} \\
 &= \boxed{7 m^4 n^5 \sqrt[3]{3 n^2}}
 \end{aligned}$$

$$\begin{aligned}
 (5) \quad \frac{\sqrt{48 x^9 y^3}}{\sqrt{10 x^6 y^8}} &= \frac{\sqrt{24 x^3}}{\sqrt{5 y^5}} \cdot \frac{\sqrt{5 y}}{\sqrt{5 y}} = \frac{\sqrt{120 x^3 y}}{\sqrt{5^2 y^6}} \\
 &= \frac{\sqrt{120 x^3 y}}{5 y^3} = \frac{\sqrt{4 \cdot 30 x^3 y}}{5 y^3} \\
 &= \boxed{\frac{2 x \sqrt{30 x y}}{5 y^3}}
 \end{aligned}$$