

What relationships do you see here?

$$\begin{array}{l} (x+6)^2 = x^2 + 12x + 36 \\ (x-4)^2 = x^2 - 8x + 16 \\ (x+11)^2 = x^2 + 22x + 121 \\ (x-7)^2 = x^2 - 14x + 49 \\ (x+8)^2 = x^2 + 16x + 64 \\ (x-5)^2 = x^2 - 10x + 25 \end{array}$$

$$(x+h)^2 = x^2 + bx + c$$

When expanding,  
b is 2 times h.  
And c is always  
h squared.

Relationships amongst the signs

$$(x \bigcirc h)^2 = x^2 \bigcirc bx \bigcirc c$$

always +  
Same

Fill in the missing values.

$$(x+h)^2 = x^2 + bx + c$$

$$x^2 - 24x + 144 = (x - 12)^2$$

$$x^2 + 18x + 81 = (x + 9)^2$$

$$x^2 - 10x + 25 = (x - 5)^2$$

h is found by either  
finding half of b or  
the square root  
of c

The sign of h is always  
the same as the sign  
of b

Fill in the missing values.

$$x^2 - 20x + 100 = (x - 10)^2$$

2nd:  $2(\sqrt{c})$   
1st:  $\sqrt{c}$

$$x^2 + 6x + 9 = (x + 3)^2$$

2nd:  $2(\sqrt{c})$   
1st:  $\sqrt{c}$

$$x^2 - 2x + 1 = (x - 1)^2$$

2nd:  $2(\sqrt{c})$   
1st:  $\sqrt{c}$

Fill in the missing values.

$$x^2 - 22x + 121 = (x - 11)^2$$

1st:  $b/2$   
2nd:  $(b/2)^2$

$$x^2 + 36x + 324 = (x + 18)^2$$

1st:  $b/2$   
2nd:  $(b/2)^2$

$$x^2 - 4x + 4 = (x - 2)^2$$

1st:  $b/2$   
2nd:  $(b/2)^2$

$$(x + h)^2 = x^2 + bx + c$$

Relationships between  $b$  and  $c$

$$(x - 5)^2 = x^2 - 10x + 25$$

$b = 2 \cdot \sqrt{c}$   
 $c = \left(\frac{b}{2}\right)^2$

$$(x + h)^2 = x^2 + bx + c$$

Relationships between  $h$  and  $c$

$$(x - 5)^2 = x^2 - 10x + 25$$

$h = \sqrt{c}$   
 $c = h^2$

$$(x + h)^2 = x^2 + bx + c$$

Relationships between  $h$  and  $b$

$$(x - 5)^2 = x^2 - 10x + 25$$

$h = \frac{b}{2}$   
 $b = 2 \cdot h$

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Fill in the blanks

$$1. \quad x^2 + 20x + \underline{100} = (x + \underline{10})^2$$

1st:  $b/2$  (from 20 to 10)  
2nd:  $(b/2)^2$  (from 10 to 100)

$$2. \quad x^2 - 4x + \underline{4} = (x - \underline{2})^2$$

1st:  $b/2$  (from -4 to -2)  
2nd:  $(b/2)^2$  (from -2 to 4)

This is called "Completing the Square."

The constant in the trinomial is half of b, squared:  $(b/2)^2$

$$(x - 5)^2 = x^2 - \boxed{10}x + 25$$

$ax^2 + bx + c$

The constant in the parentheses is half of b:  $b/2$

In general, to complete the square:

$$x^2 + 16x + 64 = (x + 8)^2$$

$$x^2 + bx + \left(\frac{b}{2}\right)^2 = \left(x + \frac{b}{2}\right)^2$$

1st: from  $b$  to  $b/2$   
2nd: from  $b/2$  to  $(b/2)^2$

Complete the square for each.

$$1. \quad x^2 - 2x + \underline{1} = (x - \underline{1})^2$$

1st:  $b/2$  (from -2 to -1)  
2nd:  $(b/2)^2$  (from -1 to 1)

$$2. \quad x^2 + 50x + \underline{625} = (x + \underline{25})^2$$

1st:  $b/2$  (from 50 to 25)  
2nd:  $(b/2)^2$  (from 25 to 625)

$$3. \quad x^2 - 3x + \underline{\frac{9}{4}} = \left(x - \underline{\frac{3}{2}}\right)^2$$

1st:  $b/2$  (from -3 to -3/2)  
2nd:  $(b/2)^2$  (from -3/2 to 9/4)

Expand.

$$(2x + 5)^2$$

$$4x^2 + 20x + 25$$

Find the value of  $k$  so that the trinomial will factor into  $(x - h)^2$ .  
Give the value of  $h$  also.

This is called a perfect square trinomial.

$$9x^2 - \underset{42x}{k}x + 49 = (\underset{3x-7}{a}x - \underset{7}{h})^2$$

You can now finish Hwk #19.

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Problems 7-12, 42, 43, 46, 47