

What is matrix Y if

$$\begin{bmatrix} 12 & -27 \\ 9 & 15 \\ -34 & -50 \end{bmatrix} - Y = \begin{bmatrix} 48 & -23 \\ 57 & -2 \\ 0 & 18 \end{bmatrix}$$

You could add Y to both sides first to get

$$\begin{bmatrix} 12 & -27 \\ 9 & 15 \\ -34 & -50 \end{bmatrix} = \begin{bmatrix} 48 & -23 \\ 57 & -2 \\ 0 & 18 \end{bmatrix} + Y$$

Then you could subtract the matrix on the right from both sides to get

$$\begin{bmatrix} 12 & -27 \\ 9 & 15 \\ -34 & -50 \end{bmatrix} - \begin{bmatrix} 48 & -23 \\ 57 & -2 \\ 0 & 18 \end{bmatrix} = Y$$

Now do matrix subtraction to get

$$\begin{bmatrix} -36 & -4 \\ -48 & 17 \\ -34 & -68 \end{bmatrix} = Y$$

Matrices using the graphing calculator.

To enter a matrix on a calculator:

1. **2ND** **MATRIX**  $X^{-1}$  → EDIT
2. Move up/down to pick the matrix you want to use [A]  
then **ENTER**
3. Enter the dimensions for your matrix
4. Enter the data in the matrix

to enter other matrices just repeat this process but use different matrices, i.e. B or C or D.....

When you are finished entering the matrices you must press **2ND** **quit** **mode**  
in order to perform any matrix operations with these matrices.

Enter the following matrices on the calculator.

$$A \begin{bmatrix} 5 & 6 & 3 \\ 0 & -9 & 12 \end{bmatrix} \quad B \begin{bmatrix} 10 & 3 & 9 \\ 17 & -5 & 1 \end{bmatrix} \quad C \begin{bmatrix} -6 & -9 & -1 \\ 20 & -13 & 49 \end{bmatrix}$$

Perform this matrix operation on the calculator:  $A + B$

to get  $[A]+[B]$  on the home screen at this point do the following:

Press **2nd** **MATRIX**  $X^{-1}$  Choose: NAME, 1:[A]

Press +

Press **2nd** **MATRIX**  $X^{-1}$  Choose: NAME, 2:[B]

You will see this on the home screen  $[A]+[B]$  then press **enter**

$$A + B = \begin{bmatrix} 15 & 9 & 12 \\ 17 & -4 & 13 \end{bmatrix}$$

$$A \begin{bmatrix} 5 & 6 & 3 \\ 0 & -9 & 12 \end{bmatrix} \quad B \begin{bmatrix} 10 & 3 & 9 \\ 17 & -5 & 1 \end{bmatrix} \quad C \begin{bmatrix} -6 & -9 & -1 \\ 20 & -13 & 49 \end{bmatrix}$$

Find each

1.  $B - C$

2.  $C - A - B$

3.  $B + C - A$

$$\begin{bmatrix} 15 & 12 & 10 \\ -3 & 8 & -48 \end{bmatrix}$$

$$\begin{bmatrix} -20 & -18 & -13 \\ 3 & 1 & 36 \end{bmatrix}$$

$$\begin{bmatrix} 0 & -12 & 5 \\ 37 & -9 & 38 \end{bmatrix}$$

$$A \begin{bmatrix} 5 & 6 & 3 \\ 0 & -9 & 12 \end{bmatrix} \quad B \begin{bmatrix} 10 & 3 & 9 \\ 17 & -5 & 1 \end{bmatrix} \quad C \begin{bmatrix} -6 & -9 & -1 \\ 20 & -13 & 49 \end{bmatrix}$$

Find this matrix:  $2A = \begin{bmatrix} 10 & 12 & 6 \\ 0 & -18 & 24 \end{bmatrix}$

$$A \begin{bmatrix} 5 & 6 & 3 \\ 0 & -9 & 12 \end{bmatrix} \quad B \begin{bmatrix} 10 & 3 & 9 \\ 17 & -5 & 1 \end{bmatrix} \quad C \begin{bmatrix} -6 & -9 & -1 \\ 20 & -13 & 49 \end{bmatrix}$$

$2A$  is called **scalar** multiplication

A **scalar** is a real number.

When you multiply a matrix by a scalar you multiply each element in the matrix by that scalar.

#### Properties

#### Scalar Multiplication

If  $A$ ,  $B$ , and  $O$  are  $m \times n$  matrices and  $c$  and  $d$  are scalars, then  $cA$  is an  $m \times n$  matrix.

$(cd)A = c(dA)$	Closure Property
$c(A + B) = cA + cB$	Associative Property of Multiplication
$(c + d)A = cA + dA$	Distributive Property
$1 \cdot A = A$	Multiplicative Identity Property
$0 \cdot A = O$ and $cO = O$	Multiplicative Property of Zero

Solve this matrix equation for matrix  $X$ .

$$-3X + 2 \begin{bmatrix} 6 & 9 \\ -12 & 15 \end{bmatrix} = \begin{bmatrix} 27 & -18 \\ 2 & 9 \end{bmatrix}$$

If you define these two matrices using variables:

$$A \begin{bmatrix} 6 & 9 \\ -12 & 15 \end{bmatrix}, \quad B \begin{bmatrix} 27 & -18 \\ 2 & 9 \end{bmatrix}$$

This equation becomes:

$$-3X + 2A = B \quad \text{move } 2A \text{ to the right side by subtracting to get}$$

$$-3X = B - 2A \quad \text{using the calculator you get:}$$

$$-3X = \begin{bmatrix} 15 & -36 \\ -26 & 7 \end{bmatrix} \quad \text{if you tried to divide the matrix on the right side of the equation by } -3 \text{ you'll get an error message because you can't use division when working with matrices. To avoid this error message you can multiply by } -1/3 \text{ instead of dividing by } -3.$$

$$X = \left(-\frac{1}{3}\right) \begin{bmatrix} 15 & -36 \\ -26 & 7 \end{bmatrix} = \begin{bmatrix} -5 & 12 \\ 8.67 & 7 \end{bmatrix}$$

Enter these matrices on the graphing calculator:

$$A \begin{bmatrix} 8 & 5 \\ -3 & 7 \end{bmatrix} \quad B \begin{bmatrix} 10 & 3 & 9 \\ 17 & -5 & 1 \end{bmatrix} \quad C \begin{bmatrix} 4 & 20 \\ 0 & 2 \\ -1 & 6 \end{bmatrix} \quad D \begin{bmatrix} 7 & 13 & 8 \\ -1 & 4 & 10 \end{bmatrix}$$

1. Which matrices can be added?

*B & D only*

2. Which can be subtracted?

*B & D only*

In order to add and subtract matrices they must have the same dimensions.